

Package ‘ale’

September 12, 2025

Title Interpretable Machine Learning and Statistical Inference with
Accumulated Local Effects (ALE)

Version 0.5.3

Description Accumulated Local Effects (ALE) were initially developed as a model-agnostic approach for global explanations of the results of black-box machine learning algorithms. ALE has a key advantage over other approaches like partial dependency plots (PDP) and SHapley Additive exPlanations (SHAP): its values represent a clean functional decomposition of the model. As such, ALE values are not affected by the presence or absence of interactions among variables in a mode. Moreover, its computation is relatively rapid. This package reimplements the algorithms for calculating ALE data and develops highly interpretable visualizations for plotting these ALE values. It also extends the original ALE concept to add bootstrap-based confidence intervals and ALE-based statistics that can be used for statistical inference. For more details, see Okoli, Chitu. 2023. “Statistical Inference Using Machine Learning and Classical Techniques Based on Accumulated Local Effects (ALE).” arXiv. <doi:10.48550/arXiv.2310.09877>.

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Language en-ca

Encoding UTF-8

RoxygenNote 7.3.2

Suggests knitr, mgcv, nnet, readr, rmarkdown, testthat (>= 3.0.0),
yaImpute

VignetteBuilder knitr

Imports broom, cli, dplyr, furrr, future, ggplot2, insight, methods,
patchwork, progressr, purrr, rlang, S7, staccuracy, stats,
stringr, tidyr, univariateML, utils

Depends R (>= 4.2.0)

URL <https://github.com/tripartio/ale>, <https://tripartio.github.io/ale/>

BugReports <https://github.com/tripartio/ale/issues>

Config/testthat/edition 3

Config/testthat/parallel true

Config/testthat/start-first ALE-numerical, ALE-binary,
ALE-categorical, ModelBoot, ALEPlot-gold-standard, ALEpDist
LazyData true
NeedsCompilation no
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Repository CRAN
Date/Publication 2025-09-12 18:20:02 UTC

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ALE	<i>ALE data and statistics that describe a trained model</i>
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Description

An ALE S7 object contains ALE data and statistics. For details, see vignette('ale-intro') or the details and examples below.

Usage

```

ALE(
  model,
  x_cols = list(d1 = TRUE),
  data = NULL,
  y_col = NULL,
  ...,
  exclude_cols = NULL,
  parallel = "all",
  model_packages = NULL,
  output_stats = TRUE,
  output_boot_data = FALSE,
  pred_fun = function(object, newdata, type = pred_type) {
    stats::predict(object =
      object, newdata = newdata, type = type)
  },
  pred_type = "response",
  p_values = "auto",
  aler_alpha = c(0.01, 0.05),
  max_num_bins = 10,
  boot_it = 0,
  boot_alpha = 0.05,
  boot_centre = "mean",
  seed = 0,
  y_type = NULL,
  sample_size = 500,
  silent = FALSE,
  .bins = NULL
)

```

Arguments

<code>model</code>	model object. Required. Model for which ALE should be calculated. May be any kind of R object that can make predictions from data.
<code>x_cols</code> , <code>exclude_cols</code>	character, list, or formula. Columns names from data requested in one of the special <code>x_cols</code> formats for which ALE data is to be calculated. Defaults to 1D ALE for all columns in data except <code>y_col</code> . See details in the documentation for resolve_x_cols() .
<code>data</code>	dataframe. Dataset from which to create predictions for the ALE. It should normally be the same dataset on which model was trained. If not provided, <code>ALE()</code> will try to detect it automatically if it is included in the model object.
<code>y_col</code>	character(1). Name of the outcome target label (y) variable. If not provided, <code>ALE()</code> will try to detect it automatically from the model object. For non-standard models, <code>y_col</code> should be provided. For time-to-event (survival) models, see details.
<code>...</code>	not used. Inserted to require explicit naming of subsequent arguments.

<code>parallel</code>	non-negative integer(1) or character(1) in <code>c("all", "all but one")</code> . Number of parallel threads (workers or tasks) for parallel execution of the constructor. The default "all" uses all available physical and logical CPU cores. "all but one" uses only physical cores and reserves one core for the system. Set <code>parallel = 0</code> to disable parallel processing. See details.
<code>model_packages</code>	character. Character vector of names of packages that <code>model</code> depends on that might not be obvious with parallel processing. If you get weird error messages when parallel processing is enabled (which is the default) but they are resolved by setting <code>parallel = 0</code> , you might need to specify <code>model_packages</code> . See details.
<code>output_stats</code>	logical(1). If TRUE (default), return ALE statistics.
<code>output_boot_data</code>	logical(1). If TRUE, return the raw ALE data for each bootstrap iteration. Default is FALSE.
<code>pred_fun, pred_type</code>	function, character(1). <code>pred_fun</code> is a function that returns a vector of predicted values of type <code>pred_type</code> from <code>model</code> on data. See details.
<code>p_values</code>	instructions for calculating p-values. Possible values are: • NULL: p-values are not calculated. • An <code>ALEpDist</code> object: the object will be used to calculate p-values. • "auto" (default): If statistics are requested (<code>output_stats = TRUE</code>) and bootstrapping is requested (<code>boot_it > 0</code>), the constructor will try to automatically create a fast surrogate <code>ALEpDist</code> object; otherwise, no p-values are calculated. However, automatic creation of a surrogate <code>ALEpDist</code> object only works with standard R model types. If the automatic process errors, then you must explicitly create and provide an <code>ALEpDist()</code> object. Note: although faster surrogate p-values are convenient for interactive analysis, they are not acceptable for definitive conclusions or publication. See details below.
<code>aler_alpha</code>	numeric(2) from 0 to 1. Thresholds for p-values ("alpha") for confidence interval ranges for the ALER band if <code>p_values</code> are provided (that is, not NULL). The inner band range will be the median value of $y \pm \text{aler_alpha}[2]$ of the relevant ALE statistic (usually ALE range or normalized ALE range). When there is a second outer band, its range will be the median $\pm \text{aler_alpha}[1]$. For example, in the ALE plots, for the default <code>aler_alpha = c(0.01, 0.05)</code> , the inner band will be the median $\pm$ ALER minimum or maximum at $p = 0.05$ and the outer band will be the median $\pm$ ALER minimum or maximum at $p = 0.01$.
<code>max_num_bins</code>	positive integer(1). Maximum number of ALE bins for numeric <code>x_cols</code> variables. The number of bins is eventually the lower of the number of unique values of a numeric variable and <code>max_num_bins</code> . Non-numeric variables such as (binary or categorical) always use all their actual values for ALE bins.
<code>boot_it</code>	non-negative integer(1). Number of bootstrap iterations for data-only bootstrapping on ALE data. This is appropriate for models that have been developed with cross-validation. For models that have not been validated, full-model bootstrapping should be used instead with a <code>ModelBoot()</code> class object. See details there. The default <code>boot_it = 0</code> turns off bootstrapping.

