# Package 'biogrowth'

July 22, 2025

```
Title Modelling of Population Growth
Version 1.0.6
Description Modelling of population growth under static and dynamic environmental conditions.
     Includes functions for model fitting and making prediction under isothermal and
     dynamic conditions. The methods (algorithms & models) are based on
     predictive microbiology (See Perez-Rodriguez and Valero (2012, ISBN:978-1-4614-5519-6)).
License GPL-3
Encoding UTF-8
LazyData true
RoxygenNote 7.2.3
Imports deSolve (>= 1.28), tibble (>= 3.0.3), dplyr (>= 0.8.5), FME
     (>= 1.3.6), MASS (>= 7.3), rlang (>= 0.4.7), purrr (>= 0.3.4),
     ggplot2 (>= 3.3.2), cowplot (>= 1.0.0), lamW (>= 1.3.0), tidyr
     (>= 1.0.2), formula.tools (>= 1.7.1), lifecycle
Suggests knitr, rmarkdown, tidyverse (>= 1.3.0)
VignetteBuilder knitr
Depends R (>= 2.10)
NeedsCompilation no
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Repository CRAN
Date/Publication 2025-03-17 16:50:02 UTC
```

Type Package

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# Description

Generates functions for linear interpolation of environmental conditions

# Usage

```
approx_env(env_conditions)
```

# **Arguments**

env\_conditions A tibble describing the variation of the environmental conditions through the storage time. Must contain a column named time and as many additional columns as environmental factors.

# Value

A list of functions that return the value of each environmental condition for some storage time

arabian\_tractors 5

arabian_tractors	Number of tractors in the Arab World according to the World Bank

# Description

A dataset showing the increase in tractors in the Arab World. It was retrieved from https://data.worldbank.org/indicator/AG.A

# Usage

```
arabian_tractors
```

# **Format**

A tibble with 40 rows (each corresponding to one year) and 7 columns:

```
year Year for the recordingtractors Number of tractors
```

Aryani_model	Secondary Aryani model	

# Description

Secondary model as defined by Aryani et al. (2015).

# Usage

```
Aryani_model(x, xmin, xhalf)
```

# Arguments

X	Value of the environmental factor.
xmin	Minimum value for growth.
xhalf	Value where $gamma = 0.5$

#### Value

The corresponding gamma factor.

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bilinear\_lag

Bilinear model with lag phase

# Description

Bilinear model with lag phase

# Usage

```
bilinear_lag(times, logN0, mu, lambda)
```

# Arguments

times Numeric vector of storage times

logN0 Initial log microbial count

mu Maximum specific growth rate (in ln CFU/t)

lambda Lag phase duration

bilinear\_stationary Bilinear model with stationary phase

# Description

Bilinear model with stationary phase

# Usage

```
bilinear_stationary(times, logN0, mu, logNmax)
```

# **Arguments**

times Numeric vector of storage times

logN0 Initial log microbial count

mu Maximum specific growth rate (in ln CFU/t)

logNmax Maximum log microbial count

calculate\_gammas 7

calcul	ate	gammas

Calculates every gamma factor

#### **Description**

A helper function for predict\_dynamic\_growth() that calculates the value of every gamma factor corresponding to some storage time.

# Usage

```
calculate_gammas(this_t, env_func, sec_models)
```

### **Arguments**

this\_t Storage time

env\_func A list of functions (generated using approxfun) that give the value of each en-

vironmental function for some storage time.

sec\_models A nested list describing the secondary models.

#### Value

A vector of gamma factors (one per environmental factor).

```
calculate_gammas_secondary
```

Gamma factors for fitting secondary models

### **Description**

A helper for fitting the secondary gamma models. Calculates the gamma factors corresponding to the models defined and the experimental conditions. In order for it to work, the environmental factors must be named identically in the 3 arguments.

#### Usage

```
calculate_gammas_secondary(sec_model_names, my_data, secondary_models)
```

### **Arguments**

```
sec_model_names
```

named character vector defining the type of secondary model. Its names correspond to the environmental conditions and its values define the corresponding type of secondary model.

Tibble of experimental conditions.

secondary\_models

my\_data

A list defining the parameters of the secondary models.

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# Value

a numeric vector of length nrow(my\_data) with the gamma factor for each experimental condition.

check\_growth\_guess

Visual check of an initial guess of the model parameters

# Description

# [Stable]

Generates a plot comparing a set of data points against the model prediction corresponding to an initial guess of the model parameters

# Usage

```
check_growth_guess(
  fit_data,
  model_keys,
  guess,
  environment = "constant",
  env_conditions = NULL,
  approach = "single",
  logbase_mu = 10,
  formula = logN ~ time
)
```

# Arguments

fit_data	Tibble (or data.frame) of data for the fit. It must have two columns, one with the elapsed time (time by default) and another one with the decimal logarithm of the population size (logN by default). Different column names can be defined using the formula argument.
model_keys	Named the equations of the secondary model as in fit_growth()
guess	Named vector with the initial guess of the model parameters as in $fit\_growth()$
environment	type of environment. Either "constant" (default) or "dynamic" (see below for details on the calculations for each condition) $\frac{1}{2}$
env_conditions	Tibble describing the variation of the environmental conditions for dynamic experiments. See fit_growth(). Ignored when environment = "constant"
approach	whether "single" (default) or "global". Please see fit_growth() for details."
logbase_mu	Base of the logarithm the growth rate is referred to. By default, 10 (i.e. $\log 10$ ). See vignette about units for details.
formula	an object of class "formula" describing the x and y variables. $logN \sim time$ as a default

check\_growth\_guess 9

#### Value

A ggplot2::ggplot() comparing the model prediction against the data

# **Examples**

```
## Examples under constant environmental conditions ------
## We need some data
my_data <- data.frame(time = 0:9,</pre>
                     logN = c(2, 2.1, 1.8, 2.5, 3.1, 3.4, 4, 4.5, 4.8, 4.7)
## We can directly plot the comparison for some values
check_growth_guess(my_data, list(primary = "modGompertz"),
                  c(logN0 = 1.5, mu = .8, lambda = 4, C = 3)
## Ot it can be combined with the automatic initial guess
check_growth_guess(my_data, list(primary = "modGompertz"),
                  make_guess_primary(my_data, "modGompertz")
## Examples under dynamic environmental conditions -----
## We will use the datasets included in the package
data("example_dynamic_growth")
data("example_env_conditions")
## Model equations are assigned as in fit_growth
sec_models <- list(temperature = "CPM", aw = "CPM")</pre>
## Guesses of model parameters are also defined as in fit_growth
guess <- list(Nmax = 1e4,</pre>
             N0 = 1e0, Q0 = 1e-3,
             mu_opt = 4,
             temperature_n = 1,
             aw_xmax = 1, aw_xmin = .9, aw_n = 1,
              temperature_xmin = 25, temperature_xopt = 35,
              temperature_xmax = 40, aw_xopt = .95
## We can now check our initial guess
check_growth_guess(example_dynamic_growth, sec_models, guess,
                   "dynamic",
                  example_env_conditions)
```

check\_primary\_pars

Basic check of parameters for primary models

# **Description**

Checks that: the model name is correct, the right number of model parameters have been defined and that the parameters have the right names

# Usage

```
check_primary_pars(model_name, pars)
```

### **Arguments**

model\_name Model identifier

pars A named list of model parameters

### Value

If there is no error, the model function.

check\_secondary\_pars Basic checks of secondary parameters

# **Description**

Checks that the model names are correct, that no parameter is defined twice, that every parameter is defined and that no unknown parameter has been defined. Raises an error if any of these conditions is not met.

# Usage

```
check_secondary_pars(
   starting_point,
   known_pars,
   sec_model_names,
   primary_pars = "mu_opt"
)
```

check\_stochastic\_pars 11

# **Arguments**

starting\_point Named vector with initial values for the model parameters to estimate from the

data. The growth rate under optimum conditions must be named mu\_opt. The rest must be called 'env\_factor'+'\_'+'parameter'. For instance, the minimum

pH for growth is 'pH\_xmin'.

known\_pars Named vector of fixed model parameters. Must be named using the same con-

vention as starting\_point.

sec\_model\_names

Named character vector defining the secondary model for each environmental

factor.

primary\_pars Character vector with the parameter names of the primary model.

check\_stochastic\_pars Model definition checks for predict\_stochastic\_growth

#### Description

Does several checks of the model parameters. Besides those by check\_primary\_pars, it checks that corr\_matrix is square, that pars and corr\_matrix have compatible dimensions, and that pars has the correct names.

### Usage

```
check_stochastic_pars(model_name, pars, corr_matrix)
```

#### **Arguments**

model\_name Character describing the primary growth model.

pars A tibble describing the parameter uncertainty (see details).

corr\_matrix Correlation matrix of the model parameters. Defined in the same order as in

pars. An identity matrix by default (uncorrelated parameters).

 ${\tt compare\_growth\_fits} \qquad {\tt \textit{Model comparison and selection for growth models}}$ 

# Description

#### [Experimental]

This function is a constructor for GrowthComparison or GlobalGrowthComparison, a class that provides several functions for model comparison and model selection for growth models fitted using fit\_growth(). Please see the help pages for GrowthComparison or GlobalGrowthComparison for further details.

Although it is not necessary, we recommend passing the models as a named list, as these names will later be kept in plots and tables.

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### Usage

```
compare_growth_fits(models)
```

### **Arguments**

models

a (we recommend named) list of models fitted using fit\_growth(). Every model should be of the same class. Otherwise, some functions may give unexpected results.

### **Examples**

```
## Example 1 - Fitting under static environmental conditions -------
## We will use the data on growth of Salmonella included in the package
data("growth_salmonella")
## We will fit 3 different models to the data
fit1 <- fit_growth(growth_salmonella,</pre>
                   list(primary = "Baranyi"),
                   start = c(lambda = 0, logNmax = 8, mu = .1, logN0 = 2),
                   known = c(),
                   environment = "constant",
                   )
fit2 <- fit_growth(growth_salmonella,</pre>
                   list(primary = "Baranyi"),
                   start = c(logNmax = 8, mu = .1, logN0 = 2),
                   known = c(lambda = 0),
                   environment = "constant",
fit3 <- fit_growth(growth_salmonella,</pre>
                   list(primary = "modGompertz"),
                   start = c(C = 8, mu = .1, logN0 = 2),
                   known = c(lambda = 0),
                   environment = "constant",
                   )
## We can now put them in a (preferably named) list
my_models <- list(`Baranyi` = fit1,</pre>
                   `Baranyi no lag` = fit2,
                  `Gompertz no lag` = fit3)
## And pass them to compare_growth_fits
model_comparison <- compare_growth_fits(my_models)</pre>
## The instance of GrowthComparison has useful S3 methods
```

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```
print(model_comparison)
plot(model_comparison)
plot(model_comparison, type = 2)
plot(model_comparison, type = 3)
## The statistical indexes can be accessed through summary and coef
summary(model_comparison)
coef(model_comparison)
## Example 2 - Fitting under dynamic environmental conditions ------
## We will use one of the example datasets
data("example_dynamic_growth")
data("example_env_conditions")
## First model fitted
sec_models <- list(temperature = "CPM", aw = "CPM")</pre>
known_pars <- list(Nmax = 1e4,</pre>
                   N0 = 1e0, Q0 = 1e-3,
                   mu_opt = 4,
                   temperature_n = 1,
                   aw_xmax = 1, aw_xmin = .9, aw_n = 1
my_start <- list(temperature_xmin = 25, temperature_xopt = 35,</pre>
                 temperature_xmax = 40, aw_xopt = .95)
dynamic_fit <- fit_growth(example_dynamic_growth,</pre>
                           sec_models,
                           my_start, known_pars,
                           environment = "dynamic",
                           env_conditions = example_env_conditions
## Second model (different secondary model for temperature)
sec_models <- list(temperature = "Zwietering", aw = "CPM")</pre>
known_pars <- list(Nmax = 1e4,</pre>
                   N0 = 1e0, Q0 = 1e-3,
                   mu_opt = 4,
                   temperature_n = 1,
                   aw_xmax = 1, aw_xmin = .9, aw_n = 1
                   )
my_start <- list(temperature_xmin = 25, temperature_xopt = 35,</pre>
                 aw\_xopt = .95)
```

```
dynamic_fit2 <- fit_growth(example_dynamic_growth,</pre>
                           sec_models,
                           my_start, known_pars,
                           environment = "dynamic",
                           env_conditions = example_env_conditions
## Once both models have been fitted, we can call the function
dynamic_comparison <- compare_growth_fits(list(m1 = dynamic_fit, m2 = dynamic_fit2))</pre>
## Which also returns an instance of GrowthComparison with the same S3 methods
print(dynamic_comparison)
plot(dynamic_comparison)
plot(dynamic_comparison, type = 2)
plot(dynamic_comparison, type = 3)
## The statistical indexes can be accessed through summary and coef
summary(dynamic_comparison)
coef(dynamic_comparison)
## Example 3 - Global fitting ------
## We use the example data
data("multiple_counts")
data("multiple_conditions")
## We need to fit (at least) two models
sec_models <- list(temperature = "CPM", pH = "CPM")</pre>
known_pars <- list(Nmax = 1e8, N0 = 1e0, Q0 = 1e-3,
                   temperature_n = 2, temperature_xmin = 20,
                   temperature\_xmax = 35,
                   pH_n = 2, pH_xmin = 5.5, pH_xmax = 7.5, pH_xopt = 6.5)
my_start <- list(mu_opt = .8, temperature_xopt = 30)</pre>
global_fit <- fit_growth(multiple_counts,</pre>
                         sec_models,
                         my_start,
                         known_pars,
                         environment = "dynamic",
                         algorithm = "regression",
                         approach = "global",
                         env_conditions = multiple_conditions
```

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```
sec_models <- list(temperature = "CPM", pH = "CPM")</pre>
known_pars <- list(Nmax = 1e8, N0 = 1e0, Q0 = 1e-3,
                   temperature_n = 1, temperature_xmin = 20,
                   temperature\_xmax = 35,
                   pH_n = 2, pH_xmin = 5.5, pH_xmax = 7.5, pH_xopt = 6.5)
my_start <- list(mu_opt = .8, temperature_xopt = 30)</pre>
global_fit2 <- fit_growth(multiple_counts,</pre>
                           sec_models,
                           my_start,
                           known_pars,
                           environment = "dynamic",
                           algorithm = "regression",
                           approach = "global",
                           env_conditions = multiple_conditions
## We can now pass both models to the function as a (named) list
global_comparison <- compare_growth_fits(list(`n=2` = global_fit,</pre>
                                                `n=1` = global_fit2)
## The residuals and model fits plots are divided by experiments
plot(global_comparison)
plot(global_comparison, type = 3)
## The remaining S3 methods are the same as before
print(global_comparison)
plot(global_comparison, type = 2)
summary(global_comparison)
coef(global_comparison)
```

compare\_secondary\_fits

Model comparison and selection for secondary growth models

# Description

# [Experimental]

This function is a constructor for SecondaryComparison a class that provides several functions for model comparison and model selection for growth models fitted using fit\_secondary\_growth(). Please see the help pages for SecondaryComparison for further details.

Although it is not necessary, we recommend passing the models as a named list, as these names will later be kept in plots and tables.

# Usage

```
compare_secondary_fits(models)
```

### **Arguments**

models a (we recommend named) list of models fitted using fit\_secondary\_growth().

### **Examples**

```
## We first need to fit some models
data("example_cardinal")
sec_model_names <- c(temperature = "Zwietering", pH = "CPM")</pre>
known_pars <- list(mu_opt = 1.2, temperature_n = 1,</pre>
                   pH_n = 2, pH_xmax = 6.8, pH_xmin = 5.2)
my_start <- list(temperature_xmin = 5, temperature_xopt = 35,</pre>
                 pH\_xopt = 6.5)
fit1 <- fit_secondary_growth(example_cardinal, my_start, known_pars, sec_model_names)</pre>
known_pars <- list(mu_opt = 1.2, temperature_n = 2,</pre>
                   pH_n = 2, pH_xmax = 6.8, pH_xmin = 5.2)
 fit2 <- fit_secondary_growth(example_cardinal, my_start, known_pars, sec_model_names)</pre>
 ## We can now pass the models to the constructor
 comparison <- compare_secondary_fits(list(`n=1` = fit1,</pre>
                                              `n=2` = fit2))
 ## The function includes several S3 methods for model selection and comparison
 print(comparison)
 plot(comparison)
 plot(comparison, type = 2)
 ## The numerical indexes can be accessed using coef and summary
 coef(comparison)
 summary(comparison)
```

 $conditions\_pH\_temperature$ 

Conditions during a dynamic growth experiment

# **Description**

A dataset to demonstrate the use of fit\_dynamic\_growth. The observations environmental conditions are described in conditions\_pH\_temperature.

# Usage

```
conditions_pH_temperature
```

#### **Format**

A tibble with 4 rows and 3 columns:

```
time elapsed timetemperature temperaturepH pH
```

cost\_coupled\_onestep

Residuals of the coupled Baranyi model

# Description

Residuals of the coupled Baranyi model

# Usage

```
cost_coupled_onestep(p, this_data, known)
```

### **Arguments**

p a numeric vector of model parameters. Must have entries logN0, logNmax,

logC0, b and Tmin

this\_data a tibble (or data.frame) with three columns: logN (microbial concentration; in

logCFU/TIME), temp the temperature and time the storage time

known a numeric vector of known model parameters

# Value

the vector of model residuals

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cost\_coupled\_twosteps Cost for the coupled model fitted in two-steps

# **Description**

Cost for the coupled model fitted in two-steps

#### **Usage**

```
cost_coupled_twosteps(p, this_data, weight = NULL, known)
```

### **Arguments**

p numeric vector (or list) of model parameters. Must have entries logC0, b and

Tmin

this\_data tibble (or data.frame) of data. It must have one column named temp (tempera-

ture), one named lambda (specific growth rate; in ln CFU/TIME) and one named

mu (specific growth rate; in ln CFU/TIME).

weight type of weights to apply. Either NULL (no weights; default), sd (standard devia-

tion) or mean (mean value).

known vector of known model parameters

### Value

vector of weighted residuals

CPM\_model Secondary Cardinal Parameter (CPM) model

# Description

Secondary cardinal parameter model as defined by Rosso et al. (1995).

### Usage

```
CPM_model(x, xmin, xopt, xmax, n)
```

# Arguments

X	Value of the environmental factor.
xmin	Minimum value for growth.
xopt	Optimum value for growth.
xmax	Maximum value for growth.
n	Order of the CPM model.

dBaranyi 19

### Value

The corresponding gamma factor.

dBaranyi	Baranyi growth model	
----------	----------------------	--

# Description

Microbial growth model as defined in Baranyi and Roberts (1994). It has been implemented according to the requirements of deSolve::ode(). For consistency in the function for isothermal growth, calculations are done assuming the user input for mu is in log10 scale. In other words, the input is multiplied by ln(10).

### Usage

```
dBaranyi(time, state, pars, env_func, sec_models)
```

# Arguments

time	numeric vector (length	1) of storage time

state named numeric vector with two components: Q and N

pars named numeric vector of model parameters (Nmax and mu\_opt)

env\_func named list of functions returning the values of the environmental conditions for

time (t)

sec\_models named list of parameters of the secondary model

### Value

A numeric vector of two components according to the requirements of deSolve::ode().

```
distribution_to_logcount
```

Distribution of times to reach a certain microbial count

# **Description**

### [Superseded]

The function distribution\_to\_logcount() has been superseded by function time\_to\_size(), which provides more general interface.

Returns the probability distribution of the storage time required for the microbial count to reach log\_count according to the predictions of a stochastic model. Calculations are done using linear interpolation of the individual model predictions.

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### Usage

```
distribution_to_logcount(model, log_count)
```

### **Arguments**

model An instance of StochasticGrowth or MCMCgrowth.

log\_count The target microbial count.

### Value

An instance of TimeDistribution().

# **Examples**

DynamicGrowth

DynamicGrowth class

# Description

### [Superseded]

The class DynamicGrowth has been superseded by the top-level class GrowthPrediction, which provides a unified approach for growth modelling.