<code>boot_alpha</code>	numeric(1) from 0 to 1. When ALE is bootstrapped (<code>boot_it > 0</code>), <code>boot_alpha</code> specifies the thresholds for p-values ("alpha") for percentile-based confidence interval range for the bootstrapped ALE values. The bootstrap confidence intervals will be the lowest and highest $(1 - 0.05) / 2$ percentiles. For example, if <code>boot_alpha = 0.05</code> (default), the confidence intervals will be from the 2.5 (low) and 97.5 (high) percentiles.
<code>boot_centre</code>	character(1) in <code>c('mean', 'median')</code> . When bootstrapping, the main estimate for the ALE y value is considered to be <code>boot_centre</code> . Regardless of the value specified here, both the mean and median will be available.
<code>seed</code>	integer(1). Random seed. Supply this between runs to assure that identical random ALE data is generated each time when bootstrapping. Without bootstrapping, ALE is a deterministic algorithm that should result in identical results each time regardless of the seed specified. However, with parallel processing enabled (as it is by default), only the exact computing setup will give reproducible results. For reproducible results across different computers, turn off parallelization with <code>parallel = 0</code> .
<code>y_type</code>	character(1) in <code>c('binary', 'numeric', 'categorical', 'ordinal')</code> . Datatype of the y (outcome) variable. Normally determined automatically; only provide if an error message for a complex non-standard model requires it.
<code>sample_size</code>	non-negative integer(1). Size of the sample of data to be returned with the ALE object. This is primarily used for rug plots in ALEPlots() .
<code>silent</code>	logical(1), default FALSE. If TRUE, do not display any non-essential messages during execution (such as progress bars). Regardless, any warnings and errors will always display. See details for how to customize progress bars.
<code>.bins</code>	Internal use only. List of ALE bin and n count vectors. If provided, these vectors will be used to set the intervals of the ALE x axis for each variable. By default (NULL), ALE() automatically calculates the bins. <code>.bins</code> is normally used in advanced analyses where the bins from a previous analysis are reused for subsequent analyses (for example, for full model bootstrapping with ModelBoot()).

Value

An object of class ALE with properties `effect` and `params`.

Properties

effect Stores the ALE data and, optionally, ALE statistics and bootstrap data for one or more categories.

params The parameters used to calculate the ALE data. These include most of the arguments used to construct the ALE object. These are either the values provided by the user or those used by default if the user did not change them but also includes several objects that are created within the constructor. These extra objects are described here, as well as those parameters that are stored differently from the form in the arguments:

- * ``max_d``: the highest dimension of ALE data present. If only 1D ALE is present, then ``max_d == 1``. I
- * ``requested_x_cols``, ``ordered_x_cols``: ``requested_x_cols`` is the resolved list of ``x_cols`` as requ
- * ``y_cats``: categories for categorical classification models. For non-categorical models, this is t

- * ``y_type``: high-level datatype of the y outcome variable.
- * ``y_summary``: summary statistics of y values used for the ALE calculation. These statistics are based on the y values.
- * ``min``, ``mean``, ``max``: the minimum, mean, and maximum y values, respectively. Note that the median is not included.
- * ``aler_lo_lo``, ``aler_lo``, ``aler_hi``, ``aler_hi_hi``: When p-values are present, ``aler_lo`` and ``aler_hi`` are the lower and upper bounds of the ALE effect, respectively.
- * ``model``: selected elements that describe the ``model`` that the ``ALE`` object interprets.
- * ``data``: selected elements that describe the ``data`` used to produce the ``ALE`` object. To avoid the use of ``data``, the user can pass ``newdata`` to the ``predict`` function.
- * ``probs_inverted``: ``TRUE`` if the original probability values of the ALE object have been inverted.

Custom predict function

The calculation of ALE requires modifying several values of the original data. Thus, `ALE()` needs direct access to the `predict` function for the model. By default, `ALE()` uses a generic default `predict` function of the form `predict(object, newdata, type)` with the default prediction type of `'response'`. If, however, the desired prediction values are not generated with that format, the user must specify what they want. Very often, the only modification needed is to change the prediction type to some other value by setting the `pred_type` argument (e.g., to `'prob'` to generate classification probabilities). But if the desired predictions need a different function signature, then the user must create a custom prediction function and pass it to `pred_fun`. The requirements for this custom function are:

- It must take three required arguments and nothing else:
 - `object`: a model
 - `newdata`: a dataframe or compatible table type such as a tibble or `data.table`
 - `type`: a string; it should usually be specified as `type = pred_type`. These argument names are according to the R convention for the generic `stats::predict()` function.
- It must return a vector or matrix of numeric values as the prediction.

You can see an example below of a custom prediction function.

ALE statistics and p-values

For details about the ALE-based statistics (ALED, ALER, NALED, and NALER), see `vignette('ale-statistics')`. For general details about the calculation of p-values, see `ALEpDist()`. Here, we clarify the automatic calculation of p-values with the `ALE()` constructor.

As explained in the documentation above for the `p_values` argument, the default `p_values = "auto"` will try to automatically create a fast surrogate `ALEpDist` object. However, this is on the condition that statistics are requested (default, `output_stats = TRUE`) and bootstrapping is also requested (not default, if `boot_it` is any value greater than 0). Requesting statistics is necessary otherwise p-values are not needed. However, the requirement for requiring bootstrapping is a pragmatic design choice. The challenge is that creating an `ALEpDist` object can be slow. (Even the fast surrogate option rarely takes less than 10 seconds, even with parallelization.) Thus, to optimize speed, p-values will not be calculated unless requested. However, if the user requests bootstrapping (which is slower than not requesting it), it can be assumed that they are willing to sacrifice some speed for the sake of greater precision in their ALE analysis; thus, extra time is taken to at least create a relatively faster surrogate `ALEpDist` object.

Parallel processing

Parallel processing using the `{furrr}` framework is enabled by default. The number of parallel threads (workers or cores) is specified with the `parallel` argument. By default (`parallel = "all"`), it will use all the available physical and logical CPU cores. However, if the procedure is very slow (with a large dataset and slow prediction algorithm), you might want to set `parallel = "all but one"`, which will only use faster physical cores and reserve one physical core so that your computer does not slow down as you continue working on other tasks while the procedure runs. To disable parallel processing, set `parallel = 0`.

The `{ale}` package should be able to automatically recognize and load most packages that are needed, but with parallel processing enabled (which is the default), some packages might not be properly loaded. This problem might be indicated if you get a strange error message that mentions something somewhere about "progress interrupted" or "future", especially if you see such errors after the progress bars begin displaying (assuming you did not disable progress bars with `silent = TRUE`). In that case, first try disabling parallel processing with `parallel = 0`. If that resolves the problem, then to get faster parallel processing to work, try adding all the package names needed for the model to the `model_packages` argument, e.g., `model_packages = c('tidymodels', 'mgcv')`.

Time-to-event (survival) models

For time-to-event (survival) models, set the following arguments:

- `y_col` must be set to the name of the binary event column.
- Include the time column in the `exclude_cols` argument so that its ALE will not be calculated, e.g., `exclude_cols = 'time'`. This is not essential but if it is not excluded, it will always result in an exactly zero ALE effect because time is an outcome, not a predictor, of the time-to-event model's outcome, so calculating it is a waste of time.
- `pred_type` must be specified according to the desired type argument for the `predict()` method of the time-to-event algorithm (e.g., "risk", "survival", "time", etc.).
- `pred_fun` might work fine without modification as long as the settings above are configured. However, for non-standard time-to-event models, a custom `pred_fun` as specified above might be needed.

Progress bars

Progress bars are implemented with the `{progressr}` package. For details on customizing the progress bars, see the introduction to the `{progressr}` package. To disable progress bars when calling a function in the `ale` package, set `silent = TRUE`.

References

Okoli, Chitu. 2023. "Statistical Inference Using Machine Learning and Classical Techniques Based on Accumulated Local Effects (ALE)." arXiv. doi:10.48550/arXiv.2310.09877.

Examples

```
# Load diamonds dataset with some cleanup
library(dplyr)
diamonds <- ggplot2::diamonds |>
```

```

filter(!(x == 0 | y == 0 | z == 0)) |>
# https://lorentzen.ch/index.php/2021/04/16/a-curious-fact-on-the-diamonds-dataset/
distinct(
  price, carat, cut, color, clarity,
  .keep_all = TRUE
) |>
rename(
  x_length = x,
  y_width = y,
  z_depth = z,
  depth_pct = depth
)

# Create a GAM model with flexible curves to predict diamond price
# Smooth all numeric variables and include all other variables
gam_diamonds <- mgcv::gam(
  price ~ s(carat) + s(depth_pct) + s(table) + s(x_length) + s(y_width) + s(z_depth) +
    cut + color + clarity,
  data = diamonds
)
summary(gam_diamonds)

# Simple ALE without bootstrapping: by default, all 1D ALE effects

# For speed, these examples use retrieve_rds() to load pre-created objects
# from an online repository.
# To run the code yourself, execute the code blocks directly.
serialized_objects_site <- "https://github.com/tripartio/ale/raw/main/download"

# Create ALE data
ale_gam_diamonds <- retrieve_rds(
  # For speed, load a pre-created object by default.
  c(serialized_objects_site, 'ale_gam_diamonds.0.5.2.rds'),
  {
    # To run the code yourself, execute this code block directly.
    # For standard models like mgcv::gam that store their data,
    # there is no need to specify the data argument.
    ALE(gam_diamonds)
  }
)

# Simple printing of all plots
plot(ale_gam_diamonds)

# Bootstrapped ALE
# This can be slow, since bootstrapping runs the algorithm boot_it times.
# In addition, bootstrapping automatically generates surrogate p-values by default.

# Create ALE with 100 bootstrap samples