Still, it is returned if the superseded predict\_dynamic\_growth() is called.

A subclass of list with items:

• simulation: A tibble with the model prediction

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- gammas: A tibble with the value of each gamma factor for each value of times.
- env\_conditions: A list of functions interpolating the environmental conditions.
- primary\_pars: A list with the model parameters of the primary model.
- sec\_models: A nested list defining the secondary models.

# Usage

```
## S3 method for class 'DynamicGrowth'
print(x, ...)
## S3 method for class 'DynamicGrowth'
plot(
  Х,
 y = NULL,
  add_factor = NULL,
 ylims = NULL,
  label_y1 = "logN",
  label_y2 = add_factor,
  line_col = "black",
  line_size = 1,
  line_type = "solid",
  line_col2 = "black",
  line\_size2 = 1,
  line_type2 = "dashed",
  label_x = "time"
)
## S3 method for class 'DynamicGrowth'
coef(object, ...)
```

# **Arguments**

X	The object of class DynamicGrowth to plot.
	ignored
У	ignored
add_factor	whether to plot also one environmental factor. If NULL (default), no environmental factor is plotted. If set to one character string that matches one entry of x\$env_conditions, that condition is plotted in the secondary axis
ylims	A two dimensional vector with the limits of the primary y-axis.
label_y1	Label of the primary y-axis.
label_y2	Label of the secondary y-axis.
line_col	Aesthetic parameter to change the colour of the line geom in the plot, see: ggplot2::geom_line()
line_size	Aesthetic parameter to change the thickness of the line geom in the plot, see: ggplot2::geom_line()

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line_type	Aesthetic parameter to change the type of the line geom in the plot, takes numbers (1-6) or strings ("solid") see: ggplot2::geom_line()
line_col2	Same as lin_col, but for the environmental factor.
line_size2	Same as line_size, but for the environmental factor.
line_type2	Same as lin_type, but for the environmental factor.
label_x	Label of the x-axis.
object	an instance of DynamicGrowth

# Methods (by generic)

• print(DynamicGrowth): print of the model

• plot(DynamicGrowth): predicted growth curve under dynamic conditions.

• coef(DynamicGrowth): coefficients of the model

example\_cardinal Growth rates obtained for several growth experiments

# Description

An example dataset illustrating the requirements of the fit\_secondary\_growth() function.

# Usage

```
example_cardinal
```

### **Format**

A data frame with 64 rows and 3 variables:

```
temperature storage temperature (°C)pH pH of the mediamu specific growth rate (log10 CFU/h)
```

example\_coupled\_onestep

Example data for two-steps fitting of the Baranyi-Ratkowsky model

# **Description**

This dataset serve as an example of the data input for fit\_coupled\_growth using the one-step mode

# Usage

example\_coupled\_onestep

#### **Format**

A tibble with three columns:

- temp: the treatment temperature
- time: the elapsed time of the sample
- logN: the (decimal) log microbial concentration

example\_coupled\_twosteps

Example data for two-steps fitting of the Baranyi-Ratkowsky model

# **Description**

This dataset serve as an example of the data input for fit\_coupled\_growth using the two-steps mode.

### Usage

example\_coupled\_twosteps

### **Format**

A tibble with three columns:

- temp: the treatment temperature
- mu: the value of mu estimated at each temperature
- lambda: the value of lambda estimated at each temperature

```
example_dynamic_growth
```

Microbial growth under dynamic conditions

# Description

An example dataset illustrating the requirements of the fit\_dynamic\_growth() function.

# Usage

```
example_dynamic_growth
```

#### **Format**

A data frame with 30 rows and 2 variables:

```
time elapsed time (h)
```

logN log population size (log10 CFU)

```
example_env_conditions
```

Environmental conditions during a dynamic experiment

# Description

An example dataset illustrating the requirements of the fit\_dynamic\_growth() function.

# Usage

```
example_env_conditions
```

### **Format**

A data frame with 3 rows and 3 variables:

```
time elapsed time (h)
```

**temperature** storage temperature (°C)

aw water activity

extract\_primary\_pars 25

extract\_primary\_pars A helper to build the primary models

# **Description**

Most of the functions for fitting mix in the vectors parameters for the primary and secondary models, but the functions for making predictions need that they are separated. This one extracts the parameters of the primary model.

### Usage

```
extract_primary_pars(this_p, known_pars)
```

### **Arguments**

this\_p A named vector of model parameters (usually, the ones fitted).

known\_pars Another named vector of model parameters (usually the known ones).

#### Value

A list with the parameters of the primary model

```
extract_secondary_pars
```

A helper to build the secondary models

### **Description**

Most of the functions for fitting mix in the vectors parameters for the primary and secondary models, but the functions for making predictions need that they are separated. This one extracts the parameters of the secondary model.

# Usage

```
extract_secondary_pars(this_p, known_pars, sec_model_names)
```

# **Arguments**

this\_p A named vector of model parameters (usually, the ones fitted).

known\_pars Another named vector of model parameters (usually the known ones).

sec\_model\_names

A named character vector defining for each environmental factor (vector names)

the type of secondary model (vector values).

### Value

A nested list defining the secondary models.

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FitCoupledGrowth

FitCoupledGrowth class

# Description

The FitCoupledGrowth class contains a Baranyi model fitted to experimental data considering the coupling between the primary and secondary models. Its constructor is fit\_coupled\_growth().

It is a subclass of list with the items:

- fit: object returned by FME::modFit().
- mode: fitting approach.
- weight: type of weights for the two-steps approach.
- logbase\_mu: base of the logarithm used for the calculation of mu.
- data: data used for the model fitting.

# Usage

```
## S3 method for class 'FitCoupledGrowth'
print(x, ...)
## S3 method for class 'FitCoupledGrowth'
coef(object, ...)
## S3 method for class 'FitCoupledGrowth'
summary(object, ...)
## S3 method for class 'FitCoupledGrowth'
predict(object, newdata = NULL, ...)
## S3 method for class 'FitCoupledGrowth'
residuals(object, ...)
## S3 method for class 'FitCoupledGrowth'
vcov(object, ...)
## S3 method for class 'FitCoupledGrowth'
deviance(object, ...)
## S3 method for class 'FitCoupledGrowth'
fitted(object, ...)
## S3 method for class 'FitCoupledGrowth'
logLik(object, ...)
## S3 method for class 'FitCoupledGrowth'
AIC(object, ..., k = 2)
```

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```
## S3 method for class 'FitCoupledGrowth'
plot(
    x,
    y = NULL,
    ...,
    line_col = "black",
    line_type = 1,
    point_col = "black",
    point_size = 3,
    point_shape = 16,
    label_y = NULL,
    label_x = NULL
)
```

### **Arguments**

The object of class FitCoupledGrowth to plot. Χ ignored. . . . object an instance of FitCoupledGrowth tibble (or data.frame) with the conditions for the prediction. If NULL (default), newdata the fitting conditions. For two\_steps fits, it must have a column named temp. For one\_step, it must have a column named temp and one named time. penalty for the parameters (k=2 by default) k ignored line\_col colour of the line line\_size size of the line type of the line line\_type point\_col colour of the points point\_size size of the points point\_shape shape of the point label\_y label for the y-axis. By default, NULL (default value depending on the mode) label\_x label for the x-axis. By default, NULL (default value depending on the mode)

### Methods (by generic)

- print(FitCoupledGrowth): print of the model
- coef(FitCoupledGrowth): vector of fitted model parameters.
- summary(FitCoupledGrowth): statistical summary of the fit.
- predict(FitCoupledGrowth): vector of model predictions.
- residuals(FitCoupledGrowth): vector of model residuals.
- vcov(FitCoupledGrowth): variance-covariance matrix of the model, estimated as 1/(0.5\*Hessian) for regression

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- deviance(FitCoupledGrowth): deviance of the model.
- fitted(FitCoupledGrowth): vector of fitted values.
- logLik(FitCoupledGrowth): loglikelihood of the model
- AIC(FitCoupledGrowth): Akaike Information Criterion
- plot(FitCoupledGrowth): compares the fitted model against the data.

FitDynamicGrowth

FitDynamicGrowth class

# Description

# [Superseded]

The class FitDynamicGrowth has been superseded by the top-level class GrowthFit, which provides a unified approach for growth modelling.

Still, it is still returned if the superseded fit\_dynamic\_growth() is called.

It is a subclass of list with the items:

- fit\_results: the object returned by modFit.
- best\_prediction: the model prediction for the fitted parameters.
- env\_conditions: environmental conditions for the fit.
- data: data used for the fit.
- starting: starting values for model fitting
- known: parameter values set as known.
- sec\_models: a named vector with the secondary model for each environmental factor

### Usage

```
## S3 method for class 'FitDynamicGrowth'
print(x, ...)
## S3 method for class 'FitDynamicGrowth'
plot(
    x,
    y = NULL,
    ...,
    add_factor = NULL,
    ylims = NULL,
    label_y1 = "logN",
    label_y2 = add_factor,
    line_col = "black",
    line_type = 1,
    point_col = "black",
```

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```
point_size = 3,
  point_shape = 16,
  line_col2 = "black",
  line\_size2 = 1,
  line_type2 = "dashed"
)
## S3 method for class 'FitDynamicGrowth'
summary(object, ...)
## S3 method for class 'FitDynamicGrowth'
residuals(object, ...)
## S3 method for class 'FitDynamicGrowth'
coef(object, ...)
## S3 method for class 'FitDynamicGrowth'
vcov(object, ...)
## S3 method for class 'FitDynamicGrowth'
deviance(object, ...)
## S3 method for class 'FitDynamicGrowth'
fitted(object, ...)
## S3 method for class 'FitDynamicGrowth'
predict(object, times = NULL, newdata = NULL, ...)
## S3 method for class 'FitDynamicGrowth'
logLik(object, ...)
## S3 method for class 'FitDynamicGrowth'
AIC(object, ..., k = 2)
```

#### **Arguments**

x	The object of class FitDynamicGrowth to plot.
	ignored
у	ignored
add_factor	whether to plot also one environmental factor. If NULL (default), no environmental factor is plotted. If set to one character string that matches one entry of x\$env_conditions, that condition is plotted in the secondary axis
ylims	A two dimensional vector with the limits of the primary y-axis.
label_y1	Label of the primary y-axis.
label_y2	Label of the secondary y-axis.
line_col	Aesthetic parameter to change the colour of the line geom in the plot, see: ggplot2::geom_line()

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line_size	Aesthetic parameter to change the thickness of the line geom in the plot, see: ggplot2::geom_line()
line_type	Aesthetic parameter to change the type of the line geom in the plot, takes numbers (1-6) or strings ("solid") see: ggplot2::geom_line()
point_col	Aesthetic parameter to change the colour of the point geom, see: ggplot2::geom_point()
point_size	Aesthetic parameter to change the size of the point geom, see: ggplot2::geom_point()
point_shape	Aesthetic parameter to change the shape of the point geom, see: ggplot2::ggplot2::geom_point()
line_col2	Same as lin_col, but for the environmental factor.
line_size2	Same as line_size, but for the environmental factor.
line_type2	Same as lin_type, but for the environmental factor.
object	an instance of FitDynamicGrowth
times	A numeric vector with the time points for the simulations. NULL by default (using the same time points as those for the simulation).
newdata	a tibble describing the environmental conditions (as env_conditions) in predict_dynamic_growth(). If NULL (default), uses the same conditions as those for fitting.
k	penalty for the parameters (k=2 by default)

# Methods (by generic)

- print(FitDynamicGrowth): comparison between the fitted model and the data.
- plot(FitDynamicGrowth): comparison between the fitted model and the data.
- summary(FitDynamicGrowth): statistical summary of the fit.
- residuals(FitDynamicGrowth): residuals of the model.
- coef(FitDynamicGrowth): vector of fitted parameters.
- vcov(FitDynamicGrowth): (unscaled) variance-covariance matrix of the model, calculated as 1/(0.5\*Hessian)
- deviance(FitDynamicGrowth): deviance of the model.
- fitted(FitDynamicGrowth): fitted values.
- predict(FitDynamicGrowth): model predictions.
- $\bullet \ \ log Lik (\texttt{FitDynamicGrowth}): \ log like lihood \ of \ the \ model$
- AIC(FitDynamicGrowth): Akaike Information Criterion

# **Description**

# [Superseded]

The class FitDynamicGrowthMCMC has been superseded by the top-level class GrowthFit, which provides a unified approach for growth modelling.

Still, it is returned if the superseded fit\_MCMC\_growth() is called.

It is a subclass of list with the items:

- fit\_results: the object returned by modMCMC.
- best\_prediction: the model prediction for the fitted parameters.
- env\_conditions: environmental conditions for the fit.
- data: data used for the fit.
- starting: starting values for model fitting
- known: parameter values set as known.
- sec\_models: a named vector with the secondary model for each environmental factor

### Usage

```
## S3 method for class 'FitDynamicGrowthMCMC'
print(x, ...)
## S3 method for class 'FitDynamicGrowthMCMC'
plot(
  х,
 y = NULL,
  add_factor = NULL,
  ylims = NULL,
  label_y1 = "logN",
  label_y2 = add_factor,
  line_col = "black",
  line_size = 1,
  line_type = 1,
  point_col = "black",
  point_size = 3,
  point_shape = 16,
  line_col2 = "black",
  line_size2 = 1,
  line_type2 = "dashed"
```

```
## S3 method for class 'FitDynamicGrowthMCMC'
summary(object, ...)
## S3 method for class 'FitDynamicGrowthMCMC'
residuals(object, ...)
## S3 method for class 'FitDynamicGrowthMCMC'
coef(object, ...)
## S3 method for class 'FitDynamicGrowthMCMC'
vcov(object, ...)
## S3 method for class 'FitDynamicGrowthMCMC'
deviance(object, ...)
## S3 method for class 'FitDynamicGrowthMCMC'
fitted(object, ...)
## S3 method for class 'FitDynamicGrowthMCMC'
predict(object, times = NULL, newdata = NULL, ...)
## S3 method for class 'FitDynamicGrowthMCMC'
logLik(object, ...)
## S3 method for class 'FitDynamicGrowthMCMC'
AIC(object, ..., k = 2)
## S3 method for class 'FitDynamicGrowthMCMC'
predictMCMC(
 model,
  times,
  env_conditions,
 niter,
  newpars = NULL,
  formula = . \sim time
)
```

#### **Arguments**

x The object of class FitDynamicGrowthMCMC to plot.
... ignored
y ignored
add\_factor whether to plot also one environmental factor. If NULL (default), no environmenta factor is plotted. If set to one character string that matches one entry of x\$env\_conditions, that condition is plotted in the secondary axis
ylims A two dimensional vector with the limits of the primary y-axis.
label\_y1 Label of the primary y-axis.

label_y2	Label of the secondary y-axis.
line_col	Aesthetic parameter to change the colour of the line geom in the plot, see: ggplot2::geom_line()
line_size	Aesthetic parameter to change the thickness of the line geom in the plot, see: ggplot2::geom_line()
line_type	Aesthetic parameter to change the type of the line geom in the plot, takes numbers (1-6) or strings ("solid") see: ggplot2::geom_line()
point_col	Aesthetic parameter to change the colour of the point geom, see: ggplot2::geom_point()
point_size	Aesthetic parameter to change the size of the point geom, see: ggplot2::geom_point()
point_shape	Aesthetic parameter to change the shape of the point geom, see: ggplot2::geom_point()
line_col2	Same as lin_col, but for the environmental factor.
line_size2	Same as line_size, but for the environmental factor.
line_type2	Same as lin_type, but for the environmental factor.
object	an instance of FitDynamicGrowthMCMC
times	Numeric vector of storage times for the predictions.
newdata	a tibble describing the environmental conditions (as env_conditions) in predict_dynamic_growth(). If NULL (default), uses the same conditions as those for fitting.
k	penalty for the parameters (k=2 by default)
model	An instance of FitDynamicGrowthMCMC
env_conditions	Tibble with the (dynamic) environmental conditions during the experiment. It must have one column named 'time' with the storage time and as many columns as required with the environmental conditions.
niter	Number of iterations.
newpars	A named list defining new values for the some model parameters. The name must be the identifier of a model already included in the model. These parameters do not include variation, so defining a new value for a fitted parameters "fixes" it. NULL by default (no new parameters).
formula	A formula stating the column named defining the elapsed time in env_conditions. By default, . ~ time.

### Value

An instance of MCMCgrowth().

# Methods (by generic)

- print(FitDynamicGrowthMCMC): print of the model
- plot(FitDynamicGrowthMCMC): compares the model fitted against the data.
- summary(FitDynamicGrowthMCMC): statistical summary of the fit.
- residuals(FitDynamicGrowthMCMC): model residuals.
- coef(FitDynamicGrowthMCMC): vector of fitted model parameters.

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• vcov(FitDynamicGrowthMCMC): variance-covariance matrix of the model, estimated as the variance of the samples from the Markov chain.

- deviance(FitDynamicGrowthMCMC): deviance of the model, calculated as the sum of squared residuals for the parameter values resulting in the best fit.
- fitted(FitDynamicGrowthMCMC): vector of fitted values.
- predict(FitDynamicGrowthMCMC): vector of model predictions.
- logLik(FitDynamicGrowthMCMC): loglikelihood of the model
- AIC(FitDynamicGrowthMCMC): Akaike Information Criterion
- predictMCMC(FitDynamicGrowthMCMC): prediction including parameter uncertainty

FitIsoGrowth

FitIsoGrowth class

### **Description**

# [Superseded]

The class FitIsoGrowth has been superseded by the top-level class GrowthFit, which provides a unified approach for growth modelling.

Still, it is still returned if the superseded fit\_isothermal\_growth() is called.

It is a subclass of list with the items:

- · data: data used for model fitting
- model: name of the primary inactivation model
- starting\_point: initial value of the model parameters
- known: fixed model parameters
- fit: object returned by FME::modFit()
- best\_prediction: model prediction for the model fitted.

### Usage

```
## S3 method for class 'FitIsoGrowth'
print(x, ...)

## S3 method for class 'FitIsoGrowth'
plot(
    x,
    y = NULL,
    ...,
    line_col = "black",
    line_type = 1,
    point_col = "black",
    point_size = 3,
```

FitIsoGrowth 35

```
point_shape = 16
## S3 method for class 'FitIsoGrowth'
summary(object, ...)
## S3 method for class 'FitIsoGrowth'
residuals(object, ...)
## S3 method for class 'FitIsoGrowth'
coef(object, ...)
## S3 method for class 'FitIsoGrowth'
vcov(object, ...)
## S3 method for class 'FitIsoGrowth'
deviance(object, ...)
## S3 method for class 'FitIsoGrowth'
fitted(object, ...)
## S3 method for class 'FitIsoGrowth'
predict(object, times = NULL, ...)
## S3 method for class 'FitIsoGrowth'
logLik(object, ...)
## S3 method for class 'FitIsoGrowth'
AIC(object, ..., k = 2)
```

# Arguments

x	The object of class FitIsoGrowth to plot.
	ignored
у	ignored
line_col	Aesthetic parameter to change the colour of the line geom in the plot, see: ggplot2::geom_line()
line_size	Aesthetic parameter to change the thickness of the line geom in the plot, see: ggplot2::geom_line()
line_type	Aesthetic parameter to change the type of the line geom in the plot, takes numbers (1-6) or strings ("solid") see: ggplot2::geom_line()
point_col	Aesthetic parameter to change the colour of the point geom, see: ggplot2::geom_point()
point_size	Aesthetic parameter to change the size of the point geom, see: ggplot2::geom_point()
point_shape	Aesthetic parameter to change the shape of the point geom, see: ggplot2::geom_point()
object	an instance of FitIsoGrowth

times numeric vector describing the time points for the prediction. If NULL (default), uses the same points as those used for fitting.

k penalty for the parameters (k=2 by default)

# Methods (by generic)

- print(FitIsoGrowth): print of the model
- plot(FitIsoGrowth): compares the fitted model against the data.
- summary(FitIsoGrowth): statistical summary of the fit.
- residuals(FitIsoGrowth): vector of model residuals.
- coef(FitIsoGrowth): vector of fitted model parameters.
- vcov(FitIsoGrowth): variance-covariance matrix of the model, estimated as 1/(0.5\*Hessian)
- deviance(FitIsoGrowth): deviance of the model.
- fitted(FitIsoGrowth): vector of fitted values.
- predict(FitIsoGrowth): vector of model predictions.
- logLik(FitIsoGrowth): loglikelihood of the model
- AIC(FitIsoGrowth): Akaike Information Criterion

FitMultipleDynamicGrowth

FitMultipleDynamicGrowth class

### **Description**

# [Superseded]

The class FitMultipleDynamicGrowth has been superseded by the top-level class GlobalGrowthFit, which provides a unified approach for growth modelling.