```

```

ale_gam_diamonds_boot <- retrieve_rds(
  # For speed, load a pre-created object by default.
  c(serialized_objects_site, 'ale_gam_diamonds_boot.0.5.2.rds'),
  {
    # To run the code yourself, execute this code block directly.
    ALE(
      gam_diamonds,
      # request all 1D ALE effects and only the carat:clarity 2D effect
      list(d1 = TRUE, d2 = 'carat:clarity'),
      boot_it = 100
    )
  }
)
# saveRDS(ale_gam_diamonds_boot, file.choose())

# More advanced plot manipulation
ale_plots <- plot(ale_gam_diamonds_boot) # Create an ALEPlots object

# Print the plots: First page prints 1D ALE; second page prints 2D ALE
ale_plots # or print(ale_plots) to be explicit

# Extract specific plots (as lists of ggplot objects)
get(ale_plots, 'carat') # extract a specific 1D plot
get(ale_plots, 'carat:clarity') # extract a specific 2D plot
get(ale_plots, type = 'effect') # ALE effects plot
# See help(get.ALEPlots) for more options, such as for categorical plots

# If the predict function you want is non-standard, you may define a
# custom predict function. It must return a single numeric vector.
custom_predict <- function(object, newdata, type = pred_type) {
  predict(object, newdata, type = type, se.fit = TRUE)$fit
}

ale_gam_diamonds_custom <- retrieve_rds(
  # For speed, load a pre-created object by default.
  c(serialized_objects_site, 'ale_gam_diamonds_custom.0.5.2.rds'),
  {
    # To run the code yourself, execute this code block directly.
    ALE(
      gam_diamonds,
      pred_fun = custom_predict,
      pred_type = 'link'
    )
  }
)
# saveRDS(ale_gam_diamonds_custom, file.choose())

# Plot the ALE data
plot(ale_gam_diamonds_custom)

```

```
# How to retrieve specific types of ALE data from an ALE object.
ale_diamonds_with_boot_data <- retrieve_rds(
  # For speed, load a pre-created object by default.
  c(serialized_objects_site, 'ale_diamonds_with_boot_data.0.5.2.rds'),
  {
    # To run the code yourself, execute this code block directly.
    # For standard models like mgcv::gam that store their data,
    # there is no need to specify the data argument.
    ALE(
      gam_diamonds,
      # For detailed options for x_cols, see examples at resolve_x_cols()
      x_cols = ~ carat + cut + clarity + carat:clarity + color:depth_pct,
      output_boot_data = TRUE,
      boot_it = 10 # just for demonstration
    )
  }
)
# saveRDS(ale_diamonds_with_boot_data, file.choose())

# See ?get.ALE for details on the various kinds of data that may be retrieved.
get(ale_diamonds_with_boot_data, ~ carat + color:depth_pct) # default ALE data
get(ale_diamonds_with_boot_data, what = 'boot_data') # raw bootstrap data
get(ale_diamonds_with_boot_data, stats = 'estimate') # summary statistics
get(ale_diamonds_with_boot_data, stats = c('aled', 'naled'))
get(ale_diamonds_with_boot_data, stats = 'all')
get(ale_diamonds_with_boot_data, stats = 'conf_regions')
get(ale_diamonds_with_boot_data, stats = 'conf_sig')
```

ALEpDist

Random variable distributions of ALE statistics for generating p-values

Description

ALE statistics are accompanied with two indicators of the confidence of their values. First, bootstrapping creates confidence intervals for ALE effects and ALE statistics to give a range of the possible ALE values. Second, we calculate p-values, an indicator of the probability that a given ALE statistic is random. An ALEpDist S7 object contains the necessary distribution data for generating such p-values.

Usage

```
ALEpDist(
  model,
  data = NULL,
  ...,
  y_col = NULL,
```

```

    rand_it = NULL,
    surrogate = FALSE,
    parallel = "all",
    model_packages = NULL,
    random_model_call_string = NULL,
    random_model_call_string_vars = character(),
    positive = TRUE,
    pred_fun = function(object, newdata, type = pred_type) {
      stats::predict(object =
        object, newdata = newdata, type = type)
    },
    pred_type = "response",
    output_residuals = FALSE,
    seed = 0,
    silent = FALSE,
    .skip_validation = FALSE
  )

```

Arguments

model	See documentation for ALE()
data	See documentation for ALE()
...	not used. Inserted to require explicit naming of subsequent arguments.
y_col	See documentation for ALE()
rand_it	non-negative integer(1). Number of times that the model should be retrained with a new random variable. The default of NULL will generate 1000 iterations, which should give reasonably stable p-values; these are considered "exact" p-values. It can be reduced for approximate ("approx") p-values as low as 100 for faster test runs but then the p-values are not as stable. rand_it below 100 is not allowed as such p-values are inaccurate.
surrogate	logical(1). Create p-value distributions based on a surrogate linear model (TRUE) instead of on the original model (default FALSE). Note that while faster surrogate p-values are convenient for interactive analysis, they are not acceptable for definitive conclusions or publication. See details.
parallel	See documentation for ALE() . Note that for exact p-values, by default 1000 random variables are trained. So, even with parallel processing, the procedure is very slow.
model_packages	See documentation for ALE()
random_model_call_string	character(1). If NULL, the ALEpDist() constructor tries to automatically detect and construct the call for p-values. If it cannot, the constructor will fail. In that case, a character string of the full call for the model must be provided that includes the random variable. See details.
random_model_call_string_vars	See documentation for model_call_string_vars in ModelBoot() ; their operation is very similar.

positive See documentation for [ModelBoot\(\)](#)
pred_fun, pred_type See documentation for [ALE\(\)](#)
output_residuals logical(1). If TRUE, returns the residuals in addition to the raw data of the generated random statistics (which are always returned). The default FALSE does not return the residuals.
seed See documentation for [ALE\(\)](#)
silent See documentation for [ALE\(\)](#)
.skip_validation Internal use only. logical(1). Skip non-mutating data validation checks. Changing the default FALSE risks crashing with incomprehensible error messages.

Value

An object of class ALEpDist with properties `rand_stats`, `residual_distribution`, `residuals`, and `params`.

Properties

rand_stats A named list of tibbles. There is normally one element whose name is the same as `y_col` except if `y_col` is a categorical variable; in that case, the elements are named for each category of `y_col`. Each element is a tibble whose rows are each of the `rand_it_ok` iterations of the random variable analysis and whose columns are the ALE statistics obtained for each random variable.

residual_distribution A `univariateML` object with the closest estimated distribution for the residuals as determined by `univariateML::model_select()`. This is the distribution used to generate all the random variables.

residuals If `output_residuals == TRUE`, returns a matrix of the actual `y_col` values from data minus the predicted values from the model (without random variables) on the data. The rows correspond to each row of data. The columns correspond to the named elements (`y_col` or categories) described above for `rand_stats`. NULL if `output_residuals == FALSE` (default).

params Parameters used to generate p-value distributions. Most of these repeat selected arguments passed to `ALEpDist()`. These are either values provided by the user or used by default if the user did not change them but the following additional or modified objects are notable:

- * ``model``: selected elements that describe the ``model`` used to generate the random distributions.
- * ``rand_it``: the number of random iterations requested by the user either explicitly (by specifying
- * ``rand_it_ok``: A whole number with the number of ``rand_it`` iterations that successfully generated.
- * ``exactness``: A string. For regular p-values generated from the original model, ``exact`` if ``rand`
- * ``probs_inverted``: ``TRUE`` if the original probability values of the ``ALEpDist`` object have been in

Exact p-values for ALE statistics

Because ALE is non-parametric (that is, it does not assume any particular distribution of data), the `{ale}` package takes a literal frequentist approach to the calculation of empirical (Monte Carlo)

p-values. That is, it literally retrains the model 1000 times, each time modifying it by adding a distinct random variable to the model. (The number of iterations is customizable with the `rand_it` argument.) The ALEs and ALE statistics are calculated for each random variable. The percentiles of the distribution of these random-variable ALEs are then used to determine p-values for non-random variables. Thus, p-values are interpreted as the frequency of random variable ALE statistics that exceed the value of ALE statistic of the actual variable in question. The specific steps are as follows:

- The residuals of the original model trained on the training data are calculated (residuals are the actual y target value minus the predicted values).
- The closest distribution of the residuals is detected with `univariateML::model_select()`.
- 1000 new models are trained by generating a random variable each time with `univariateML::rml()` and then training a new model with that random variable added.
- The ALEs and ALE statistics are calculated for each random variable.
- For each ALE statistic, the empirical cumulative distribution function (`stats::ecdf()`) is used to create a function to determine p-values according to the distribution of the random variables' ALE statistics.

Because the `ale` package is model-agnostic (that is, it works with any kind of R model), the `ALEpDist()` constructor cannot always automatically manipulate the model object to create the p-values. It can only do so for models that follow the standard R statistical modelling conventions, which includes almost all base R algorithms (like `stats::lm()` and `stats::glm()`) and many widely used statistics packages (like `mgcv` and `survival`), but which excludes most machine learning algorithms (like `tidymodels` and `caret`). For non-standard algorithms, the user needs to do a little work to help the `ALEpDist()` constructor correctly manipulate its model object:

- The full model call must be passed as a character string in the argument `random_model_call_string`, with two slight modifications as follows.
- In the formula that specifies the model, you must add a variable named `'random_variable'`. This corresponds to the random variables that the constructor will use to estimate p-values.
- The dataset on which the model is trained must be named `'rand_data'`. This corresponds to the modified datasets that will be used to train the random variables.

See the example below for how this is implemented.

If the model generation is unstable (because of a small dataset size or a finicky model algorithm), then one or more iterations might fail, possibly dropping the number of successful iterations to below 1000. Then the p-values are only considered approximate; they are no longer exact. If that is the case, then request `rand_it` at a sufficiently high number such that even if some iterations fail, at least 1000 will succeed. For example, for an `ALEpDist` object named `p_dist`, if `p_dist@params$rand_it_ok` is 950, you could rerun `ALEpDist()` with `rand_it = 1100` or higher to allow for up to 100 possible failures.

Faster approximate and surrogate p-values

The procedure we have just described requires at least 1000 random iterations for p-values to be considered **"exact"**. Unfortunately, this procedure is rather slow—it takes at least 1000 times as long as the time it takes to train the model once.

With fewer iterations (at least 100), p-values can only be considered **approximate** ("approx"). Fewer than 100 such p-values are invalid. There might be fewer iterations either because the user requests them with the `rand_it` argument or because some iterations fail for whatever reason. As long as at least 1000 iterations succeed, p-values will be considered exact.

Because the procedure can be very slow, a faster version of the algorithm generates **"surrogate"** p-values by substituting the original model with a linear model that predicts the same `y_col` outcome from all the other columns in data. By default, these surrogate p-values use only 100 iterations and if the dataset is large, the surrogate model samples 1000 rows. Thus, the surrogate p-values can be generated much faster than for slower model algorithms on larger datasets. Although they are suitable for model development and analysis because they are faster to generate, they are less reliable than approximate p-values based on the original model. In any case, **definitive conclusions (e.g., for publication) always require exact p-values with at least 1000 iterations on the original model**. Note that surrogate p-values are always marked as "surrogate"; even if they are generated based on over 1000 iterations, they can never be considered exact because they are not based on the original model.

References

Okoli, Chitu. 2023. "Statistical Inference Using Machine Learning and Classical Techniques Based on Accumulated Local Effects (ALE)." arXiv. doi:10.48550/arXiv.2310.09877.