Still, it is still returned if the superseded fit\_multiple\_growth() is called.

It is a subclass of list with the items:

- fit\_results: the object returned by modFit.
- best\_prediction: a list with the models predictions for each condition.
- data: a list with the data used for the fit.
- starting: starting values for model fitting
- known: parameter values set as known.
- sec\_models: a named vector with the secondary model for each environmental factor.

```
## S3 method for class 'FitMultipleDynamicGrowth'
print(x, ...)
## S3 method for class 'FitMultipleDynamicGrowth'
plot(
  х,
 y = NULL
  . . . ,
  add_factor = NULL,
 ylims = NULL,
  label_x = "time",
  label_y1 = "logN",
  label_y2 = add_factor,
  line_col = "black",
  line_size = 1,
  line_type = "solid",
  line_col2 = "black",
  line\_size2 = 1,
  line_type2 = "dashed",
  point_size = 3,
  point_shape = 16,
  subplot_labels = "AUTO"
)
## S3 method for class 'FitMultipleDynamicGrowth'
summary(object, ...)
## S3 method for class 'FitMultipleDynamicGrowth'
residuals(object, ...)
## S3 method for class 'FitMultipleDynamicGrowth'
coef(object, ...)
## S3 method for class 'FitMultipleDynamicGrowth'
vcov(object, ...)
## S3 method for class 'FitMultipleDynamicGrowth'
deviance(object, ...)
## S3 method for class 'FitMultipleDynamicGrowth'
fitted(object, ...)
## S3 method for class 'FitMultipleDynamicGrowth'
predict(object, env_conditions, times = NULL, ...)
## S3 method for class 'FitMultipleDynamicGrowth'
logLik(object, ...)
```

```
## S3 method for class 'FitMultipleDynamicGrowth'
AIC(object, ..., k = 2)
```

# **Arguments**

X	an instance of FitMultipleDynamicGrowth.
• • •	ignored
У	ignored
add_factor	whether to plot also one environmental factor. If NULL (default), no environmental factor is plotted. If set to one character string that matches one entry of $x$ env_conditions, that condition is plotted in the secondary axis
ylims	A two dimensional vector with the limits of the primary y-axis.
label_x	label of the x-axis
label_y1	Label of the primary y-axis.
label_y2	Label of the secondary y-axis.
line_col	Aesthetic parameter to change the colour of the line geom in the plot, see: ggplot2::geom_line()
line_size	Aesthetic parameter to change the thickness of the line geom in the plot, see: ggplot2::geom_line()
line_type	Aesthetic parameter to change the type of the line geom in the plot, takes numbers (1-6) or strings ("solid") see: ggplot2::geom_line()
line_col2	Same as lin_col, but for the environmental factor.
line_size2	Same as line_size, but for the environmental factor.
line_type2	Same as lin_type, but for the environmental factor.
point_size	Size of the data points
point_shape	shape of the data points
subplot_labels	labels of the subplots according to plot_grid.
object	an instance of FitMultipleDynamicGrowth
env_conditions	a tibble describing the environmental conditions (as in $fit\_multiple\_growth().$
times	A numeric vector with the time points for the simulations. NULL by default (using the same time points as the ones defined in env_conditions).
k	penalty for the parameters (k=2 by default)

# Methods (by generic)

- print(FitMultipleDynamicGrowth): print of the model
- plot(FitMultipleDynamicGrowth): comparison between the fitted model and the experimental data.
- summary(FitMultipleDynamicGrowth): statistical summary of the fit.
- residuals(FitMultipleDynamicGrowth): calculates the model residuals. Returns a tibble with 4 columns: time (storage time), logN (observed count), exp (name of the experiment) and res (residual).

- coef(FitMultipleDynamicGrowth): vector of fitted parameters.
- vcov(FitMultipleDynamicGrowth): (unscaled) variance-covariance matrix, estimated as 1/(0.5\*Hessian).
- deviance(FitMultipleDynamicGrowth): deviance of the model.
- fitted(FitMultipleDynamicGrowth): fitted values. They are returned as a tibble with 3 columns: time (storage time), exp (experiment identifier) and fitted (fitted value).
- predict(FitMultipleDynamicGrowth): vector of model predictions
- logLik(FitMultipleDynamicGrowth): loglikelihood of the model
- AIC(FitMultipleDynamicGrowth): Akaike Information Criterion

 ${\tt FitMultipleGrowthMCMC}\ \ \textit{FitMultipleGrowthMCMC}\ \ \textit{class}$ 

#### **Description**

# [Superseded]

The class FitMultipleGrowthMCMC has been superseded by the top-level class GlobalGrowthFit, which provides a unified approach for growth modelling.

Still, it is still returned if the superseded fit\_multiple\_growth\_MCMC() is called.

It is a subclass of list with the items:

- fit results: the object returned by modFit.
- best\_prediction: a list with the models predictions for each condition.
- data: a list with the data used for the fit.
- starting: starting values for model fitting
- known: parameter values set as known.
- sec\_models: a named vector with the secondary model for each environmental factor.

```
## S3 method for class 'FitMultipleGrowthMCMC'
print(x, ...)

## S3 method for class 'FitMultipleGrowthMCMC'
plot(
    x,
    y = NULL,
    ...,
    add_factor = NULL,
    ylims = NULL,
    label_x = "time",
    label_y1 = "logN",
    label_y2 = add_factor,
```

```
line_col = "black",
  line\_size = 1,
  line_type = "solid",
  line_col2 = "black",
  line\_size2 = 1,
  line_type2 = "dashed",
  point_size = 3,
  point_shape = 16,
  subplot_labels = "AUTO"
)
## S3 method for class 'FitMultipleGrowthMCMC'
summary(object, ...)
## S3 method for class 'FitMultipleGrowthMCMC'
residuals(object, ...)
## S3 method for class 'FitMultipleGrowthMCMC'
coef(object, ...)
## S3 method for class 'FitMultipleGrowthMCMC'
vcov(object, ...)
## S3 method for class 'FitMultipleGrowthMCMC'
deviance(object, ...)
## S3 method for class 'FitMultipleGrowthMCMC'
fitted(object, ...)
## S3 method for class 'FitMultipleGrowthMCMC'
predict(object, env_conditions, times = NULL, ...)
## S3 method for class 'FitMultipleGrowthMCMC'
logLik(object, ...)
## S3 method for class 'FitMultipleGrowthMCMC'
AIC(object, ..., k = 2)
## S3 method for class 'FitMultipleGrowthMCMC'
predictMCMC(
 model,
  times,
  env_conditions,
 niter,
 newpars = NULL,
  formula = . \sim time
)
```

#### **Arguments**

x an instance of FitMultipleGrowthMCMC	
----------------------------------------	--

y ignored

add\_factor whether to plot also one environmental factor. If NULL (default), no environ-

mental factor is plotted. If set to one character string that matches one entry of

111010

x\$env\_conditions, that condition is plotted in the secondary axis

ylims A two dimensional vector with the limits of the primary y-axis.

CE: 3 f 1: 1 G

label\_x label of the x-axis

label\_y1 Label of the primary y-axis.
label\_y2 Label of the secondary y-axis.

line\_col Aesthetic parameter to change the colour of the line geom in the plot, see:

ggplot2::geom\_line()

line\_size Aesthetic parameter to change the thickness of the line geom in the plot, see:

ggplot2::geom\_line()

line\_type Aesthetic parameter to change the type of the line geom in the plot, takes num-

bers (1-6) or strings ("solid") see: ggplot2::geom\_line()

line\_col2 Same as lin\_col, but for the environmental factor.

line\_size2 Same as line\_size, but for the environmental factor.

Same as line\_type2 Same as line type, but for the environmental factor.

point\_size Size of the data points
point\_shape shape of the data points

 $subplot_labels \ labels \ of the \ subplots \ according \ to \ plot_grid.$ 

object an instance of FitMultipleGrowthMCMC

env\_conditions Tibble with the (dynamic) environmental conditions during the experiment. It

must have one column named 'time' with the storage time and as many columns

as required with the environmental conditions.

times Numeric vector of storage times for the predictions.

k penalty for the parameters (k=2 by default)
model An instance of FitMultipleGrowthMCMC

niter Number of iterations.

newpars A named list defining new values for the some model parameters. The name

must be the identifier of a model already included in the model. These parameters do not include variation, so defining a new value for a fitted parameters

"fixes" it. NULL by default (no new parameters).

formula A formula stating the column named defining the elapsed time in env\_conditions.

By default, . ~ time.

#### Value

An instance of MCMCgrowth().

42 FitSecondaryGrowth

## Methods (by generic)

- print(FitMultipleGrowthMCMC): print of the model
- plot(FitMultipleGrowthMCMC): comparison between the model fitted and the data.
- summary(FitMultipleGrowthMCMC): statistical summary of the fit.
- residuals(FitMultipleGrowthMCMC): model residuals. They are returned as a tibble with 4 columns: time (storage time), logN (observed count), exp (name of the experiment) and res (residual).
- coef(FitMultipleGrowthMCMC): vector of fitted model parameters.
- vcov(FitMultipleGrowthMCMC): variance-covariance matrix of the model, estimated as the variance of the samples from the Markov chain.
- deviance(FitMultipleGrowthMCMC): deviance of the model, calculated as the sum of squared residuals of the prediction with the lowest standard error.
- fitted(FitMultipleGrowthMCMC): fitted values of the model. They are returned as a tibble with 3 columns: time (storage time), exp (experiment identifier) and fitted (fitted value).
- predict(FitMultipleGrowthMCMC): model predictions. They are returned as a tibble with 3 columns: time (storage time), logN (observed count), and exp (name of the experiment).
- logLik(FitMultipleGrowthMCMC): loglikelihood of the model
- AIC(FitMultipleGrowthMCMC): Akaike Information Criterion
- predictMCMC(FitMultipleGrowthMCMC): prediction including parameter uncertainty

FitSecondaryGrowth

FitSecondaryGrowth class

#### **Description**

The FitSecondaryGrowth class contains a model fitted to a set of growth rates gathered under a variety of static conditions. Its constructor is fit\_secondary\_growth().

It is a subclass of list with the items:

- fit\_results: object returned by FME::modFit().
- secondary\_model: secondary model fitted to the data.
- mu\_opt\_fit: estimated growth rate under optimum conditions.
- data: data used for the fit.
- transformation: type of transformation of mu for the fit.

FitSecondaryGrowth 43

# Usage

```
## S3 method for class 'FitSecondaryGrowth'
print(x, ...)
## S3 method for class 'FitSecondaryGrowth'
plot(x, y = NULL, ..., which = 1, add_trend = FALSE, add_segment = FALSE)
## S3 method for class 'FitSecondaryGrowth'
summary(object, ...)
## S3 method for class 'FitSecondaryGrowth'
residuals(object, ...)
## S3 method for class 'FitSecondaryGrowth'
coef(object, ...)
## S3 method for class 'FitSecondaryGrowth'
vcov(object, ...)
## S3 method for class 'FitSecondaryGrowth'
deviance(object, ...)
## S3 method for class 'FitSecondaryGrowth'
fitted(object, ...)
## S3 method for class 'FitSecondaryGrowth'
predict(object, newdata = NULL, ...)
## S3 method for class 'FitSecondaryGrowth'
logLik(object, ...)
## S3 method for class 'FitSecondaryGrowth'
AIC(object, ..., k = 2)
```

#### **Arguments**

X	An instance of FitSecondaryGrowth.
	ignored
у	ignored.
which	A numeric with the type of plot. 1 for obs versus predicted (default), 2 for gamma curve
add_trend	Whether to add a trend line (only for which=2)
add_segment	Whether to join the observed and fitted points (only for which=2)
object	an instance of FitSecondaryGrowth
newdata	A tibble describing the environmental conditions as in fit_secondary_growth(). If NULL, it uses the same conditions as for model fitting (default).
k	penalty for the parameters (k=2 by default)

44 fit\_coupled\_growth

## Methods (by generic)

- print(FitSecondaryGrowth): print of the model
- plot(FitSecondaryGrowth): plots to evaluate the goodness of the fit.
- summary(FitSecondaryGrowth): statistical summary of the fit.
- residuals(FitSecondaryGrowth): vector of model residuals.
- coef(FitSecondaryGrowth): vector of fitted model parameters.
- vcov(FitSecondaryGrowth): variance-covariance matrix of the model, estimated as 1/(0.5\*Hessian)
- deviance(FitSecondaryGrowth): deviance of the model.
- fitted(FitSecondaryGrowth): vector of fitted values.

  The fitted values are returned in the same scale as the one used for the fitting (sqrt, log or none).
- predict(FitSecondaryGrowth): vector of model predictions.
- logLik(FitSecondaryGrowth): loglikelihood of the model
- AIC(FitSecondaryGrowth): Akaike Information Criterion

fit\_coupled\_growth Growth fitting considering link between mu and lambda for the Baranyi-Ratkowsky model

### Description

# [Experimental]

This function implements the methodology suggested by Garre et al. (2025; doi: 10.1016/j.ijfoodmicro.2025.111078) for the Baranyi-Ratkowsky model. Rather than fitting independent models for mu and lambda, this approach considers a link between both secondary models, reducing the number of unknown parameters from 3 to 4.

The function implements too modes of fitting: two-steps and one-step. Please see the respective sections for further information.

```
fit_coupled_growth(
  fit_data,
  start,
  known = c(),
  mode = "two_steps",
  weight = "sd",
   ...,
  logbase_mu = exp(1),
  logbase_logN = 10
)
```

fit\_coupled\_growth 45

# Arguments

fit_data	a tibble (or data.frame) with the data for the fit. The content must be different depending on the fitting mode (see relevant sections within the help page).
start	a numeric vector of initial guesses for the parameter estimates
known	a numeric vector of known mode parameters. An empty vector by default (no knonw parameter)
mode	the type of model fitting approach. Either two_steps (fitted from the values of mu and lambda) or one_step (fitted from logN)
weight	weights to apply for the two_steps fit. Either NULL (no weights), sd (standard deviation; default) or mean (mean value).
	ignored
logbase_mu	Base for the definition of mu. By default, exp(1) (natural logarithm).
logbase_logN	Base for the definition of logN. By default, 10 (decimal logarithm).

# Two-steps fitting

In this mode, it is assumed that primary models have been already fitted to each experiment. Therefore, the data is available as a table of values of mu and lambda estimated at each temperature. Hence, fit\_data must be a tibble (or data.frame) with three columns: temp (storage temperature), mu (specific growth rate) and lambda (lag phase duration). By default, mu must be defined in the scale of natural logarithm, although this can be modified using the logbase\_mu argument. The package includes the dataset example\_coupled\_twosteps as an illustration of the type of data.

# **One-step fitting**

In this mode, secondary models are directly fitted to the observed (log) microbial counts. Hence, fit\_data must be a tibble (or data.frame) with three columns: temp (storage temperature), time (the elapsed time) and logN (the log-microbial concentration). By default, logN must be defined in the scale of decimal logarithm, although this can be modified using the logbase\_logN argument. The package includes the dataset example\_coupled\_onestep as an illustration of the type of data.

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```
## Common S3 methods are included
print(my_fit)
coef(my_fit)
summary(my_fit)
plot(my_fit)
## Any model parameter can be fixed using the known argument
known \leftarrow c(b = .01)
## Please note that the guess must be updated, as now parameter can appear both as a guess and known
guess <- c(logC0 = -1, Tmin = 0)
fixed_fit <- fit_coupled_growth(example_coupled_twosteps,</pre>
                               start = guess,
                               known = known,
                               mode = "two_steps")
print(fixed_fit)
coef(fixed_fit)
summary(fixed_fit)
plot(fixed_fit)
## Example 2: One-step fitting-------
## We can use an example dataset with the right format
data("example_coupled_onestep")
## The function requires initial guesses for every model parameter
guess <- c(logN0 = 2, logNmax = 8, b = 0.04, logC0 = -4, Tmin = 5)
## We can now call the fitting function
my_fit <- fit_coupled_growth(example_coupled_onestep,</pre>
                            start = guess,
                            mode = "one_step")
## The package includes common S3 methods
print(my_fit)
coef(my_fit)
summary(my_fit)
plot(my_fit)
## Any model parameter can be fixed before fitting
known <- c(logNmax = 7)
```

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fit\_dynamic\_growth

Fit dynamic growth models

# Description

# [Superseded]

The function fit\_dynamic\_growth() has been superseded by the top-level function fit\_growth(), which provides a unified approach for growth modelling.

Nonetheless, it can still fit a growth model to data obtained under dynamic conditions using the one-step approach (non-linear regression).

```
fit_dynamic_growth(
  fit_data,
  env_conditions,
  starting_point,
  known_pars,
  sec_model_names,
  ...,
  check = TRUE,
  logbase_mu = logbase_logN,
  logbase_logN = 10,
  formula = logN ~ time
)
```

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#### **Arguments**

fit\_data Tibble with the data to use for model fit. It must contain a column with the

elapsed time (named "time" by default) and another one with the decimal logarithm of the observed population size (named "logN" by default). Different

column names can be specified using the "formula" argument.

env\_conditions Tibble with the (dynamic) environmental conditions during the experiment. It

must have one column with the elapsed time (named "time" by default) and as many columns as required with the environmental conditions. A different column name can be specified using the "formula" argument, although it must be the same one as in "fit\_data". Note that only those defined in "sec\_model\_names"

will be considered for the model fit.

starting\_point A named vector of starting values for the model parameters. Parameters for the

primary model must be named in the usual way. Parameters for the secondary model are named as env\_factor+'\_'+parameter. For instance, the maximum

growth temperature shall be named 'temperature\_xmax'.

known\_pars A named vector of known model parameters (i.e. not fitted). They must be

named using the same convention as for starting\_point.

sec\_model\_names

A named character vector defining the secondary model for each environmental factor. The names define the factor and the value the type of model. Names must

match columns in fit\_data and env\_conditions.

... Additional arguments passed to modFit.

check Whether to check model parameters (TRUE by default).

logbase\_mu Base of the logarithm the growth rate is referred to. By default, the same as

logbase\_logN. See vignette about units for details.

logbase\_logN Base of the logarithm for the population size. By default, 10 (i.e. log10). See

vignette about units for details.

formula an object of class "formula" describing the x and y variables.  $logN \sim time$  as a

default.

#### Value

An instance of FitDynamicGrowth().

```
## We use the datasets included in the package

data("example_dynamic_growth")
data("example_env_conditions")

## Define the secondary models

sec_model_names <- c(temperature = "CPM", aw= "CPM")

## Any model parameter can be fixed</pre>
```

```
known_pars <- list(Nmax = 1e4, # Primary model</pre>
    N0 = 1e0, Q0 = 1e-3, # Initial values of the primary model
   mu_opt = 4, # mu_opt of the gamma model
    temperature_n = 1, # Secondary model for temperature
   aw_xmax = 1, aw_xmin = .9, aw_n = 1 # Secondary model for water activity
## The remaining parameters need initial values
my_start <- list(temperature_xmin = 25, temperature_xopt = 35,</pre>
    temperature_xmax = 40, aw_xopt = .95)
## We can now call the fitting function
my_dyna_fit <- fit_dynamic_growth(example_dynamic_growth, example_env_conditions,</pre>
    my_start, known_pars, sec_model_names)
summary(my_dyna_fit)
## We can compare the data and the fitted curve
plot(my_dyna_fit)
## We can plot any environmental condition using add_factor
plot(my_dyna_fit, add_factor = "aw",
    label_y1 = "Log count (log CFU/ml)",
    label_y2 = "Water activity")
```

fit\_growth

Fitting microbial growth

# Description

#### [Stable]

This function provides a top-level interface for fitting growth models to data describing the variation of the population size through time, either under constant or dynamic environment conditions. See below for details on the calculations.