Examples

```
library(dplyr)

# Load diamonds dataset with some cleanup
diamonds <- ggplot2::diamonds |>
  filter(!(x == 0 | y == 0 | z == 0)) |>
  # https://lorentzen.ch/index.php/2021/04/16/a-curious-fact-on-the-diamonds-dataset/
  distinct(
    price, carat, cut, color, clarity,
    .keep_all = TRUE
  ) |>
  rename(
    x_length = x,
    y_width = y,
    z_depth = z,
    depth_pct = depth
  )

# Create a GAM model with flexible curves to predict diamond price
# Smooth all numeric variables and include all other variables
# Build the model on training data, not on the full dataset.
gam_diamonds <- mgcv::gam(
  price ~ s(carat) + s(depth_pct) + s(table) + s(x_length) + s(y_width) + s(z_depth) +
    cut + color + clarity,
  data = diamonds
)
summary(gam_diamonds)
```

```

# For speed, these examples use retrieve_rds() to load pre-created objects
# from an online repository.
# To run the code yourself, execute the code blocks directly.
serialized_objects_site <- "https://github.com/tripartio/ale/raw/main/download"

# Generating p_value distribution objects is slow because it retrains the model 100 times,
# so this example loads a pre-created ALEpDist object.
p_dist_gam_diamonds <- retrieve_rds(
  c(serialized_objects_site, 'p_dist_gam_diamonds_readme.0.5.2.rds'),
  {
    # To run the code yourself, execute this code block directly.
    ALEpDist(
      gam_diamonds, diamonds,
      # Normally should be default 1000, but just 100 for quicker demo
      rand_it = 100
    )
  }
)

# Examine the structure of the returned object
print(p_dist_gam_diamonds)

# Calculate ALEs with p-values
ale_gam_diamonds <- retrieve_rds(
  # For speed, load a pre-created object by default.
  c(serialized_objects_site, 'ale_gam_diamonds_stats_readme.0.5.2.rds'),
  {
    # To run the code yourself, execute this code block directly.
    ALE(
      gam_diamonds,
      # generate ALE for all 1D variables and the carat:clarity 2D interaction,
      x_cols = list(d1 = TRUE, d2 = 'carat:clarity'),
      data = diamonds,
      p_values = p_dist_gam_diamonds,
      # Usually at least 100 bootstrap iterations, but just 10 here for a faster demo
      boot_it = 10
    )
  }
)

# Plot the ALE data. The horizontal bands in the plots use the p-values.
plot(ale_gam_diamonds)

# For non-standard models that give errors with the default settings,
# you can use 'random_model_call_string' to specify a model for the estimation
# of p-values from random variables as in this example.
# See details above for an explanation.

pd_diamonds_non_standard <- retrieve_rds(
  # For speed, load a pre-created object by default.
  c(serialized_objects_site, 'pd_diamonds_non_standard.0.5.2.rds'),

```

```

{
  # To run the code yourself, execute this code block directly.
  ALEpDist(
    gam_diamonds,
    diamonds,
    random_model_call_string = 'mgcv::gam(
      price ~ s(carat) + s(depth_pct) + s(table) + s(x_length) + s(y_width) + s(z_depth) +
        cut + color + clarity + random_variable,
      data = rand_data
    )',
    # Normally should be default 1000, but just 100 for quicker demo
    rand_it = 100
  )
}
)
# saveRDS(pd_diamonds_non_standard, file.choose())

# Examine the structure of the returned object
print(pd_diamonds_non_standard)

```

ALEPlots

ALE plots with print and plot methods

Description

An ALEPlots S7 object contains the ALE plots from ALE or ModelBoot objects stored as ggplot objects. The ALEPlots constructor creates all possible plots from the ALE or ModelBoot passed to it—not only individual 1D and 2D ALE plots, but also special plots like the ALE effects plot. So, an ALEPlots object is a collection of plots, almost never a single plot. To retrieve specific plots, use the `get.ALEPlots()` method. See the examples with the `ALE()` and `ModelBoot()` objects for how to manipulate ALEPlots objects.

Usage

```

ALEPlots(
  obj,
  ...,
  ale_centre = "median",
  y_1d_refs = c("25%", "75%"),
  rug_sample_size = obj@params$sample_size,
  min_rug_per_interval = 1,
  y_nonsig_band = 0.05,
  seed = 0,
  silent = FALSE
)

```

Arguments

<code>obj</code>	ALE or ModelBoot object. The object containing ALE data to be plotted.
<code>...</code>	not used. Inserted to require explicit naming of subsequent arguments.
<code>ale_centre</code>	character(1) in <code>c('median', 'mean', 'zero')</code> . The ALE y values in the plots will be centred relative to this value. 'median' is the default. 'zero' will maintain the actual ALE values, which are centred on zero.
<code>y_1d_refs</code>	character or numeric vector. For 1D ALE plots, the y outcome values for which a reference line should be drawn. If a character vector, <code>y_1d_refs</code> values are names from <code>obj@params\$y_summary</code> (usually quantile names). If a numeric vector, <code>y_1d_refs</code> values must be values within the range of y, that is, between <code>obj@params\$y_summary\$min</code> and <code>obj@params\$y_summary\$max</code> inclusive.
<code>rug_sample_size, min_rug_per_interval</code>	non-negative integer(1). Rug plots are down-sampled to <code>rug_sample_size</code> rows, otherwise they can be very slow for large datasets. By default, their size is the value of <code>obj@params\$sample_size</code> . They maintain representativeness of the data by guaranteeing that each of the ALE bins will retain at least <code>min_rug_per_interval</code> elements; usually set to just 1 (default) or 2. To prevent this down-sampling, set <code>rug_sample_size</code> to <code>Inf</code> (but then the ALEPlots object would store the entire dataset, so could become very large).
<code>y_nonsig_band</code>	numeric(1) from 0 to 1. If there are no p-values, some plots (notably the 1D effects plot) will shade grey the inner <code>y_nonsig_band</code> quantile below and above the <code>ale_centre</code> average (the median, by default) to indicate nonsignificant effects.
<code>seed</code>	See documentation for ALE()
<code>silent</code>	See documentation for ALE()

Value

An object of class ALEPlots with properties `plots` and `params`.

Properties

plots Stores the ALE plots. Use [get.ALEPlots\(\)](#) to access them.

params The parameters used to calculate the ALE plots. These include most of the arguments used to construct the ALEPlots object. These are either the values provided by the user or used by default if the user did not change them but also includes several objects that are created within the constructor. These extra objects are described here, as well as those parameters that are stored differently from the form in the arguments:

* ``y_col``, ``y_cats``: See documentation for [\[ALE\(\)\]](#)

* ``max_d``: See documentation for [\[ALE\(\)\]](#)

* ``requested_x_cols``: See documentation for [\[ALE\(\)\]](#). Note, however, that ``ALEPlots`` does not store

Examples

```
# See examples with ALE() and ModelBoot() objects.
```

census

*Census Income***Description**

Census data that indicates, among other details, if the respondent's income exceeds \$50,000 per year. Also known as "Adult" dataset.

Usage

census

Format

A tibble with 32,561 rows and 15 columns:

higher_income TRUE if income > \$50,000

age continuous

workclass Private, Self-emp-not-inc, Self-emp-inc, Federal-gov, Local-gov, State-gov, Without-pay, Never-worked

fnlwgt continuous. "A proxy for the demographic background of the people: 'People with similar demographic characteristics should have similar weights'" For more details, see <https://www.openml.org/search?type=d>

education Bachelors, Some-college, 11th, HS-grad, Prof-school, Assoc-acdm, Assoc-voc, 9th, 7th-8th, 12th, Masters, 1st-4th, 10th, Doctorate, 5th-6th, Preschool

education_num continuous

marital_status Married-civ-spouse, Divorced, Never-married, Separated, Widowed, Married-spouse-absent, Married-AF-spouse

occupation Tech-support, Craft-repair, Other-service, Sales, Exec-managerial, Prof-specialty, Handlers-cleaners, Machine-op-inspct, Adm-clerical, Farming-fishing, Transport-moving, Priv-house-serv, Protective-serv, Armed-Forces

relationship Wife, Own-child, Husband, Not-in-family, Other-relative, Unmarried

race White, Asian-Pac-Islander, Amer-Indian-Eskimo, Other, Black

sex Female, Male

capital_gain continuous

capital_loss continuous

hours_per_week continuous

native_country United-States, Cambodia, England, Puerto-Rico, Canada, Germany, Outlying-US(Guam-USVI-etc), India, Japan, Greece, South, China, Cuba, Iran, Honduras, Philippines, Italy, Poland, Jamaica, Vietnam, Mexico, Portugal, Ireland, France, Dominican-Republic, Laos, Ecuador, Taiwan, Haiti, Columbia, Hungary, Guatemala, Nicaragua, Scotland, Thailand, Yugoslavia, El-Salvador, Trinidad&Tobago, Peru, Hong, Holland-Netherlands

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Source

Becker, Barry and Kohavi, Ronny. (1996). Adult. UCI Machine Learning Repository. <https://doi.org/10.24432/C5XW20>.

customize	<i>Customize plots contained in an ALEPlots object</i>
-----------	--

Description

Customize an ALEPlots object by modifying plots indicated by the combination of `x_cols`, `type`, and `cats` as specified. Some arguments indicate some common customizations such as zooming in or out; see the argument documentation for available simple options.

The most flexible option is to specify a list of ggplot layers with the `layers` argument; this appends the provided layers to each plot by applying the `ggplot2::+.gg()` method to them. Thus, any customization supported by appending ggplot layers can be applied. If both `layers` and simple options like `zoom_y` are specified, then the `layers` are applied first and then any other option is applied in the order presented in the argument list. For full control over the order of customizations, only provide `layers`.

See `get.ALE()` for explanation of parameters not described here.

Usage

```
customize(
  plots_obj,
  x_cols = NULL,
  ...,
  exclude_cols = NULL,
  type = "ale",
  cats = NULL,
  layers = NULL,
  zoom_x = NULL,
  zoom_y = NULL
)
```

Arguments

<code>plots_obj</code>	ALEPlots object to customize.
<code>x_cols</code> , <code>exclude_cols</code>	See documentation for <code>get.ALE()</code>
<code>...</code>	not used. Inserted to require explicit naming of subsequent arguments.
<code>type</code>	See documentation for <code>get.ALE()</code>
<code>cats</code>	See documentation for <code>get.ALE()</code>
<code>layers</code>	List of ggplot layers. These are appended to each plot indicated by the combination of <code>x_cols</code> , <code>type</code> , and <code>cats</code> by applying the <code>ggplot2 +</code> operator to them.
<code>zoom_x</code> , <code>zoom_y</code>	numeric(2). Zoom the specified plots in or out to match the specified x or y limits, respectively. Must be a two-element numeric vector where the first element $\leq$ the second. Default NULL does not zoom.

Value

An ALEPlots object where elements specified by `x_cols` and `exclude_cols` are modified accordingly. Non-specified elements are not modified.

get	<i>S7 generic get method for objects in the ale package</i>
-----	---

Description

Retrieve specific data elements from an object based on their X column names.

If `obj` is not an object from the `ale` package, then this generic passes on all arguments to the `base::get()` function.

Usage

```
get(obj, ...)
```

Arguments

<code>obj</code>	object.
<code>...</code>	For <code>ale</code> package objects, instructions for which predictor (x) columns should be retrieved. For everything else, arguments to pass to <code>base::get()</code> .

get.ALE	<i>get method for ALE objects</i>
---------	-----------------------------------

Description

Retrieve specific elements from an ALE object.