```
fit_growth(
  fit_data,
  model_keys,
  start,
  known,
  environment = "constant",
```

```
algorithm = "regression",
approach = "single",
env_conditions = NULL,
niter = NULL,
...,
check = TRUE,
logbase_mu = logbase_logN,
logbase_logN = 10,
formula = logN ~ time
)
```

# Arguments

fit_data	observed microbial growth. The format varies depending on the type of model fit. See the relevant sections (and examples) below for details.
model_keys	a named list assigning equations for the primary and secondary models. See the relevant sections (and examples) below for details.
start	a named numeric vector assigning initial guesses to the model parameters to estimate from the data. See relevant section (and examples) below for details.
known	named numeric vector of fixed model parameters, using the same conventions as for "start".
environment	type of environment. Either "constant" (default) or "dynamic" (see below for details on the calculations for each condition)
algorithm	either "regression" (default; Levenberg-Marquard algorithm) or "MCMC" (Adaptive Monte Carlo algorithm).
approach	approach for model fitting. Either "single" (the model is fitted to a unique experiment) or "global" (the model is fitted to several dynamic experiments).
env_conditions	Tibble describing the variation of the environmental conditions for dynamic experiments. See the relevant sections (and examples) below for details. Ignored for environment="constant".
niter	number of iterations of the MCMC algorithm. Ignored when algorithm!="MCMC"
	Additional arguments for FME::modFit().
check	Whether to check the validity of the models. TRUE by default.
logbase_mu	Base of the logarithm the growth rate is referred to. By default, the same as logbase_logN. See vignette about units for details.
logbase_logN	Base of the logarithm for the population size. By default, 10 (i.e. log10). See vignette about units for details.
formula	An object of class "formula" defining the names of the $x$ and $y$ variables in the data. $logN \sim time$ as a default.

# Value

If approach="single, an instance of GrowthFit. If approach="multiple", an instance of GlobalGrowthFit

Please check the help pages of each class for additional information.

#### Fitting under constant conditions

When environment="constant", the functions fits a primary growth model to the population size observed during an experiment. In this case, the data has to be a tibble (or data.frame) with two columns:

- time: the elapsed time
- logN: the logarithm of the observed population size Nonetheless, the names of the columns can be modified with the formula argument.

The model equation is defined through the model\_keys argument. It must include an entry named "primary" assigned to a model. Valid model keys can be retrieved calling primary\_model\_data().

The model is fitted by non-linear regression (using FME::modFit()). This algorithm needs initial guesses for every model parameter. This are defined as a named numeric vector. The names must be valid model keys, which can be retrieved using primary\_model\_data() (see example below). Apart from that, any model parameter can be fixed using the "known" argument. This is a named numeric vector, with the same convenctions as "start".

# Fitting under dynamic conditions to a single experiment

When environment="constant" and approach="single", a dynamic growth model combining the Baranyi primary growth model with the gamma approach for the effect of the environmental conditions on the growth rate is fitted to an experiment gathered under dynamic conditions. In this case, the data is similar to fitting under constant conditions: a tibble (or data frame) with two columns:

- time: the elapsed time
- logN: the logarithm of the observed population size Note that these default names can be changed using the formula argument.

The values of the experimental conditions during the experiment are defined using the "env\_conditions" argument. It is a tibble (or data.frame) with one column named ("time") defining the elapsed time. Note that this default name can be modified using the formula argument of the function. The tibble needs to have as many additional columns as environmental conditions included in the model, providing the values of the environmental conditions.

The model equations are defined through the model\_keys argument. It must be a named list where the names match the column names of "env\_conditions" and the values are model keys. These can be retrieved using secondary\_model\_data().

The model can be fitted using regression (FME::modFit()) or an adaptive Monte Carlo algorithm (FME::modMCMC()). Both algorithms require initial guesses for every model parameter to fit. These are defined through the named numeric vector "start". Each parameter must be named as *factor+*"\_"+parameter, where *factor* is the name of the environmental factor defined in "model\_keys". The *parameter* is a valid key that can be retrieved from secondary\_model\_data(). For instance, parameter Xmin for the factor temperature would be defined as "temperature\_xmin".

Note that the argument ... allows passing additional arguments to the fitting functions.

#### Fitting under dynamic conditions to multiple experiments (global fitting)

When environment="constant" and approach="global", fit\_growth tries to find the vector of model parameters that best describe the observations of several growth experiments.

The input requirements are very similar to the case when approach="single". The models (equations, initial guesses, known parameters, algorithms...) are identical. The only difference is that "fit\_data" must be a list, where each element describes the results of an experiment (using the same conventions as when approach="single"). In a similar fashion, "env\_conditions" must be a list describing the values of the environmental factors during each experiment. Although it is not mandatory, it is recommended that the elements of both lists are named. Otherwise, the function assigns automatically-generated names, and matches them by order.#'

```
## Example 1 - Fitting a primary model -----
## A dummy dataset describing the variation of the population size
my_{data} \leftarrow data.frame(time = c(0, 25, 50, 75, 100),
                     logN = c(2, 2.5, 7, 8, 8))
## A list of model keys can be gathered from
primary_model_data()
## The primary model is defined as a list
models <- list(primary = "Baranyi")</pre>
## The keys of the model parameters can also be gathered from primary_model_data
primary_model_data("Baranyi")$pars
## Any model parameter can be fixed
known \leftarrow c(mu = .2)
## The remaining parameters need initial guesses
start < c(logNmax = 8, lambda = 25, logN0 = 2)
primary_fit <- fit_growth(my_data, models, start, known,</pre>
                          environment = "constant",
## The instance of FitIsoGrowth includes several useful methods
print(primary_fit)
plot(primary_fit)
coef(primary_fit)
summary(primary_fit)
## time_to_size can be used to calculate the time for some concentration
time_to_size(primary_fit, 4)
```

```
## Example 2 - Fitting under dynamic conditions-----
## We will use the example data included in the package
data("example_dynamic_growth")
## And the example environmental conditoins (temperature & aw)
data("example_env_conditions")
## Valid keys for secondary models can be retrived from
secondary_model_data()
## We need to assign a model equation (secondary model) to each environmental factor
sec_models <- list(temperature = "CPM", aw = "CPM")</pre>
## The keys of the model parameters can be gathered from the same function
secondary_model_data("CPM")$pars
## Any model parameter (of the primary or secondary models) can be fixed
known_pars <- list(Nmax = 1e4, # Primary model</pre>
                  N0 = 1e0, Q0 = 1e-3, # Initial values of the primary model
                  mu_opt = 4, # mu_opt of the gamma model
                   temperature_n = 1, # Secondary model for temperature
                aw_xmax = 1, aw_xmin = .9, aw_n = 1 # Secondary model for water activity
                  )
## The rest, need initial guesses (you know, regression)
my_start <- list(temperature_xmin = 25, temperature_xopt = 35,</pre>
                 temperature_xmax = 40, aw_xopt = .95)
## We can now fit the model
dynamic_fit <- fit_growth(example_dynamic_growth,</pre>
                          sec_models,
                          my_start, known_pars,
                          environment = "dynamic",
                          env_conditions = example_env_conditions
## The instance of FitDynamicGrowth has several S3 methods
plot(dynamic_fit, add_factor = "temperature")
summary(dynamic_fit)
## We can use time_to_size to calculate the time required to reach a given size
```

```
time_to_size(dynamic_fit, 3)
## Example 3- Fitting under dynamic conditions using MCMC ------
## We can reuse most of the arguments from the previous example
## We just need to define the algorithm and the number of iterations
set.seed(12421)
MCMC_fit <- fit_growth(example_dynamic_growth,</pre>
                       sec_models,
                       my_start, known_pars,
                       environment = "dynamic",
                       env_conditions = example_env_conditions,
                       algorithm = "MCMC",
                       niter = 1000
                       )
## The instance of FitDynamicGrowthMCMC has several S3 methods
plot(MCMC_fit, add_factor = "aw")
summary(MCMC_fit)
## We can use time_to_size to calculate the time required to reach a given size
time_to_size(MCMC_fit, 3)
## It can also make growth predictions including uncertainty
uncertain_growth <- predictMCMC(MCMC_fit,</pre>
                                seq(0, 10, length = 1000),
                                example_env_conditions,
                                niter = 1000)
## The instance of MCMCgrowth includes several nice S3 methods
plot(uncertain_growth)
print(uncertain_growth)
## time_to_size can calculate the time to reach some count
time_to_size(uncertain_growth, 2)
time_to_size(uncertain_growth, 2, type = "distribution")
## Example 4 - Fitting a unique model to several dynamic experiments ------
## We will use the data included in the package
data("multiple_counts")
```

```
data("multiple_conditions")
## We need to assign a model equation for each environmental factor
sec_models <- list(temperature = "CPM", pH = "CPM")</pre>
## Any model parameter (of the primary or secondary models) can be fixed
known_pars <- list(Nmax = 1e8, N0 = 1e0, Q0 = 1e-3,
                   temperature_n = 2, temperature_xmin = 20,
                   temperature\_xmax = 35,
                   pH_n = 2, pH_xmin = 5.5, pH_xmax = 7.5, pH_xopt = 6.5)
## The rest, need initial guesses
my_start <- list(mu_opt = .8, temperature_xopt = 30)</pre>
## We can now fit the model
global_fit <- fit_growth(multiple_counts,</pre>
                         sec_models,
                         my_start,
                         known_pars,
                          environment = "dynamic",
                         algorithm = "regression",
                          approach = "global",
                          env_conditions = multiple_conditions
## The instance of FitMultipleDynamicGrowth has nice S3 methods
plot(global_fit)
summary(global_fit)
print(global_fit)
## We can use time_to_size to calculate the time to reach a given size
time_to_size(global_fit, 4.5)
## Example 5 - MCMC fitting a unique model to several dynamic experiments ---
## Again, we can re-use all the arguments from the previous example
## We just need to define the right algorithm and the number of iterations
## On top of that, we will also pass upper and lower bounds to modMCMC
set.seed(12421)
global_MCMC <- fit_growth(multiple_counts,</pre>
                          sec_models,
                         my_start,
```

```
known_pars,
                         environment = "dynamic",
                         algorithm = "MCMC",
                         approach = "global",
                         env_conditions = multiple_conditions,
                         niter = 1000,
                         lower = c(.2, 29), # lower limits of the model parameters
                         upper = c(.8, 34) # upper limits of the model parameters
## The instance of FitMultipleDynamicGrowthMCMC has nice S3 methods
plot(global_MCMC)
summary(global_MCMC)
print(global_MCMC)
## We can use time_to_size to calculate the time to reach a given size
time_to_size(global_MCMC, 3)
## It can also be used to make model predictions with parameter uncertainty
uncertain_prediction <- predictMCMC(global_MCMC,</pre>
                                    seq(0, 50, length = 1000),
                                    multiple_conditions[[1]],
                                    niter = 100
## The instance of MCMCgrowth includes several nice S3 methods
plot(uncertain_growth)
print(uncertain_growth)
## time_to_size can calculate the time to reach some count
time_to_size(uncertain_growth, 2)
time_to_size(uncertain_growth, 2, type = "distribution")
```

fit\_isothermal\_growth Fit primary growth models

# **Description**

#### [Superseded]

The function fit\_isothermal\_growth() has been superseded by the top-level function fit\_growth(), which provides a unified approach for growth modelling.

Nonetheless, it can still fit a primary growth model to data obtained under static environmental conditions.

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#### Usage

```
fit_isothermal_growth(
   fit_data,
   model_name,
   starting_point,
   known_pars,
   ...,
   check = TRUE,
   formula = logN ~ time,
   logbase_mu = logbase_logN,
   logbase_logN = 10
)
```

## **Arguments**

fit\_data Tibble of data for the fit. It must have two columns, one with the elapsed time

(time by default) and another one with the decimal logarithm of the population size (logN by default). Different column names can be defined using the

formula argument.

model\_name Character defining the primary growth model

starting\_point Named vector of initial values for the model parameters.

known\_pars Named vector of known model parameters (not fitted).

 $... Additional \ arguments \ passed \ to \ FME::modFit().$ 

check Whether to do some basic checks (TRUE by default).

formula an object of class "formula" describing the x and y variables. logN ~ time as a

default.

logbase\_mu Base of the logarithm the growth rate is referred to. By default, the same as

logbase\_logN. See vignette about units for details.

logbase\_logN Base of the logarithm for the population size. By default, 10 (i.e. log10). See

vignette about units for details.

#### Value

An instance of FitIsoGrowth().

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```
## Initial values for the model parameters
start = c(logNmax = 8, lambda = 25, logN0 = 2)
## Any model parameter can be fixed
known <- c(mu = .2)
## Now, we can call the function
static_fit <- fit_isothermal_growth(my_data, my_model, start, known)
summary(static_fit)
## We can plot the fitted model against the observations
plot(static_fit)</pre>
```

fit\_MCMC\_growth

Fit growth models using MCMC

# **Description**

# [Superseded]

The function fit\_MCMC\_growth() has been superseded by the top-level function fit\_growth(), which provides a unified approach for growth modelling.

But, it can still fit a growth model to a data obtained under dynamic conditions using the one-step approach (MCMC algorithm).

```
fit_MCMC_growth(
   fit_data,
   env_conditions,
   starting_point,
   known_pars,
   sec_model_names,
   niter,
   ...,
   check = TRUE,
   formula = logN ~ time,
   logbase_mu = logbase_logN,
   logbase_logN = 10
)
```

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#### **Arguments**

fit\_data Tibble with the data to use for model fit. It must contain a column with the

elapsed time (named "time" by default) and another one with the decimal logarithm of the observed population size (named "logN" by default). Different

column names can be specified using the "formula" argument.

env\_conditions Tibble with the (dynamic) environmental conditions during the experiment. It

must have one column with the elapsed time (named "time" by default) and as many columns as required with the environmental conditions. A different column name can be specified using the "formula" argument, although it must be the same one as in "fit\_data". Note that only those defined in "sec\_model\_names"

will be considered for the model fit.

starting\_point A named vector of starting values for the model parameters. Parameters for the

primary model must be named in the usual way. Parameters for the secondary model are named as env\_factor+'\_'+parameter. For instance, the maximum

growth temperature shall be named 'temperature\_xmax'.

known\_pars A named vector of known model parameters (i.e. not fitted). They must be

named using the same convention as for starting\_point.

sec\_model\_names

A named character vector defining the secondary model for each environmental factor. The names define the factor and the value the type of model. Names must

match columns in fit\_data and env\_conditions.

niter number of iterations of the MCMC algorithm.

. . . Additional arguments passed to modFit.

check Whether to check model parameters (TRUE by default).

formula an object of class "formula" describing the x and y variables. logN ~ time as a

default.

logbase\_mu Base of the logarithm the growth rate is referred to. By default, the same as

logbase\_logN. See vignette about units for details.

logbase\_logN Base of the logarithm for the population size. By default, 10 (i.e. log10). See

vignette about units for details.

## Value

An instance of FitDynamicGrowthMCMC().

```
## We use the example data included in the package
data("example_dynamic_growth")
data("example_env_conditions")

## Definition of the secondary models
sec_model_names <- c(temperature = "CPM", aw= "CPM")

## Any model parameter can be fixed</pre>
```

60 fit\_multiple\_growth

```
known_pars <- list(Nmax = 1e4, # Primary model</pre>
    N0 = 1e0, Q0 = 1e-3, # Initial values of the primary model
    mu_opt = 4, # mu_opt of the gamma model
    temperature_n = 1, # Secondary model for temperature
    aw_xmax = 1, aw_xmin = .9, aw_n = 1 # Secondary model for water activity
## We need starting values for the remaining parameters
my_start <- list(temperature_xmin = 25, temperature_xopt = 35,</pre>
     temperature\_xmax = 40,
    aw\_xopt = .95)
## We can now call the fitting function
set.seed(12124) # Setting seed for repeatability
\label{eq:my_MCMC_fit} $$\operatorname{MCMC\_growth}(\operatorname{example\_dynamic\_growth}, \ \operatorname{example\_env\_conditions}, \ \operatorname{my_MCMC\_fit} <- \ \operatorname{fit\_MCMC\_growth}(\operatorname{example\_dynamic\_growth}, \ \operatorname{example\_env\_conditions}, \ \operatorname{my_MCMC\_fit}) $$
    my_start, known_pars, sec_model_names, niter = 3000)
## Always check the MCMC chain!!
plot(my_MCMC_fit$fit_results)
## We can compare data against fitted curve
plot(my_MCMC_fit)
## Any environmental factor can be included using add_factor
plot(my_MCMC_fit, add_factor = "temperature",
     label_y1 = "Count (log CFU/ml)", label_y2 = "Temperature (C)")
```

### Description

#### [Superseded]

The function fit\_multiple\_growth() has been superseded by the top-level function fit\_growth(), which provides a unified approach for growth modelling.

But, if you so wish, this function still enables fitting a growth model using a dataset comprised of several experiments with potentially different dynamic experimental conditions. Note that the definition of secondary models must comply with the secondary\_model\_data function.

fit\_multiple\_growth 61

#### Usage

```
fit_multiple_growth(
    starting_point,
    experiment_data,
    known_pars,
    sec_model_names,
    ...,
    check = TRUE,
    formula = logN ~ time,
    logbase_mu = logbase_logN,
    logbase_logN = 10
)
```

#### **Arguments**

starting\_point a named vector of starting values for the model parameters. experiment\_data

a nested list with the experimental data. Each entry describes one experiment as a list with two elements: data and conditions. data is a tibble with a column giving the elapsed time (named "time" by default) and another one with the decimal logarithm of the population size (named "logN" by default). conditions is a tibble with one column giving the elapsed time (using the same name as data) and as many additional columns as environmental factors. The default column names can be changed with the formula argument.

known\_pars named vector of known model parameters

sec\_model\_names

named character vector with names of the environmental conditions and values

of the secondary model (see secondary\_model\_data).

... additional arguments for FME::modFit().

check Whether to check the validity of the models. TRUE by default.

formula an object of class "formula" describing the x and y variables. logN ~ time as a

default.

logbase\_mu Base of the logarithm the growth rate is referred to. By default, the same as

logbase\_logN. See vignette about units for details.

logbase\_logN Base of the logarithm for the population size. By default, 10 (i.e. log10). See

vignette about units for details.

### Value

An instance of FitMultipleDynamicGrowth().

```
## We will use the multiple_experiments data set
data("multiple_experiments")
```

```
## For each environmental factor, we need to defined a model
sec_names <- c(temperature = "CPM", pH = "CPM")</pre>
## Any model parameter can be fixed
known <- list(Nmax = 1e8, N0 = 1e0, Q0 = 1e-3,
    temperature_n = 2, temperature_xmin = 20, temperature_xmax = 35,
   pH_n = 2, pH_xmin = 5.5, pH_xmax = 7.5, pH_xopt = 6.5)
## The rest require starting values for model fitting
start <- list(mu_opt = .8, temperature_xopt = 30)</pre>
## We can now call the fitting function
global_fit <- fit_multiple_growth(start, multiple_experiments, known, sec_names)</pre>
## Parameter estimates can be retrieved with summary
summary(global_fit)
## We can compare fitted model against observations
plot(global_fit)
## Any single environmental factor can be added to the plot using add_factor
plot(global_fit, add_factor = "temperature")
```

fit\_multiple\_growth\_MCMC

Fitting growth models to multiple dynamic experiments using MCMC

# Description

# [Superseded]

The function fit\_multiple\_growth\_MCMC() has been superseded by the top-level function fit\_growth(), which provides a unified approach for growth modelling.

However, this functions can still be used to fit a growth model using a dataset comprised of several experiments with potentially different dynamic experimental conditions.

```
fit_multiple_growth_MCMC(
   starting_point,
   experiment_data,
```

```
known_pars,
sec_model_names,
niter,
...,
check = TRUE,
formula = logN ~ time,
logbase_mu = logbase_logN,
logbase_logN = 10
```

#### **Arguments**

starting\_point a named vector of starting values for the model parameters. experiment\_data

a nested list with the experimental data. Each entry describes one experiment as a list with two elements: data and conditions. data is a tibble with a column giving the elapsed time (named "time" by default) and another one with the decimal logarithm of the population size (named "logN" by default). conditions is a tibble with one column giving the elapsed time (using the same name as data) and as many additional columns as environmental factors. The default column names can be changed with the formula argument.

known\_pars named vector of known model parameters

sec\_model\_names

named character vector with names of the environmental conditions and values

of the secondary model (see secondary\_model\_data).

niter number of samples of the MCMC algorithm.

additional arguments for FME::modMCMC (e.g. upper and lower bounds).

check Whether to check the validity of the models. TRUE by default.

formula an object of class "formula" describing the x and y variables. logN ~ time as a

default.

logbase\_mu Base of the logarithm the growth rate is referred to. By default, the same as

logbase\_logN. See vignette about units for details.

logbase\_logN Base of the logarithm for the population size. By default, 10 (i.e. log10). See

vignette about units for details.

### Value

An instance of FitMultipleGrowthMCMC().

```
## We will use the multiple_experiments data set
data("multiple_experiments")
## For each environmental factor, we need to defined a model
```

```
sec_names <- c(temperature = "CPM", pH = "CPM")</pre>
## Any model parameter can be fixed
known <- list(Nmax = 1e8, N0 = 1e0, Q0 = 1e-3,
   temperature_n = 2, temperature_xmin = 20, temperature_xmax = 35,
   pH_n = 2, pH_xmin = 5.5, pH_xmax = 7.5, pH_xopt = 6.5)
## The rest require starting values for model fitting
start <- list(mu_opt = .8, temperature_xopt = 30)</pre>
## We can now call the fitting function
set.seed(12412)
global_MCMC <- fit_multiple_growth_MCMC(start, multiple_experiments, known, sec_names, niter = 1000,</pre>
  lower = c(.2, 29), # lower limits of the model parameters
  upper = c(.8, 34)) # upper limits of the model parameters
## Parameter estimates can be retrieved with summary
summary(global_MCMC)
## We can compare fitted model against observations
plot(global_MCMC)
## Any single environmental factor can be added to the plot using add_factor
plot(global_MCMC, add_factor = "temperature")
```

fit\_secondary\_growth Fit secondary growth models

### Description

# [Stable]

Fits a secondary growth model to a set of growth rates obtained experimentally. Modelling is done according to the gamma concept proposed by Zwietering (1992) and cardinal parameter models.

```
fit_secondary_growth(
  fit_data,
  starting_point,
  known_pars,
  sec_model_names,
```

fit\_secondary\_growth 65

```
transformation = "sq",
...,
check = TRUE,
formula = mu ~ .
```

# Arguments

fit\_data Tibble with the data used for the fit. It must have one column with the observed

growth rate (named mu by default; can be changed using the "formula" argument)

and as many columns as needed with the environmental factors.

starting\_point Named vector with initial values for the model parameters to estimate from the

data. The growth rate under optimum conditions must be named mu\_opt. The rest must be called 'env\_factor'+'\_'+'parameter'. For instance, the minimum

pH for growth is 'pH\_xmin'.

known\_pars Named vector of fixed model parameters. Must be named using the same con-

vention as starting\_point.

sec\_model\_names

Named character vector defining the secondary model for each environmental

factor.

transformation Character defining the transformation of mu for model fitting. One of sq (square

root; default), log (log-transform) or none (no transformation).

... Additional arguments passed to FME::modFit().

check Whether to do some basic checks (TRUE by default).

formula an object of class "formula" describing the y variable. The right hand side must

be ".". By default mu ~ ..

#### Value

An instance of FitSecondaryGrowth().

66 full\_Ratkowski

full\_Ratkowski

Full Ratkowsky model

# Description

Gamma model adapted from the one by Ratkowsky et al. (1983).

### Usage

```
full_Ratkowski(x, xmin, xmax, c)
```

# **Arguments**

x Value of the environmental factor.

xmin Minimum value for growthxmax Maximum value for growth

c Parameter defining the speed of the decline

get\_all\_predictions 67

```
get_all_predictions A helper for making the plots
```

# Description

A helper for making the plots

#### Usage

```
get_all_predictions(model)
```

# **Arguments**

model

An instance of FitMultipleDynamicGrowth

# Description

Function for calculating residuals of a dynamic prediction according to the requirements of FME::modFit().

# Usage

```
get_dyna_residuals(
  this_p,
  fit_data,
  env_conditions,
  known_pars,
  sec_model_names,
  cost = NULL,
  logbase_mu = logbase_logN,
  logbase_logN = 10
)
```

# **Arguments**

```
this_p named vector of model parameters

fit_data tibble with the data for the fit

env_conditions tibble with the environmental conditions

known_pars named vector of known model parameters

sec_model_names
```

named character vector with names the environmental conditions and values the secondary model (e.g. 'CPM').

get\_iso\_residuals

an instance of modCost to be combined (to fit multiple models).

logbase\_mu Base of the logarithm of the growthrate. By default, the same as logbase\_logN.

See vignette about units for details.

logbase\_logN Base of the logarithm for the population size. By default, 10 (i.e. log10). See

vignette about units for details.

#### Value

An instance of FME::modCost().

get\_iso\_residuals

Residuals of isothermal prediction

## **Description**

Residuals of isothermal prediction

# Usage

```
get_iso_residuals(
  this_p,
  fit_data,
  model_name,
  known_pars,
  logbase_mu = logbase_logN,
  logbase_logN = 10
)
```

### **Arguments**

this\_p named vector of model parameters to fit

fit\_data tibble with the data for the fit

model\_name character defining the primary growth model known\_pars named vector of fixed model parameters

logbase\_mu Base of the logarithm the growth rate is referred to. By default, the same as

logbase\_logN. See vignette about units for details.

logbase\_logN Base of the logarithm for the population size. By default, 10 (i.e. log10). See

vignette about units for details.

# Value

An instance of modCost.

```
get_multi_dyna_residuals
```

Residuals of multiple dynamic predictions

### **Description**

Function for calculating residuals of dynamic predictions under different conditions for the same model parameters according to the requirements of FME::modFit().

## Usage

```
get_multi_dyna_residuals(
    this_p,
    experiment_data,
    known_pars,
    sec_model_names,
    logbase_mu = logbase_logN,
    logbase_logN = 10
)
```

## **Arguments**

this\_p named vector of model parameters

 ${\tt experiment\_data}$ 

a nested list with the experimental data. Each entry describes one experiment as a list with two elements: data and conditions. data is a tibble with two columns: time and logN. conditions is a tibble with one column named time and as many additional columns as environmental factors.

named vector of known model parameters

sec\_model\_names

known\_pars

named character vector with names of the environmental conditions and values

of the secondary model (see secondary\_model\_data).

logbase\_mu Base of the logarithm the growth rate is referred to. By default, the same as

logbase\_logN. See vignette about units for details.

logbase\_logN Base of the logarithm for the population size. By default, 10 (i.e. log10). See

vignette about units for details.

#### Value

an instance of modCost.

```
get_secondary_residuals
```

Residuals of secondary models

# Description

Residual function for fit\_secondary\_growth().

# Usage

```
get_secondary_residuals(
  this_p,
  my_data,
  known_pars,
  sec_model_names,
  transformation
)
```

# Arguments

this\_p Named vector of model parameter values.

my\_data Tibble with the data used for the fit.

known\_pars Named vector of fixed model paramaters.

sec\_model\_names

Named character vector defining the secondary model for each environmental

factor.

transformation Character defining the tranformation of mu for model fitting. One of sq (square

root), log (log-transform) or none (no transformation).

#### Value

A numeric vector of residuals.

GlobalGrowthComparison

GlobalGrowthComparison class

### **Description**

The GlobalGrowthComparison class contains several functions for model comparison and model selection of growth models. It should not be instanced directly. Instead, it should be constructed using compare\_growth\_fits(). It is similar to GrowthComparison, although with specific tools to deal with several experiments.

It includes two type of tools for model selection and comparison: statistical indexes and visual analyses. Please check the sections below for details.

Note that all these tools use the names defined in compare\_growth\_fits(), so we recommend passing a named list to that function.

### Usage

```
## S3 method for class 'GlobalGrowthComparison'
coef(object, ...)

## S3 method for class 'GlobalGrowthComparison'
summary(object, ...)

## S3 method for class 'GlobalGrowthComparison'
print(x, ...)

## S3 method for class 'GlobalGrowthComparison'
plot(x, y, ..., type = 1, add_trend = TRUE)
```

# **Arguments**

object	an instance of GlobalGrowthComparison
	ignored
X	an instance of GlobalGrowthComparison
у	ignored
type	if type==1, the plot compares the model predictions. If type ==2, the plot compares the parameter estimates. If type==3, the plot shows the residuals
add_trend	should a trend line of the residuals be added for type==3? TRUE by default

#### Methods (by generic)

- coef(GlobalGrowthComparison): table of parameter estimates
- summary(GlobalGrowthComparison): summary table for the comparison
- print(GlobalGrowthComparison): print of the model comparison
- plot(GlobalGrowthComparison): illustrations comparing the fitted models

## Statistical indexes

GlobalGrowthComparison implements two S3 methods to obtain numerical values to facilitate model comparison and selection.

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• the coef method returns a tibble with the values of the parameter estimates and their corresponding standard errors for each model.

• the summary returns a tibble with the AIC, number of degrees of freedom, mean error and root mean squared error for each model.

#### Visual analyses

The S3 plot method can generate three types of plots:

- when type = 1, the plot compares the fitted growth curves against the experimental data used to fit the model.
- when type = 2, the plot compares the parameter estimates using error bars, where the limits of the error bars are the expected value +/- one standard error. In case one model does not has some model parameter (i.e. either because it is not defined or because it was fixed), the parameter is not included in the plot.
- when type=3, the plot shows the tendency of the residuals for each model. This plot can be used to detect deviations from independence.

These plots are divided by facets for each experiment.

GlobalGrowthFit

GlobalGrowthFit class

# **Description**

#### [Stable]

The GlobalGrowthFit class contains a growth model fitted to data using a global approach. Its constructor is fit\_growth().

It is a subclass of list with the items:

- algorithm: type of algorithm as in fit\_growth()
- data: data used for model fitting
- start: initial guess of the model parameters
- known: fixed model parameters
- primary\_model: a character describing the primary model
- fit results: an instance of modFit or modMCMC with the results of the fit
- best\_prediction: Instance of GrowthPrediction with the best growth fit
- sec\_models: a named vector with the secondary models assigned for each environmental factor. NULL for environment="constant"
- env\_conditions: a list with the environmental conditions used for model fitting. NULL for environment="constant"
- niter: number of iterations of the Markov chain. NULL if algorithm != "MCMC"
- logbase\_mu: base of the logarithm for the definition of parameter mu (check the relevant vignette)
- logbase\_logN: base of the logarithm for the definition of the population size (check the relevant vignette)
- environment: "dynamic". Always

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### Usage

```
## S3 method for class 'GlobalGrowthFit'
print(x, ...)
## S3 method for class 'GlobalGrowthFit'
coef(object, ...)
## S3 method for class 'GlobalGrowthFit'
summary(object, ...)
## S3 method for class 'GlobalGrowthFit'
predict(object, env_conditions, times = NULL, ...)
## S3 method for class 'GlobalGrowthFit'
residuals(object, ...)
## S3 method for class 'GlobalGrowthFit'
vcov(object, ...)
## S3 method for class 'GlobalGrowthFit'
deviance(object, ...)
## S3 method for class 'GlobalGrowthFit'
fitted(object, ...)
## S3 method for class 'GlobalGrowthFit'
logLik(object, ...)
## S3 method for class 'GlobalGrowthFit'
AIC(object, ..., k = 2)
## S3 method for class 'GlobalGrowthFit'
plot(
  Х,
 y = NULL,
  add_factor = NULL,
  ylims = NULL,
  label_x = "time",
  label_y1 = NULL,
  label_y2 = add_factor,
  line_col = "black",
  line_size = 1,
  line_type = "solid",
  line_col2 = "black",
  line\_size2 = 1,
  line_type2 = "dashed",
  point_size = 3,
```

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```
point_shape = 16,
   subplot_labels = "AUTO"
)

## S3 method for class 'GlobalGrowthFit'
predictMCMC(
   model,
   times,
   env_conditions,
   niter,
   newpars = NULL,
   formula = . ~ time
)
```

# Arguments

... ignored

object an instance of GlobalGrowthFit

env\_conditions Tibble with the (dynamic) environmental conditions during the experiment. It

must have one column named 'time' with the storage time and as many columns

as required with the environmental conditions.

times Numeric vector of storage times for the predictions.

an instance of GlobalGrowthFit

k penalty for the parameters (k=2 by default)

y ignored

add\_factor whether to plot also one environmental factor. If NULL (default), no environ-

mental factor is plotted. If set to one character string that matches one entry of

x\$env\_conditions, that condition is plotted in the secondary axis

ylims A two dimensional vector with the limits of the primary y-axis.

label\_x label of the x-axis

label\_y1 Label of the primary y-axis.
label\_y2 Label of the secondary y-axis.

line\_col Aesthetic parameter to change the colour of the line geom in the plot, see:

ggplot2::geom\_line()

line\_size Aesthetic parameter to change the thickness of the line geom in the plot, see:

ggplot2::geom\_line()

line\_type Aesthetic parameter to change the type of the line geom in the plot, takes num-

bers (1-6) or strings ("solid") see: ggplot2::geom\_line()

line\_col2 Same as lin\_col, but for the environmental factor.
line\_size2 Same as line\_size, but for the environmental factor.
line\_type2 Same as lin\_type, but for the environmental factor.

point\_size Size of the data points
point\_shape shape of the data points

greek\_tractors 75

subplot\_labels labels of the subplots according to plot\_grid.

model An instance of GlobalGrowthFit

niter Number of iterations.

newpars A named list defining new values for the some model parameters. The name

must be the identifier of a model already included in the model. These parameters do not include variation, so defining a new value for a fitted parameters

"fixes" it. NULL by default (no new parameters).

formula A formula stating the column named defining the elapsed time in env\_conditions.

By default, . ~ time.

#### Value

An instance of MCMCgrowth.

## Methods (by generic)

- print(GlobalGrowthFit): print of the model
- coef(GlobalGrowthFit): vector of fitted model parameters.
- summary(GlobalGrowthFit): statistical summary of the fit.
- predict(GlobalGrowthFit): vector of model predictions
- residuals (GlobalGrowthFit): model residuals. They are returned as a tibble with 4 columns: time (storage time), logN (observed count), exp (name of the experiment) and res (residual).
- vcov(GlobalGrowthFit): variance-covariance matrix of the model, estimated as 1/(0.5\*Hessian) for regression and as the variance-covariance of the draws for MCMC
- deviance(GlobalGrowthFit): deviance of the model.
- fitted(GlobalGrowthFit): fitted values. They are returned as a tibble with 3 columns: time (storage time), exp (experiment identifier) and fitted (fitted value).
- logLik(GlobalGrowthFit): loglikelihood of the model
- AIC(GlobalGrowthFit): Akaike Information Criterion
- plot(GlobalGrowthFit): comparison between the fitted model and the experimental data.
- predictMCMC(GlobalGrowthFit): prediction including parameter uncertainty

greek\_tractors Number of tractors in Greece according to the World Bank

#### **Description**

A dataset showing the increase in tractors in Greece. It was retrieved from https://data.worldbank.org/indicator/AG.AGR.TRA

## Usage

greek\_tractors

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### **Format**

A tibble with 46 rows (each corresponding to one year) and 7 columns:

```
year Year for the recordingtractors Number of tractors
```

GrowthComparison

GrowthComparison class

# Description

The GrowthComparison class contains several functions for model comparison and model selection of growth models. It should not be instanced directly. Instead, it should be constructed using compare\_growth\_fits().

It includes two type of tools for model selection and comparison: statistical indexes and visual analyses. Please check the sections below for details.

Note that all these tools use the names defined in compare\_growth\_fits(), so we recommend passing a named list to that function.

#### **Usage**

```
## S3 method for class 'GrowthComparison'
plot(x, y, ..., type = 1, add_trend = TRUE)
## S3 method for class 'GrowthComparison'
coef(object, ...)
## S3 method for class 'GrowthComparison'
print(x, ...)
## S3 method for class 'GrowthComparison'
summary(object, ...)
```

## Arguments

X	an instance of GrowthComparison
у	ignored
	ignored
type	if type==1, the plot compares the model predictions. If type ==2, the plot compares the parameter estimates. If type==3, the plot shows the residuals
add_trend	should a trend line of the residuals be added for type==3? TRUE by default
object	an instance of GrowthComparison

## Methods (by generic)

- plot(GrowthComparison): illustrations comparing the fitted models
- coef(GrowthComparison): table of parameter estimates
- print(GrowthComparison): print of the model comparison
- summary (GrowthComparison): summary table for the comparison

### Statistical indexes

GrowthComparison implements two S3 methods to obtain numerical values to facilitate model comparison and selection.

- the coef method returns a tibble with the values of the parameter estimates and their corresponding standard errors for each model.
- the summary returns a tibble with the AIC, number of degrees of freedom, mean error and root mean squared error for each model.

## Visual analyses

The S3 plot method can generate three types of plots:

- when type = 1, the plot compares the fitted growth curves against the experimental data used to fit the model.
- when type = 2, the plot compares the parameter estimates using error bars, where the limits of the error bars are the expected value +/- one standard error. In case one model does not have some model parameter (i.e. either because it is not defined or because it was fixed), the parameter is not included in the plot.
- when type=3, the plot shows the tendency of the residuals for each model. This plot can be used to detect deviations from independence.

GrowthFit

GrowthFit class

## **Description**

## [Stable]

The GrowthFit class contains a growth model fitted to data under static or dynamic conditions. Its constructor is fit\_growth().

It is a subclass of list with the items:

- environment: type of environment as in fit\_growth()
- algorithm: type of algorithm as in fit\_growth()
- data: data used for model fitting
- start: initial guess of the model parameters
- known: fixed model parameters

- primary\_model: a character describing the primary model
- fit\_results: an instance of modFit or modMCMC with the results of the fit
- best\_prediction: Instance of GrowthPrediction with the best growth fit
- sec\_models: a named vector with the secondary models assigned for each environmental factor. NULL for environment="constant"
- env\_conditions: a tibble with the environmental conditions used for model fitting. NULL for environment="constant"
- niter: number of iterations of the Markov chain. NULL if algorithm != "MCMC"
- logbase\_mu: base of the logarithm for the definition of parameter mu (check the relevant vignette)
- logbase\_logN: base of the logarithm for the definition of the population size (check the relevant vignette)

#### **Usage**

```
## S3 method for class 'GrowthFit'
print(x, ...)
## S3 method for class 'GrowthFit'
coef(object, ...)
## S3 method for class 'GrowthFit'
summary(object, ...)
## S3 method for class 'GrowthFit'
predict(object, times = NULL, env_conditions = NULL, ...)
## S3 method for class 'GrowthFit'
residuals(object, ...)
## S3 method for class 'GrowthFit'
vcov(object, ...)
## S3 method for class 'GrowthFit'
deviance(object, ...)
## S3 method for class 'GrowthFit'
fitted(object, ...)
## S3 method for class 'GrowthFit'
logLik(object, ...)
## S3 method for class 'GrowthFit'
AIC(object, ..., k = 2)
## S3 method for class 'GrowthFit'
plot(
```

```
Х,
 y = NULL
  add_factor = NULL,
  line_col = "black",
  line_size = 1,
  line_type = 1,
  point_col = "black",
  point_size = 3,
  point_shape = 16,
 ylims = NULL,
  label_y1 = NULL,
  label_y2 = add_factor,
  label_x = "time",
  line_col2 = "black",
  line_size2 = 1,
  line_type2 = "dashed"
## S3 method for class 'GrowthFit'
predictMCMC(
 model,
  times,
  env_conditions,
 niter,
 newpars = NULL,
  formula = . \sim time
)
```

### **Arguments**

x The object of class GrowthFit to plot.

... ignored.

object an instance of GrowthFit

times Numeric vector of storage times for the predictions.

env\_conditions Tibble with the (dynamic) environmental conditions during the experiment. It

must have one column named 'time' with the storage time and as many columns

as required with the environmental conditions.

k penalty for the parameters (k=2 by default)

y ignored

add\_factor whether to plot also one environmental factor. If NULL (default), no environ-

mental factor is plotted. If set to one character string that matches one entry of x\$env\_conditions, that condition is plotted in the secondary axis. Ignored if

environment="constant"

line\_col Aesthetic parameter to change the colour of the line geom in the plot, see:

ggplot2::geom\_line()

line_size	Aesthetic parameter to change the thickness of the line geom in the plot, see: ggplot2::geom_line()
line_type	Aesthetic parameter to change the type of the line geom in the plot, takes numbers (1-6) or strings ("solid") see: ggplot2::geom_line()
point_col	Aesthetic parameter to change the colour of the point geom, see: ggplot2::geom_point()
<pre>point_size</pre>	Aesthetic parameter to change the size of the point geom, see: ggplot2::geom_point()
point_shape	Aesthetic parameter to change the shape of the point geom, see: ggplot2::geom_point()
ylims	A two dimensional vector with the limits of the primary y-axis. NULL by default
label_y1	Label of the primary y-axis.
label_y2	Label of the secondary y-axis. Ignored if environment="constant"
label_x	Label of the x-axis
line_col2	Same as lin_col, but for the environmental factor. Ignored if environment="constant"
line_size2	Same as line_size, but for the environmental factor. Ignored if environment="constant"
line_type2	Same as lin_type, but for the environmental factor. Ignored if environment="constant"
model	An instance of GrowthFit
niter	Number of iterations.
newpars	A named list defining new values for the some model parameters. The name must be the identifier of a model already included in the model. These parameters do not include variation, so defining a new value for a fitted parameters "fixes" it. NULL by default (no new parameters).
formula	A formula stating the column named defining the elapsed time in env_conditions. By default, . ~ time.

#### Value

An instance of MCMCgrowth.

# Methods (by generic)

- print(GrowthFit): print of the model
- coef(GrowthFit): vector of fitted model parameters.
- summary(GrowthFit): statistical summary of the fit.
- predict(GrowthFit): vector of model predictions.
- residuals(GrowthFit): vector of model residuals.
- vcov(GrowthFit): variance-covariance matrix of the model, estimated as 1/(0.5\*Hessian) for regression and as the variance-covariance of the draws for MCMC
- deviance(GrowthFit): deviance of the model.
- fitted(GrowthFit): vector of fitted values.
- logLik(GrowthFit): loglikelihood of the model
- AIC(GrowthFit): Akaike Information Criterion
- plot(GrowthFit): compares the fitted model against the data.
- predictMCMC(GrowthFit): prediction including parameter uncertainty

GrowthPrediction 81

GrowthPrediction

GrowthPrediction class

#### **Description**

## [Stable]

The GrowthPrediction class contains the results of a growth prediction. Its constructor is predict\_growth(). It is a subclass of list with the items:

- simulation: a tibble with the model simulation
- primary model: a list describing the primary model as in predict\_growth()
- environment: a character describing the type of environmental conditions as in predict\_growth()
- env\_conditions: a named list with the functions used to approximate the (dynamic) environmental conditions. NULL if environment="constant".
- sec\_models: a named list describing the secondary models as in predict\_growth(). NULL if environment="constant".
- gammas: a tibble describing the variation of the gamma factors through the experiment. NUll if environment="constant".
- logbase\_mu: the log-base for the definition of parameter mu (see the relevant vignette)
- logbase\_logN: the log-base for the definition of the logarithm of the population size

#### Usage

```
## S3 method for class 'GrowthPrediction'
print(x, ...)
## S3 method for class 'GrowthPrediction'
summary(object, ...)
## S3 method for class 'GrowthPrediction'
plot(
  х,
 y = NULL
  add_factor = NULL,
  ylims = NULL,
  label_y1 = NULL,
  label_y2 = add_factor,
  line_col = "black",
  line_size = 1,
  line_type = "solid",
  line_col2 = "black",
  line_size2 = 1,
  line_type2 = "dashed",
```

82 GrowthPrediction

```
label_x = "time"
)
## S3 method for class 'GrowthPrediction'
coef(object, ...)
```

## **Arguments**

The object of class GrowthPrediction to plot. Χ ignored an instance of GrowthPrediction object ignored add\_factor whether to plot also one environmental factor. If NULL (default), no environmental factor is plotted. If set to one character string that matches one entry of x\$env\_conditions, that condition is plotted in the secondary axis. Ignored for environment="constant". ylims A two dimensional vector with the limits of the primary y-axis. label\_y1 Label of the primary y-axis. label\_y2 Label of the secondary y-axis. line\_col Aesthetic parameter to change the colour of the line geom in the plot, see: ggplot2::geom\_line() Aesthetic parameter to change the thickness of the line geom in the plot, see: line\_size ggplot2::geom\_line() Aesthetic parameter to change the type of the line geom in the plot, takes numline\_type bers (1-6) or strings ("solid") see: ggplot2::geom\_line() line\_col2 Same as lin\_col, but for the environmental factor. line\_size2 Same as line\_size, but for the environmental factor. line\_type2 Same as lin\_type, but for the environmental factor. label x Label of the x-axis.

### Methods (by generic)

- print(GrowthPrediction): print of the model
- summary(GrowthPrediction): summary of the model
- plot(GrowthPrediction): predicted growth curve.
- coef(GrowthPrediction): coefficients of the model

GrowthUncertainty 83

GrowthUncertainty

GrowthUncertainty class

## Description

### [Stable]

The GrowthUncertainty class contains the results of a growth prediction under isothermal conditions considering parameter uncertainty. Its constructor is predict\_growth\_uncertainty().

It is a subclass of list with the items:

- sample: parameter sample used for the calculations.
- simulations: growth curves predicted for each parameter.
- quantiles: limits of the credible intervals (5%, 10%, 50%, 90%, 95%) for each time point.
- model: Model used for the calculations.
- mus: Mean parameter values used for the simulations.
- sigma: Variance-covariance matrix used for the simulations.
- logbase\_mu: base of the logarithm for the definition of parameter mu (check the relevant vignette)
- logbase\_logN: base of the logarithm for the definition of the population size (check the relevant vignette)

## Usage

```
## $3 method for class 'GrowthUncertainty'
print(x, ...)

## $3 method for class 'GrowthUncertainty'
plot(
    x,
    y = NULL,
    ...,
    line_col = "black",
    line_size = 0.5,
    line_type = "solid",
    ribbon80_fill = "grey",
    ribbon90_fill = "grey",
    alpha80 = 0.5,
    alpha90 = 0.4
)
```

# Arguments

```
x The object of class GrowthUncertainty to plot.
```

... ignored.

У	ignored
line_col	Aesthetic parameter to change the colour of the line geom in the plot, see: ggplot2::geom_line()
line_size	Aesthetic parameter to change the thickness of the line geom in the plot, see: ggplot2::geom_line()
line_type	Aesthetic parameter to change the type of the line geom in the plot, takes numbers (1-6) or strings ("solid") see: ggplot2::geom_line()
ribbon80_fill	fill colour for the space between the 10th and 90th quantile, see: ggplot2::geom_ribbon()
ribbon90_fill	fill colour for the space between the 5th and 95th quantile, see: ggplot2::geom_ribbon()
alpha80	transparency of the ribbon aesthetic for the space between the 10th and 90th quantile. Takes a value between 0 (fully transparant) and 1 (fully opaque)
alpha90	transparency of the ribbon aesthetic for the space between the 5th and 95th quantile. Takes a value between 0 (fully transparant) and 1 (fully opaque).

# Methods (by generic)

- print(GrowthUncertainty): print of the model
- plot(GrowthUncertainty): Growth prediction (prediction band) considering parameter uncertainty.

 ${\tt growth\_pH\_temperature} \ \ \textit{Example of dynamic growth}$ 

## **Description**

A dataset to demonstrate the use of fit\_dynamic\_growth. The values of the environmental conditions are described in conditions\_pH\_temperature.

# Usage

growth\_pH\_temperature

## **Format**

A tibble with 20 rows and 2 columns:

time elapsed time

logN decimal logarithm of the population size

growth\_salmonella 85

	growth	salmone	lla
--	--------	---------	-----

Growth of Salmonella spp in broth

## **Description**

An example dataset to illustrate fit\_isothermal\_growth(). It describes the growth of Salmonella spp. in broth. It was retrieved from ComBase (ID: B092\_10).

### Usage

```
growth_salmonella
```

### **Format**

A tibble with 21 rows and 2 columns:

time elapsed time in hours.

logN observed population size (log CFU/g).

inhibitory\_model

Secondary model for inhibitory compounds

## **Description**

Secondary model for the effect of inhibitory compounds.

## Usage

```
inhibitory_model(x, MIC, alpha)
```

# Arguments

x Value of the environmental factor (in principle, concentration of compound).

MIC Minimum Inhibitory Concentration

alpha shape factor of the miodel

## Value

The corresponding gamma factor.

86 is.FitDynamicGrowth

is.DynamicGrowth

Test of DynamicGrowth object

# Description

Tests if an object is of class DynamicGrowth.

# Usage

```
is.DynamicGrowth(x)
```

## **Arguments**

Х

object to be checked.

### Value

A boolean specifying whether x is of class DynamicGrowth

 $\verb"is.FitDynamicGrowth"$ 

Test of FitDynamicGrowth object

# Description

Tests if an object is of class FitDynamicGrowth.

## Usage

```
is.FitDynamicGrowth(x)
```

# Arguments

Х

object to be checked.

## Value

A boolean specifying whether x is of class FitDynamicGrowth

is.FitDynamicGrowthMCMC

 $Test\ of\ FitDynamic Growth MCMC\ object$ 

# Description

Tests if an object is of class FitDynamicGrowthMCMC.

## Usage

```
is.FitDynamicGrowthMCMC(x)
```

# Arguments

x object to be checked.

# Value

A boolean specifying whether x is of class FitDynamicGrowthMCMC

is.FitIsoGrowth

Test of FitIsoGrowth object

## **Description**

Tests if an object is of class FitIsoGrowth.

# Usage

```
is.FitIsoGrowth(x)
```

## **Arguments**

x object to be checked.

## Value

A boolean specifying whether x is of class FitIsoGrowth

is.FitMultipleDynamicGrowth

Test of FitMultipleDynamicGrowth object

# Description

Tests if an object is of class FitMultipleDynamicGrowth.

# Usage

```
is.FitMultipleDynamicGrowth(x)
```

# Arguments

x object to be checked.

### Value

A boolean specifying whether x is of class FitMultipleDynamicGrowth

 $is. Fit {\tt MultipleDynamicGrowthMCMC}$ 

Test of FitMultipleDynamicGrowthMCMC object

# Description

Tests if an object is of class FitMultipleDynamicGrowthMCMC.

# Usage

```
is.FitMultipleDynamicGrowthMCMC(x)
```

## **Arguments**

x object to be checked.

### Value

A boolean specifying whether x is of class FitMultipleDynamicGrowthMCMC

is.FitSecondaryGrowth 89

is.FitSecondaryGrowth Test of FitSecondaryGrowth object

# Description

Tests if an object is of class FitSecondaryGrowth.

# Usage

```
is.FitSecondaryGrowth(x)
```

## **Arguments**

x object to be checked.

### Value

A boolean specifying whether x is of class FitSecondaryGrowth

 $\verb|is.GlobalGrowthFit| Test of GlobalGrowthFit| object$ 

# Description

Tests if an object is of class GlobalGrowthFit

## Usage

```
is.GlobalGrowthFit(x)
```

## **Arguments**

x object to be checked.

## Value

A boolean specifying whether x is of class GlobalGrowthFit

90 is.GrowthPrediction

is.GrowthFit

Test of GrowthFit object

# Description

Tests if an object is of class GrowthFit

# Usage

```
is.GrowthFit(x)
```

## **Arguments**

Х

object to be checked.

### Value

A boolean specifying whether x is of class GrowthFit

is.GrowthPrediction

Test of GrowthPrediction object

# Description

Tests if an object is of class GrowthPrediction

## Usage

```
is.GrowthPrediction(x)
```

# Arguments

Х

object to be checked.

## Value

A boolean specifying whether x is of class GrowthPrediction

is.GrowthUncertainty 91

# Description

Tests if an object is of class GrowthUncertainty

# Usage

```
is.GrowthUncertainty(x)
```

## **Arguments**

x object to be checked.

### Value

A boolean specifying whether x is of class GrowthUncertainty

 $is. Is other mal Growth \quad \textit{Test of Isothermal Growth object}$ 

# Description

Tests if an object is of class IsothermalGrowth.

## Usage

```
is.IsothermalGrowth(x)
```

# Arguments

x object to be checked.

## Value

A boolean specifying whether x is of class IsothermalGrowth

92 is.StochasticGrowth

is.MCMCgrowth

Test of MCMCgrowth object

# Description

Tests if an object is of class MCMCgrowth.

# Usage

```
is.MCMCgrowth(x)
```

## **Arguments**

Х

object to be checked.

### Value

A boolean specifying whether x is of class MCMCgrowth

is.StochasticGrowth

Test of StochasticGrowth object

# Description

Tests if an object is of class StochasticGrowth.

## Usage

```
is.StochasticGrowth(x)
```

# Arguments

Х

object to be checked.

## Value

A boolean specifying whether x is of class StochasticGrowth

IsothermalGrowth 93

IsothermalGrowth

IsothermalGrowth class

### **Description**

## [Superseded]

The class IsothermalGrowth has been superseded by the top-level class GrowthPrediction, which provides a unified approach for growth modelling.

Still, it is still returned if the superseded predict\_isothermal\_growth() is called.

It is a subclass of list with the items:

- simulation: A tibble with the model simulation.
- model: The name of the model used for the predictions.
- pars: A list with the values of the model parameters.

## Usage

## **Arguments**

```
x The object of class IsothermalGrowth to plot.
... ignored
y ignored
line_col Aesthetic parameter to change the colour of the line, see: ggplot2::geom_line()
line_size Aesthetic parameter to change the thickness of the line, see: ggplot2::geom_line()
line_type Aesthetic parameter to change the type of the line, takes numbers (1-6) or strings
("solid") see: ggplot2::geom_line()
```

94 iso\_Baranyi

ylims Two-dimensional numeric vector with the limits of the y-axis (or NULL, which is

the default)

label\_y Title of the y-axis
label\_x Title of the x-axis

object an instance of IsothermalGrowth

## Methods (by generic)

• print(IsothermalGrowth): print of the model

• plot(IsothermalGrowth): plot of the predicted growth curve.

• coef(IsothermalGrowth): coefficients of the model

iso\_Baranyi Isothermal Baranyi model

## **Description**

Baranyi growth model as defined by Baranyi and Roberts (1994). We use the solution calculated by Poschet et al. (2005, doi: https://doi.org/10.1016/j.ijfoodmicro.2004.10.008) after log-transformation according to MONTE CARLO ANALYSIS FOR MICROBIAL GROWTH CURVES, by Oksuz and Buzrul.

### Usage

```
iso_Baranyi(times, logN0, mu, lambda, logNmax)
```

## **Arguments**

times Numeric vector of storage times

logN0 Initial log microbial count

mu Maximum specific growth rate (in ln CFU/t)

lambda Lag phase duration

logNmax Maximum log microbial count

#### Value

Numeric vector with the predicted microbial count.

iso\_Baranyi\_noLag 95

ranyi_noLag
-------------

#### **Description**

Baranyi growth model as defined by Baranyi and Roberts (1994). We use the solution calculated by Poschet et al. (2005, doi: https://doi.org/10.1016/j.ijfoodmicro.2004.10.008) after log-transformation according to MONTE CARLO ANALYSIS FOR MICROBIAL GROWTH CURVES, by Oksuz and Buzrul.

## Usage

```
iso_Baranyi_noLag(times, logN0, mu, logNmax)
```

## Arguments

times Numeric vector of storage times logN0 Initial log microbial count

mu Maximum specific growth rate (in ln CFU/t)

logNmax Maximum log microbial count

#### Value

Numeric vector with the predicted microbial count.

# Description

Baranyi growth model as defined by Baranyi and Roberts (1994). We use the solution calculated by Poschet et al. (2005, doi: https://doi.org/10.1016/j.ijfoodmicro.2004.10.008) after log-transformation according to MONTE CARLO ANALYSIS FOR MICROBIAL GROWTH CURVES, by Oksuz and Buzrul.

#### Usage

```
iso_Baranyi_noStat(times, logN0, mu, lambda)
```

### **Arguments**

times Numeric vector of storage times logN0 Initial log microbial count

mu Maximum specific growth rate (in ln CFU/t)

lambda Lag phase duration

96 lambda\_to\_Q0

### Value

Numeric vector with the predicted microbial count.

iso\_repGompertz

Reparameterized Gompertz model

## **Description**

Reparameterized Gompertz growth model defined by Zwietering et al. (1990).

## Usage

```
iso_repGompertz(times, logN0, C, mu, lambda)
```

## Arguments

times Numeric vector of storage times logN0 Initial log microbial count

C Difference between logN0 and the maximum log-count.

mu Maximum specific growth rate (in ln CFU/t)

lambda Lag phase duration

## Value

Numeric vector with the predicted microbial count.

lambda\_to\_Q0

Q0 from lag phase duration

# Description

# [Stable]

Convenience function to calculate the value of Q0 for the Baranyi model from the duration of the lag phase

### Usage

```
lambda_to_Q0(lambda, mu, logbase_mu = 10)
```

# Arguments

lambda Duration of the lag phase.

mu Specific growth rate in the exponential phase.

logbase\_mu Base of the logarithm the growth rate is referred to. By default, 10 (i.e. log10).

See vignette about units for details.

logistic\_model 97

logistic_model Logistic gr	owth model
----------------------------	------------

# Description

Logistic growth model

# Usage

```
logistic_model(times, logN0, mu, lambda, C)
```

# Arguments

times Numeric vector of storage times logN0 Initial log microbial count

mu Maximum specific growth rate (in ln CFU/t)

lambda Lag phase duration

C Difference between logN0 and the maximum log-count.

### Value

Numeric vector with the predicted microbial count

loglinear_model	Loglinear model	

# Description

Loglinear model

# Usage

```
loglinear_model(times, logN0, mu)
```

# Arguments

times	Numeric vector of storage times
logN0	Initial log microbial count

mu Maximum specific growth rate (in ln CFU/t)

make\_guess\_factor

Initial guesses for the secondary model of one factor

## Description

Initial guesses for the secondary model of one factor

## Usage

```
make_guess_factor(fit_data, sec_model, factor)
```

#### **Arguments**

fit\_data Tibble with the data used for the fit. It must have one column with the observed

growth rate (named mu by default; can be changed using the "formula" argument)

and as many columns as needed with the environmental factors.

sec\_model character defining the secondary model equation according to secondary\_model\_data()

factor character defining the environmental factor

make\_guess\_primary

Initial guesses for fitting primary growth models

### **Description**

#### [Experimental]

The function uses some heuristics to provide initial guesses for the parameters of the growth model selected that can be used with fit\_growth().

#### Usage

```
make_guess_primary(
  fit_data,
  primary_model,
  logbase_mu = 10,
  formula = logN ~ time
)
```

## **Arguments**

fit\_data the experimental data. A tibble (or data.frame) with a column named time with

the elapsed time and one called logN with the logarithm of the population size

primary\_model a string defining the equation of the primary model, as defined in primary\_model\_data()

logbase\_mu Base of the logarithm the growth rate is referred to. By default, 10 (i.e. log10).

See vignette about units for details.

formula an object of class "formula" describing the x and y variables. logN ~ time as a

default.

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### Value

make\_guess\_secondary

A named numeric vector of initial guesses for the model parameters

# Examples

```
## An example of experimental data
my_data <- data.frame(time = 0:9,
                      logN = c(2, 2.1, 1.8, 2.5, 3.1, 3.4, 4, 4.5, 4.8, 4.7))
## We just need to pass the data and the model equation
make_guess_primary(my_data, "Logistic")
## We can use this together with fit_growth()
fit_growth(my_data,
           list(primary = "Logistic"),
           make_guess_primary(my_data, "Logistic"),
           c()
           )
## The parameters returned by the function are adapted to the model
make_guess_primary(my_data, "Baranyi")
## It can express mu in other logbases
make_guess_primary(my_data, "Baranyi", logbase_mu = exp(1)) # natural
make_guess_primary(my_data, "Baranyi", logbase_mu = 2) # base2
```

## **Description**

# [Experimental]

Uses some heuristic rules to generate an initial guess of the model parameters of secondary growth models that can be used for model fitting with fit\_secondary\_growth().

#### **Usage**

```
make_guess_secondary(fit_data, sec_model_names)
```

100 MCMCgrowth

#### **Arguments**

fit\_data

Tibble with the data used for the fit. It must have one column with the observed growth rate (named mu by default; can be changed using the "formula" argument) and as many columns as needed with the environmental factors.

sec\_model\_names

Named character vector defining the secondary model for each environmental factor.

## **Examples**

MCMCgrowth

MCMCgrowth class

## **Description**

## [Stable]

The MCMCgrowth class contains the results of a growth prediction consider parameter variability based on a model fitted using an MCMC algorithm.

It is a subclass of list with items:

- sample: Parameter sample used for the calculations.
- simulations: Individual growth curves calculated based on the parameter sample.
- quantiles: Tibble with the limits of the credible intervals (5%, 10%, 50%, 90% and 95%) for each time point.
- model: Instance of FitDynamicGrowthMCMC used for predictions.
- env\_conditions: A tibble with the environmental conditions of the simulation.

MCMCgrowth 101

## Usage

```
## S3 method for class 'MCMCgrowth'
print(x, ...)
## S3 method for class 'MCMCgrowth'
plot(
  х,
  y = NULL,
  add_factor = NULL,
  alpha_80 = 0.5,
  fill_80 = "grey",
  alpha_90 = 0.5,
  fill_90 = "grey",
  label_y1 = "logN",
  label_y2 = add_factor,
  line_col = "black",
  line_type = 1,
  line\_size = 1,
  line_type2 = 2,
  line_col2 = "black",
  line\_size2 = 1,
  ylims = NULL
)
```

# Arguments

X	The object of class MCMCgrowth to plot.
	ignored.
У	ignored
add_factor	Includes the variation of one environmental factor in the plot. It must be one of the column names in x\$env_conditions.
alpha_80	transparency of the ribbon for the 80th posterior5 by default.
fill_80	fill colour of the ribbon for the 80th posterior. "grey" by default.
alpha_90	transparency of the ribbon for the 90th posterior5 by default.
fill_90	fill colour of the ribbon for the 90th posterior. "grey" by default.
label_y1	label of the primary y axis. "logN" by default.
label_y2	label of the secondary y axis. The name of the environmental factor by default.
line_col	colour of the line representing the median. "black" by default.
line_type	linetype for the line representing the median. solid by default.
line_size	size of the line representing the median. 1 by default.
line_type2	linetype for the line representing the environmental condition. Dashed by default.
line_col2	colour of the line representing the environmental condition. "black" by default.

multiple\_counts

line\_size2 size of the line representing the environmental condition. 1 by default. ylims limits of the primary y-axis. NULL by default (let ggplot choose).

## Methods (by generic)

- print(MCMCgrowth): print of the model
- plot(MCMCgrowth): plot of predicted growth (prediction band).

multiple\_conditions Environme

Environmental conditions during several dynamic experiments

### **Description**

This dataset is paired with multiple\_counts to illustrate the global fitting of fit\_growth().

#### Usage

multiple\_conditions

#### **Format**

A nested list with two elements, each one corresponding to one experiment. Each element is a data.frame with three columns:

• time: elapsed time

• temperature: observed temperature

• pH: observed pH

multiple\_counts

Population growth observed in several dynamic experiments

# Description

This dataset is paired with multiple\_conditions to illustrate the global fitting of fit\_growth().

### Usage

```
multiple_counts
```

#### **Format**

A nested list with two elements, each one corresponding to one experiment. Each element is a data.frame with two columns:

• time: elapsed time

• logN: log10 of the microbial concentration

multiple\_experiments 103

multiple\_experiments A set of growth experiments under dynamic conditions

## **Description**

An example dataset illustrating the requirements of  $fit_multiple_growth()$  and  $fit_multiple_growth_MCMC()$ .

## Usage

```
multiple_experiments
```

#### **Format**

A nested list with two elements. Each element corresponds to one experiment and is described by a list with two data frames:

data a tibble describing the microbial counts. It has 2 columns: time (elapsed time) and logN (logarithm of the microbial count).

**conditions** a tibble describing the environmental conditions. It has 3 columns: time (elapsed time), temperature (storage temperature) and pH (pH of the media).

predictMCMC

Generic for calculating predictions with uncertainty from fits

# Description

Generic for calculating predictions with uncertainty from fits

## Usage

```
predictMCMC(
  model,
  times,
  env_conditions,
  niter,
  newpars = NULL,
  formula = . ~ time
)
```

#### **Arguments**

model Fit object

times see specific methods for each class env\_conditions see specific methods for each class niter see specific methods for each class newpars see specific methods for each class

formula A formula stating the column named defining the elapsed time in env\_conditions.

By default, . ~ time.

predict\_dynamic\_growth

Growth under dynamic conditions

## **Description**

## [Superseded]

The function predict\_dynamic\_growth() has been superseded by the top-level function predict\_growth(), which provides a unified approach for growth modelling.

Regardless on that, it can still predict population growth under dynamic conditions based on the Baranyi model (Baranyi and Roberts, 1994) and secondary models based on the gamma concept (Zwietering et al. 1992).

Model predictions are done by linear interpolation of the environmental conditions defined in env\_conditions.

#### Usage

```
predict_dynamic_growth(
   times,
   env_conditions,
   primary_pars,
   secondary_models,
   ...,
   check = TRUE,
   logbase_logN = 10,
   logbase_mu = logbase_logN,
   formula = . ~ time
)
```

## **Arguments**

times Numeric vector of storage times to make the predictions

env\_conditions Tibble (or data.frame) describing the variation of the environmental conditions

during storage. It must have with the elapsed time (named time by default; can be changed with the "formula" argument), and as many additional columns as

environmental factors.

primary\_pars A named list defining the parameters of the primary model and the initial values of the model variables. That is, with names mu\_opt, Nmax, N0, Q0.

secondary\_models

A nested list describing the secondary models.

... Additional arguments for deSolve::ode().

check Whether to check the validity of the models. TRUE by default.

logbase\_logN Base of the logarithm for the population size. By default, 10 (i.e. log10). See

vignette about units for details.

logbase\_mu Base of the logarithm the growth rate is referred to. By default, the same as

logbase\_logN. See vignette about units for details.

formula An object of class "formula" describing the x variable. . ~ time as a default.

### Value

An instance of DynamicGrowth().

## **Examples**

```
## Definition of the environmental conditions
library(tibble)
my\_conditions <- tibble(time = c(0, 5, 40),
    temperature = c(20, 30, 35),
    pH = c(7, 6.5, 5)
## Definition of the model parameters
my_primary <- list(mu_opt = 2,</pre>
    Nmax = 1e8, N0 = 1e0,
    Q0 = 1e-3
sec_temperature <- list(model = "Zwietering",</pre>
    xmin = 25, xopt = 35, n = 1)
sec_pH = list(model = "CPM",
    xmin = 5.5, xopt = 6.5,
    xmax = 7.5, n = 2)
my_secondary <- list(</pre>
    temperature = sec_temperature,
    pH = sec_pH
my_times < - seq(0, 50, length = 1000)
## Do the simulation
dynamic_prediction <- predict_dynamic_growth(my_times,</pre>
```

106 predict\_growth

```
my_conditions, my_primary,
    my_secondary)

## Plot the results

plot(dynamic_prediction)

## We can plot some environmental factor with add_factor

plot(dynamic_prediction, add_factor = "temperature", ylims= c(0, 8),
    label_y1 = "Microbial count (log CFU/ml)",
    label_y2 = "Storage temperature (C)")
```

predict\_growth

Prediction of microbial growth

## **Description**

### [Stable]

This function provides a top-level interface for predicting population growth. Predictions can be made either under constant or dynamic environmental conditions. See below for details on the calculations.

## Usage

```
predict_growth(
   times,
   primary_model,
   environment = "constant",
   secondary_models = NULL,
   env_conditions = NULL,
   ...,
   check = TRUE,
   logbase_mu = logbase_logN,
   logbase_logN = 10,
   formula = . ~ time
)
```

### **Arguments**

times numeric vector of time points for making the predictions

primary\_model named list defining the values of the parameters of the primary growth model

environment type of environment. Either "constant" (default) or "dynamic" (see below for details on the calculations for each condition)

secondary\_models

a nested list describing the secondary models. See below for details

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env\_conditions Tibble describing the variation of the environmental conditions for dynamic experiments. It must have with the elapsed time (named time by default; can be changed with the "formula" argument), and as many additional columns as environmental factors. Ignored for "constant" environments.

... Additional arguments for deSolve::ode().

check Whether to check the validity of the models. TRUE by default.

logbase\_mu Base of the logarithm the growth rate is referred to. By default, the same as logbase\_logN. See vignette about units for details.

logbase\_logN Base of the logarithm for the population size. By default, 10 (i.e. log10). See vignette about units for details.

formula An object of class "formula" describing the x variable for predictions under

#### **Details**

To ease data input, the functions can convert between parameters defined in different scales. Namely, for predictions in constant environments (environment="constant"):

- "logN0" can be defined as "N0". The function automatically calculates the log-transformation.
- "logNmax" can be defined as "Nmax". The function automatically calculates the log-transformation.
- "mu" can be defined as "mu\_opt". The function assumes the prediction is under optimal growth conditions.
- "lambda" can be defined by "Q0". The duration of the lag phase is calculated using Q0\_to\_lambda().

And, for predictions in dynamic environments (environment="dynamic"):

dynamic conditions. . ~ time as a default.

- "N0" can be defined as "N0". The function automatically calculates the antilog-transformation.
- "Nmax" can be defined as "logNmax". The function automatically calculates the antilogtransformation.
- "mu" can be defined as "mu\_opt". The function assumes mu was calculated under optimal growth conditions.
- "Q0" can be defined by the value of "lambda" under dynamic conditions. Then, the value of Q0 is calculated using lambda\_to\_Q0().

#### Value

An instance of GrowthPrediction.

#### **Predictions in constant environments**

Predictions under constant environments are calculated using only primary models. Consequently, the arguments "secondary\_models" and "env\_conditions" are ignored. If these were passed, the function would return a warning. In this case, predictions are calculated using the algebraic form of the primary model (see vignette for details).

The growth model is defined through the "primary\_model" argument using a named list. One of the list elements must be named "model" and must take take one of the valid keys returned by

108 predict\_growth

primary\_model\_data(). The remaining entries of the list define the values of the parameters of the selected model. A list of valid keys can be retrieved using primary\_model\_data() (see example below). Note that the functions can do some operations to facilitate the compatibility between constant and dynamic environments (see Details).

### Predictions in dynamic environments

Predictions under dynamic environments are calculated by solving numerically the differential equation of the Baranyi growth model. The effect of changes in the environmental conditions in the growth rate are calculated according to the gamma approach. Therefore, one must define both primary and secondary models.

The dynamic environmental conditions are defined using a tibble (or data.frame) through the "env\_conditions" argument. It must include one column named "time" stating the elapsed time and as many additional columns as environmental conditions included in the prediction. For values of time not included in the tibble, the values of the environmental conditions are calculated by linear interpolation.

Primary models are defined as a named list through the "primary\_model" argument. It must include the following elements:

- N0: initial population size
- Nmax: maximum population size in the stationary growth phase
- mu\_opt: growth rate under optimal growth conditions
- Q0: value defining the duration of the lag phase Additional details on these parameters can be found in the package vignettes.

Secondary models are defined as a nested list through the "secondary\_models" argument. The list must have one entry per environmental condition, whose name must match those used in the "env\_conditions" argument. Each of these entries must be a named list defining the secondary model for each environmental condition. The model equation is defined in an entry named "model" (valid keys can be retrieved from secondary\_model\_data()). Then, additional entries defined the values of each model parameters (valid keys can be retrieved from secondary\_model\_data())

For additional details on how to define the secondary models, please see the package vignettes (and examples below).

### **Examples**

```
## Example 1 - Growth under constant conditions ------
## Valid model keys can be retrieved calling primary_model_data()
primary_model_data()

my_model <- "modGompertz" # we will use the modified-Gompertz

## The keys of the model parameters can also be obtained from primary_model_data()
primary_model_data(my_model)$pars

## We define the primary model as a list</pre>
```

predict\_growth 109

```
my_model <- list(model = "modGompertz", logN0 = 0, C = 6, mu = .2, lambda = 20)
## We can now make the predictions
my_time <- seq(0, 100, length = 1000) # Vector of time points for the calculations
my_prediction <- predict_growth(my_time, my_model, environment = "constant")</pre>
## The instance of IsothermalGrowth includes several S3 methods
print(my_prediction)
plot(my_prediction)
coef(my_prediction)
## Example 2 - Growth under dynamic conditions ------
## We will consider the effect of two factors: temperature and pH
my\_conditions \leftarrow data.frame(time = c(0, 5, 40),
                            temperature = c(20, 30, 35),
                            pH = c(7, 6.5, 5)
## The primary model is defined as a named list
my_primary <- list(mu = 2, Nmax = 1e7, N0 = 1, Q0 = 1e-3)
## The secondary model is defined independently for each factor
sec_temperature <- list(model = "Zwietering",</pre>
   xmin = 25, xopt = 35, n = 1)
sec_pH = list(model = "CPM",
   xmin = 5.5, xopt = 6.5,
   xmax = 7.5, n = 2)
## Then, they are assigned to each factor using a named list
my_secondary <- list(</pre>
    temperature = sec_temperature,
   pH = sec_pH
   )
## We can call the function now
my\_times <- seq(0, 50, length = 1000) # Where the output is calculated
dynamic_prediction <- predict_growth(environment = "dynamic",</pre>
                                     my_times, my_primary, my_secondary,
                                     my\_conditions
                                     )
```

## The instance of DynamicGrowth includes several useful S3 methods

```
print(dynamic_prediction)
plot(dynamic_prediction)
plot(dynamic_prediction, add_factor = "pH")
coef(dynamic_prediction)
## The time_to_size function can predict the time to reach a population size
time_to_size(my_prediction, 3)
```

predict\_growth\_uncertainty

Isothermal growth with parameter uncertainty

# **Description**

# [Stable]

Simulation of microbial growth considering uncertianty in the model parameters. Calculations are based on Monte Carlo simulations, considering the parameters follow a multivariate normal distribution.

#### Usage

```
predict_growth_uncertainty(
   model_name,
   times,
   n_sims,
   pars,
   corr_matrix = diag(nrow(pars)),
   check = TRUE,
   logbase_mu = logbase_logN,
   logbase_logN = 10
)
```

## **Arguments**

model\_name Character describing the primary growth model.

times Numeric vector of storage times for the simulations.

n\_sims Number of simulations.

pars A tibble describing the parameter uncertainty (see details).

corr\_matrix Correlation matrix of the model parameters. Defined in the same order as in

pars. An identity matrix by default (uncorrelated parameters).

check Whether to do some tests. FALSE by default.

logbase\_mu Base of the logarithm the growth rate is referred to. By default, the same as logbase\_logN. See vignette about units for details.

logbase\_logN Base of the logarithm for the population size. By default, 10 (i.e. log10). See

vignette about units for details.

#### **Details**

The distributions of the model parameters are defined in the pars argument using a tibble with 4 columns:

- par: identifier of the model parameter (according to primary\_model\_data()),
- mean: mean value of the model parameter.,
- sd: standard deviation of the model parameter.,
- scale: scale at which the model parameter is defined. Valid values are 'original' (no transformation), 'sqrt' square root or 'log' log-scale. The parameter sample is generated considering the parameter follows a marginal normal distribution at this scale, and is later converted to the original scale for calculations.

#### Value

An instance of GrowthUncertainty().

## **Examples**

```
## Definition of the simulation settings
my_model <- "Baranyi"</pre>
my_times <- seq(0, 30, length = 100)
n_sims <- 3000
library(tibble)
pars <- tribble(
    ~par, ~mean, ~sd, ~scale,
    "logN0", 0, .2, "original",
    "mu", 2, .3, "sqrt",
    "lambda", 4, .4, "sqrt",
    "logNmax", 6, .5, "original"
)
## Calling the function
stoc_growth <- predict_growth_uncertainty(my_model, my_times, n_sims, pars)</pre>
## We can plot the results
plot(stoc_growth)
## Adding parameter correlation
my\_cor \leftarrow matrix(c(1, 0, 0, 0,
```

```
0, 1, 0.7, 0,
0, 0.7, 1, 0,
0, 0, 0, 0, 1),
nrow = 4)

stoc_growth2 <- predict_growth_uncertainty(my_model, my_times, n_sims, pars, my_cor)

plot(stoc_growth2)

## The time_to_size function can calculate the median growth curve to reach a size

time_to_size(stoc_growth, 4)

## Or the distribution of times

dist <- time_to_size(stoc_growth, 4, type = "distribution")

plot(dist)</pre>
```

predict\_isothermal\_growth

Isothermal microbial growth

# **Description**

# [Superseded]

The function predict\_isothermal\_growth() has been superseded by the top-level function predict\_growth(), which provides a unified approach for growth modelling.

Regardless of that, it can still be used to predict population growth under static environmental conditions (i.e. using primary models).

# Usage

```
predict_isothermal_growth(
  model_name,
  times,
  model_pars,
  check = TRUE,
  logbase_mu = 10,
  logbase_logN = 10
)
```

#### **Arguments**

model\_name Character defining the growth model.

times Numeric vector of storage times for the predictions.

model\_pars Named vector or list defining the values of the model parameters.

check Whether to do basic checks (TRUE by default).

logbase\_mu Base of the logarithm the growth rate is referred to. By default, the same as

logbase\_logN. See vignette about units for details.

logbase\_logN Base of the logarithm for the population size. By default, 10 (i.e. log10). See

vignette about units for details.

#### Value

An instance of IsothermalGrowth().

# Examples

```
## Define the simulations parameters

my_model <- "modGompertz"

my_pars <- list(logN0 = 2, C = 6, mu = .2, lambda = 25)

my_time <- seq(0, 100, length = 1000)

## Do the simulation

static_prediction <- predict_isothermal_growth(my_model, my_time, my_pars)

## Plot the results

plot(static_prediction)</pre>
```

predict\_MCMC\_growth

Stochastic growth of MCMC fit

# **Description**

#### [Superseded]

The function predict\_MCMC\_growth() has been superseded by predictMCMC() S3 methods of the relevant classes.

Nonetheless, it can still make a prediction of microbial growth including parameter uncertainty based on a growth model fitted using fit\_MCMC\_growth() or fit\_multiple\_growth\_MCMC(). This function predicts growth curves for niter samples (with replacement) of the samples of the MCMC algorithm. Then, credible intervals are calculated based on the quantiles of the model predictions at each time point.

#### Usage

```
predict_MCMC_growth(
   MCMCfit,
   times,
   env_conditions,
   niter,
   newpars = NULL,
   formula = . ~ time
)
```

#### **Arguments**

MCMCfit An instance of FitDynamicGrowthMCMC or FitMultipleGrowthMCMC.

times Numeric vector of storage times for the predictions.

env\_conditions Tibble with the (dynamic) environmental conditions during the experiment. It

must have one column named 'time' with the storage time and as many columns

as required with the environmental conditions.

niter Number of iterations.

newpars A named list defining new values for the some model parameters. The name

must be the identifier of a model already included in the model. These parameters do not include variation, so defining a new value for a fitted parameters

"fixes" it. NULL by default (no new parameters).

formula A formula stating the column named defining the elapsed time in env\_conditions.

By default, . ~ time.

#### Value

An instance of MCMCgrowth().

## **Examples**

```
## We need a FitDynamicGrowthMCMC object

data("example_dynamic_growth")
data("example_env_conditions")

sec_model_names <- c(temperature = "CPM", aw= "CPM")

known_pars <- list(Nmax = 1e4, # Primary model
    N0 = 1e0, Q0 = 1e-3, # Initial values of the primary model
    mu_opt = 4, # mu_opt of the gamma model
    temperature_n = 1, # Secondary model for temperature
    aw_xmax = 1, aw_xmin = .9, aw_n = 1 # Secondary model for water activity
)

my_start <- list(temperature_xmin = 25, temperature_xopt = 35,
    temperature_xmax = 40,
    aw_xopt = .95)</pre>
```

```
set.seed(12124) # Setting seed for repeatability
my_MCMC_fit <- fit_MCMC_growth(example_dynamic_growth, example_env_conditions,</pre>
    my_start, known_pars, sec_model_names, niter = 3000)
## Define the conditions for the simulation
my_times < - seq(0, 15, length = 50)
niter <- 2000
newpars <- list(N0 = 1e-1, # A parameter that was fixed</pre>
                temperature_xmax = 120  # A parameter that was fitted
## Make the simulations
my_MCMC_prediction <- predict_MCMC_growth(my_MCMC_fit,</pre>
    example_env_conditions, # It could be different from the one used for fitting
    niter,
    newpars)
## We can plot the prediction interval
plot(my_MCMC_prediction)
## We can also get the quantiles at each time point
print(my_MCMC_prediction$quantiles)
```

predict\_stochastic\_growth

Deprecated isothermal growth with parameter uncertainty

# **Description**

#### [Deprecated]

predict\_stochastic\_growth() was renamed predict\_growth\_uncertainty() because the original function name may be misleading, as this is not a stochastic differential equation

# Usage

```
predict_stochastic_growth(
  model_name,
  times,
  n_sims,
```

```
pars,
  corr_matrix = diag(nrow(pars)),
  check = TRUE
)
```

#### **Arguments**

model\_name Character describing the primary growth model.

times Numeric vector of storage times for the simulations.

n\_sims Number of simulations.

pars A tibble describing the parameter uncertainty (see details).

corr\_matrix Correlation matrix of the model parameters. Defined in the same order as in

pars. An identity matrix by default (uncorrelated parameters).

check Whether to do some tests. FALSE by default.

# **Description**

Predictions of the coupled Baranyi model

# Usage

```
pred_coupled_baranyi(p, temp, times)
```

# Arguments

p a numeric vector of model parameters. Must have entries logN0, logNmax,

logC0, b and Tmin

temp a numeric vector of temperature values

times a numeric vector of time points for the prediction

#### Value

a numeric vector of predicted logN (in log CFU/TIME)

pred\_lambda 117

pred\_lambda

Prediction of lambda for the coupled model

# Description

Prediction of lambda for the coupled model

# Usage

```
pred_lambda(p, temp)
```

# Arguments

p numeric vector (or list) of model parameters. Must have entries logC0, b and

Tmin

temp numeric vector of temperatures

# Value

the values of lambda

pred\_sqmu

Prediction of the square root of mu for the coupled model

# **Description**

Prediction of the square root of mu for the coupled model

# Usage

```
pred_sqmu(p, temp)
```

#### **Arguments**

p numeric vector (or list) of model parameters. Must have entries b and Tmin

temp numeric vector of temperatures

#### Value

the values of the square root of mu (in ln CFU/TIME)

118 Q0\_to\_lambda

primary\_model\_data

Metainformation of primary growth models

#### **Description**

#### [Stable]

Provides different types of meta-data about the primary growth models included in biogrowth. This information is the basis of the automatic checks, and can also help in the definition of models for predict\_growth() and fit\_growth().

# Usage

```
primary_model_data(model_name = NULL)
```

# **Arguments**

model\_name

The name of the model or NULL (default).

#### Value

If model\_name is NULL, returns a character string with the available models. If is a valid identifier, it returns a list with metainformation about the model. If model\_name name is not a valid identifier, raises an error.

Q0\_to\_lambda

Lag phase duration from Q0

# **Description**

#### [Stable]

Convenience function to calculate the lag phase duration (lambda) of the Baranyi model from the maximum specific growth rate and the initial value of the variable Q.

Note that this function uses the unit system of biogrowth (i.e. log10). Care must be taken when using parameters obtained from other sources.

## Usage

```
Q0_to_lambda(q0, mu, logbase_mu = 10)
```

#### **Arguments**

q0 Initial value of the variable Q.

mu Specific growth rate in the exponential phase.

logbase\_mu Base of the logarithm the growth rate is referred to. By default, 10 (i.e. log10).

See vignette about units for details.

refrigeratorSpain 119

emperature recorded in refrigerators	frigeratorSpain
--------------------------------------	-----------------

# Description

This dataset includes the temperature recorded in refrigerators in households of the Catalonia region. The data was published as part of Jofre et al. (2019) Domestic refrigerator temperatures in Spain: Assessment of its impact on the safety and shelf-life of cooked meat products. Food Research International, 126, 108578. And was kindly provided by the original authors of the study.

## Usage

```
refrigeratorSpain
```

#### **Format**

A tibble with three columns:

- time: elapsed time in hours
- A1: temperature observed in refrigerator "1"
- A2: temperature observed in refrigerator "2"

residuals\_lambda Residuals for lambda for the coupled model

# **Description**

Residuals for lambda for the coupled model

# Usage

```
residuals_lambda(p, my_d)
```

# **Arguments**

р	numeric vector (or list) of model parameters. Must have entries logC0, b and
	Tmin
my_d	tibble (or data.frame) of data. It must have one column named temp (tempera-
	ture) and one named lambda (specific growth rate: in In CFLI/TIME)

#### Value

vector of residuals

120 richards\_model

resi	duals	samu

Residuals for the square root of mu for the coupled model

# Description

Residuals for the square root of mu for the coupled model

# Usage

```
residuals_sqmu(p, my_d)
```

# **Arguments**

p numeric vector (or list) of model parameters. Must have entries b and Tmin

my\_d tibble (or data.frame) of data. It must have one column named temp (tempera-

ture) and one named mu (specific growth rate; in ln CFU/TIME).

#### Value

vector of residuals

richards\_model

Richards growth model

# **Description**

Richards growth model

# Usage

```
richards_model(times, logN0, mu, lambda, C, nu)
```

# Arguments

times	Numeric vector of storage times
logN0	Initial log microbial count

mu Maximum specific growth rate (in ln CFU/t)

lambda Lag phase duration

C Difference between logN0 and the maximum log-count.

nu Parameter describing the transition between growth phases

Rossoaw\_model 121

Rossoaw\_model

Secondary Rosso model for water activity

## **Description**

Secondary model for water activity as defined by Aryani et al. (2001).

#### Usage

```
Rossoaw_model(x, xmin)
```

#### **Arguments**

x Value of the environmental factor (in principle, aw). xmin Minimum value for growth (in principle, aw).

#### Value

The corresponding gamma factor.

SecondaryComparison

SecondaryComparison class

#### **Description**

The SecondaryComparison class contains several functions for model comparison and model selection of growth models. It should not be instanced directly. Instead, it should be constructed using compare\_secondary\_fits().

It includes two type of tools for model selection and comparison: statistical indexes and visual analyses. Please check the sections below for details.

Note that all these tools use the names defined in compare\_secondary\_fits(), so we recommend passing a named list to that function.

# Usage

```
## S3 method for class 'SecondaryComparison'
coef(object, ...)

## S3 method for class 'SecondaryComparison'
summary(object, ...)

## S3 method for class 'SecondaryComparison'
print(x, ...)

## S3 method for class 'SecondaryComparison'
plot(x, y, ..., type = 1, add_trend = TRUE)
```

## **Arguments**

object	an instance of SecondaryComparison
	ignored
x	an instance of SecondaryComparison
У	ignored
type	if type==1, the plot compares the model predictions. If type ==2, the plot compares the parameter estimates.
add_trend	should a trend line of the residuals be added for type==3? TRUE by default

# Methods (by generic)

• coef(SecondaryComparison): table of parameter estimates

• summary(SecondaryComparison): summary table for the comparison

• print(SecondaryComparison): print of the model comparison

• plot(SecondaryComparison): illustrations comparing the fitted models

#### Statistical indexes

SecondaryComparison implements two S3 methods to obtain numerical values to facilitate model comparison and selection.

- the coef method returns a tibble with the values of the parameter estimates and their corresponding standard errors for each model.
- the summary returns a tibble with the AIC, number of degrees of freedom, mean error and root mean squared error for each model.

## Visual analyses

The S3 plot method can generate three types of plots:

- when type = 1, the plot compares the observations against the model predictions for each model. The plot includes a linear model fitted to the residuals. In the case of a perfect fit, the line would have slope=1 and intercept=0 (shown as a black, dashed line).
- when type = 2, the plot compares the parameter estimates using error bars, where the limits of the error bars are the expected value +/- one standard error. In case one model does not has some model parameter (i.e. either because it is not defined or because it was fixed), the parameter is not included in the plot.

secondary\_model\_data 123

# Description

# [Stable]

Provides different types of meta-data about the secondary growth models included in biogrowth. This information is the basis of the automatic checks, and can also help in the definition of models for predict\_growth() and fit\_growth().

#### Usage

```
secondary_model_data(model_name = NULL)
```

# **Arguments**

model\_name

The name of the model or NULL (default).

#### Value

If model\_name is NULL, returns a character string with the available models. If is a valid identifier, it returns a list with metainformation about the model. If model\_name name is not a valid identifier, raises an error.

show\_guess\_dynamic

Plot of the initial guess for growth under dynamic environmental conditions

# **Description**

Compares the prediction corresponding to a guess of the parameters of the model against experimental data

# Usage

```
show_guess_dynamic(
  fit_data,
  model_keys,
  guess,
  env_conditions,
  logbase_mu = 10,
  formula = logN ~ time
)
```

# Arguments

fit_data	Tibble (or data.frame) of data for the fit. It must have two columns, one with the elapsed time (time by default) and another one with the decimal logarithm of the population size (logN by default). Different column names can be defined using the formula argument.
model_keys	Named the equations of the secondary model as in fit_growth()
guess	Named vector with the initial guess of the model parameters as in fit_growth()
env_conditions	Tibble describing the variation of the environmental conditions for dynamic experiments. See fit_growth().
logbase_mu	Base of the logarithm the growth rate is referred to. By default, 10 (i.e. log10). See vignette about units for details.
formula	an object of class "formula" describing the x and y variables. $logN \sim time$ as a default.

# Value

A ggplot2::ggplot() comparing the model prediction against the data

show_guess_primary	Plot of the initial guess for growth under constant environmental con-
	ditions

# Description

Compares the prediction corresponding to a guess of the parameters of the primary model against experimental data

# Usage

```
show_guess_primary(
  fit_data,
  model_name,
  guess,
  logbase_mu = 10,
  formula = logN ~ time
)
```

# Arguments

fit_data	Tibble (or data.frame) of data for the fit. It must have two columns, one with the elapsed time (time by default) and another one with the decimal logarithm of the population size (logN by default). Different column names can be defined using the formula argument.
model_name	Character defining the primary growth model as per primary_model_data()
guess	Named vector with the initial guess of the model parameters

StochasticGrowth 125

logbase\_mu

Base of the logarithm the growth rate is referred to. By default, 10 (i.e. log10).

See vignette about units for details.

formula

an object of class "formula" describing the x and y variables. logN ~ time as a

default.

#### Value

A ggplot2::ggplot() comparing the model prediction against the data

StochasticGrowth StochasticGrowth class

# **Description**

#### [Deprecated]

The class StochasticGrowth has been deprecated by class GrowthUncertainty, which provides less misleading name.

Still, it is still returned if the deprecated predict\_stochastic\_growth() is called.

The StochasticGrowth class contains the results of a growth prediction under isothermal conditions considering parameter unceratinty. Its constructor is predict\_stochastic\_growth().

It is a subclass of list with the items:

- sample: parameter sample used for the calculations.
- simulations: growth curves predicted for each parameter.
- quantiles: limits of the credible intervals (5%, 10%, 50%, 90%, 95%) for each time point.
- model: Model used for the calculations.
- mus: Mean parameter values used for the simulations.
- sigma: Variance-covariance matrix used for the simulations.

#### Usage

```
## S3 method for class 'StochasticGrowth'
print(x, ...)

## S3 method for class 'StochasticGrowth'
plot(
    x,
    y = NULL,
    ...,
    line_col = "black",
    line_size = 0.5,
    line_type = "solid",
    ribbon80_fill = "grey",
    ribbon90_fill = "grey",
    alpha80 = 0.5,
    alpha90 = 0.4
)
```

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# **Arguments**

The object of class StochasticGrowth to plot.
ignored.
ignored
Aesthetic parameter to change the colour of the line geom in the plot, see: ggplot2::geom_line()
Aesthetic parameter to change the thickness of the line geom in the plot, see: ggplot2::geom_line()
Aesthetic parameter to change the type of the line geom in the plot, takes numbers (1-6) or strings ("solid") see: ggplot2::geom_line()
fill colour for the space between the 10th and 90th quantile, see: ggplot2::geom_ribbon()
fill colour for the space between the 5th and 95th quantile, see: ggplot2::geom_ribbon()
transparency of the ribbon aesthetic for the space between the 10th and 90th quantile. Takes a value between 0 (fully transparant) and 1 (fully opaque)
transparency of the ribbon aesthetic for the space between the 5th and 95th quantile. Takes a value between 0 (fully transparant) and 1 (fully opaque).

# **Details**

FitIsoGrowth class

# Methods (by generic)

- print(StochasticGrowth): print of the model
- plot(StochasticGrowth): Growth prediction (prediction band) considering parameter uncertainty.

TimeDistribution	TimeDistribution class	
------------------	------------------------	--

# Description

The TimeDistribution class contains an estimate of the probability distribution of the time to reach a given microbial count. Its constructor is distribution\_to\_logcount().

It is a subclass of list with the items:

- distribution Sample of the distribution of times to reach log\_count.
- summary Summary statistics of distribution (mean, sd, median, q10 and q90).

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## Usage

```
## S3 method for class 'TimeDistribution'
print(x, ...)
## S3 method for class 'TimeDistribution'
summary(object, ...)
## S3 method for class 'TimeDistribution'
plot(x, y = NULL, ..., bin_width = NULL)
```

#### **Arguments**

x The object of class TimeDistribution to plot.

... ignored.

object An instance of TimeDistribution.

y ignored.

bin\_width A number that specifies the width of a bin in the histogram, see: ggplot2::geom\_histogram().

NULL by default.

## Methods (by generic)

• print(TimeDistribution): print of the model

• summary(TimeDistribution): summary of the model

• plot(TimeDistribution): plot of the distribution of the time to reach a microbial count.

time\_to\_logcount

Time to reach a given microbial count

# **Description**

#### [Superseded]

The function time\_to\_logcount() has been superseded by function time\_to\_size(), which provides a more general interface.

But it still returns the storage time required for the microbial count to reach log\_count according to the predictions of model. Calculations are done using linear interpolation of the model predictions.

# Usage

```
time_to_logcount(model, log_count)
```

# Arguments

model An instance of IsothermalGrowth or DynamicGrowth.

log\_count The target log microbial count.

time\_to\_size

# Value

The predicted time to reach log\_count.

# **Examples**

```
## First of all, we will get an IsothermalGrowth object

my_model <- "modGompertz"

my_pars <- list(logN0 = 2, C = 6, mu = .2, lambda = 25)

my_time <- seq(0, 100, length = 1000)

static_prediction <- predict_isothermal_growth(my_model, my_time, my_pars)
plot(static_prediction)

## And now we calculate the time to reach a microbial count

time_to_logcount(static_prediction, 2.5)

## If log_count is outside the range of the predicted values, NA is returned

time_to_logcount(static_prediction, 20)</pre>
```

time\_to\_size

Time for the population to reach a given size

# **Description**

# [Experimental]

Calculates the elapsed time required for the population to reach a given size (in log scale)

# Usage

```
time_to_size(model, size, type = "discrete", logbase_logN = NULL)
```

# **Arguments**

model	An instance of GrowthPrediction, GrowthFit, GlobalGrowthFit, GrowthUncertainty or MCMCgrowth.
size	Target population size (in log scale)
type	Tye of calculation, either "discrete" (default) or "distribution"
logbase_logN	Base of the logarithm for the population size. By default, 10 (i.e. log10). See vignette about units for details.

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#### **Details**

The calculation method differs depending on the value of type. If type="discrete" (default), the function calculates by linear interpolation a discrete time to reach the target population size. If type="distribution", this calculation is repeated several times, generating a distribution of the time. Note that this is only possible for instances of GrowthUncertainty or MCMCgrowth.

#### Value

If type="discrete", a number. If type="distribution", an instance of TimeDistribution.

#### **Examples**

```
## Example 1 - Growth predictions ------
## The model is defined as usual with predict_growth
my_model <- list(model = "modGompertz", logN0 = 0, C = 6, mu = .2, lambda = 20)
my_time \leftarrow seq(0, 100, length = 1000) # Vector of time points for the calculations
my_prediction <- predict_growth(my_time, my_model, environment = "constant")</pre>
plot(my_prediction)
## We just have to pass the model and the size (in log10)
time_to_size(my_prediction, 3)
## If the size is not reached, it returns NA
time_to_size(my_prediction, 8)
## By default, it considers the population size is defined in the same log-base
## as the prediction. But that can be changed using logbase_logN
time_to_size(my_prediction, 3)
time_to_size(my_prediction, 3, logbase_logN = 10)
time_to_size(my_prediction, log(100), logbase_logN = exp(1))
## Example 2 - Model fit -------
my_{data} \leftarrow data.frame(time = c(0, 25, 50, 75, 100),
                     logN = c(2, 2.5, 7, 8, 8))
models <- list(primary = "Baranyi")</pre>
known \leftarrow c(mu = .2)
start \leftarrow c(logNmax = 8, lambda = 25, logN0 = 2)
primary_fit <- fit_growth(my_data, models, start, known,</pre>
                         environment = "constant",
```

trilinear\_model

```
)
plot(primary_fit)
time_to_size(primary_fit, 4)
## Example 3 - Global fitting ------
## We need a model first
data("multiple_counts")
data("multiple_conditions")
sec_models <- list(temperature = "CPM", pH = "CPM")</pre>
known_pars <- list(Nmax = 1e8, N0 = 1e0, Q0 = 1e-3,</pre>
                   temperature_n = 2, temperature_xmin = 20,
                   temperature\_xmax = 35,
                   temperature_xopt = 30,
                   pH_n = 2, pH_xmin = 5.5, pH_xmax = 7.5, pH_xopt = 6.5)
my_start <- list(mu_opt = .8)</pre>
global_fit <- fit_growth(multiple_counts,</pre>
                        sec_models,
                        my_start,
                         known_pars,
                         environment = "dynamic",
                         algorithm = "regression",
                         approach = "global",
                         env_conditions = multiple_conditions
                         )
plot(global_fit)
## The function calculates the time for each experiment
time_to_size(global_fit, 3)
## It returns NA for the particular experiment if the size is not reached
time_to_size(global_fit, 4.5)
```

trilinear\_model

Trilinear growth model

# **Description**

Trilinear growth model defined by Buchanan et al. (1997).

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#### Usage

```
trilinear_model(times, logN0, mu, lambda, logNmax)
```

# **Arguments**

times Numeric vector of storage times logN0 Initial log microbial count

mu Maximum specific growth rate (in ln CFU/t)

lambda Lag phase duration

logNmax Maximum log microbial count

#### Value

Numeric vector with the predicted microbial count.

zwietering\_gamma model

# **Description**

Gamma model as defined by Zwietering et al. (1992). To avoid unreasonable predictions, it has been modified setting gamma=0 for values of x outside (xmin, xopt)

# Usage

```
zwietering_gamma(x, xmin, xopt, n)
```

# **Arguments**

x Value of the environmental factor.

xmin Minimum value of the environmental factor for growth.

xopt Maximum value for growth

n Exponent of the secondary model

# Value

The corresponding gamma factor.

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