Arguments

<code>obj</code>	ALE object from which to retrieve elements.
<code>x_cols, exclude_cols</code>	character, list, or formula. Columns names and interaction terms from <code>obj</code> requested in one of the special <code>x_cols</code> formats. The default value of <code>NULL</code> for <code>x_cols</code> retrieves all available data of the output requested in <code>what</code> . See details in the documentation for <code>resolve_x_cols()</code> .
<code>what</code>	character(1). What kind of output is requested. Must be either "ale" (default) or "boot_data". To retrieve ALE statistics, see the <code>stats</code> argument.
<code>...</code>	not used. Inserted to require explicit naming of subsequent arguments.

stats	character(1). Retrieve ALE statistics. If stats is specified, then what must be left at the default ("ale"). Otherwise, get() errors if stats is specified and what has some other value. See the return value details below for valid values for stats.
cats	character. Optional category names to retrieve if the ALE is for a categorical y outcome model.
ale_centre	Same as in documentation for ALEPlots()
simplify	logical(1). If TRUE (default), the results will be simplified to the simplest list structure possible to give the requested results. If FALSE, a complex but consistent list structure will be returned; this might be preferred for programmatic and non-interactive use.
silent	See documentation for resolve_x_cols()

Value

Regardless of the requested data, all [get.ALE\(\)](#) have a common structure:

- If more than one category of the y outcome is returned, then the top level is a list named by each category. If, however, the y outcome is not categorical or only one category of multiple possibilities is specified using the cats argument, then the top level never has categories, regardless of the value of simplify.
- The next level (or top level if there are zero or one category) is a list with one or two levels:
 - d1: 1D ALE elements.
 - d2: 2D ALE elements. However, if elements of only one dimension (either 1D or 2D) are requested and simplify = TRUE (default), the empty list is eliminated and the level is skipped to provide only the elements present. For example, if only 1D ALE data is requested, then there will be no d1 sublist but only a list of the ALE data as described for the next level. If simplify = FALSE, both d1 and d2 sublists will always be returned; the empty sublist will be NULL.

While all results follow the general structure just described, the specific type of data returned depends on the values of the what and stats arguments:

what = 'ale' (default) and stats = NULL (default) A list whose elements, named by each requested x variable, are each a tibble. The rows each represent one ALE bin. The tibble has the following columns: * var.bin or var.ceil where var is the name of a variable (column): For non-numeric x, var.bin is the value of each of the ALE categories. For numeric x, var.ceil is the value of the upper bound (ceiling) of each ALE bin. The first "bin" of numeric variables represents the minimum value. For 2D ALE with an var1 by var2 interaction, both var1.bin and var2.bin columns are returned (or var1.ceil or var2.ceil for numeric var1 or var2). * .n: the number of rows of data in each bin represented by var.bin or var.ceil. For numeric x, the first bin contains all data elements that have exactly the minimum value of x. This is often 1, but might be more than 1 if more than one data element has exactly the minimum value. * .y: the ALE function value calculated for that bin. For bootstrapped ALE, this is the same as .y_mean by default or .y_median if boot_centre = 'median'. Regardless, both .y_mean and .y_median are returned as columns here. * .y_lo, .y_hi: the lower and upper confidence intervals, respectively, for the bootstrapped .y value based on the boot_alpha argument in the [ALE\(\)](#) constructor.

what = 'boot_data' and stats = NULL (default) A list whose elements, named by each requested x variable, are each a tibble. These are the data from which .y_mean, .y_median, .y_lo, and .y_hi are summarized when what = 'ale'. The rows each represent one ALE bin for a specified bootstrap iteration. The tibble has the following columns: * .it: The bootstrap iteration. Iteration 0 represents the ALE calculations on the full dataset; the remaining values of .it are from 1 to boot_it (number of bootstrap iterations specified in the ALE() constructor. * var where var is the name of a variable (column): For non-numeric x, var is the value of each of the ALE categories. For numeric x, var is the value of the upper bound (ceiling) of each ALE bin. They are otherwise similar to their meanings described for what = 'ale' above. * .n and .y: Same as for what = 'ale'.

what = 'ale' (default) and stats = 'estimate' A list with elements d1 and d2 with the value of each ALE statistic. Each row represents one variable or interaction. The tibble has the following columns: * term: The variables or columns for the 1D or 2D ALE statistic. * aled, aler_min, aler_max, naled, naler_min, naler_max: the respective ALE statistic for the variable or interaction.

what = 'ale' (default) and stats is one or more values in c('aled', 'aler_min', 'aler_max', 'naled', 'naler_min') A list with elements d1 and d2 with the distribution value of the single requested ALE statistic. Each element d1 and d2 is a tibble. Each row represents one statistic for one variable or interaction. The tibble has the following columns: * term: Same as for stats = 'estimate'. * statistic: The requested ALE statistic(s). * estimate, mean, median: The average of the bootstrapped value of the requested statistic. estimate is equal to either mean or median depending on the boot_centre argument in the ALE() constructor. If ALE is not bootstrapped, then estimate, mean, and median are equal. * conf.low, conf.high: the lower and upper confidence intervals, respectively, for the bootstrapped statistic based on the boot_alpha argument in the ALE() constructor. If ALE is not bootstrapped, then estimate, conf.low, and conf.high are equal.

what = 'ale' (default) and stats = 'all' A list with elements d1 and d2 with the distribution values of all available ALE statistics for the requested variables and interactions. Whereas the stats = 'aled' (for example) format returns data for a single statistic, stats = 'all' returns all statistics for the requested variables. Thus, the data structure and columns are identical as for single statistics above, except that all available ALE statistics are returned.

what = 'ale' (default) and stats = 'conf_regions' A list with elements d1 and d2 with the confidence regions for the requested variables and interactions. Each element is a list with the requested d1 and d2 sub-elements as described in the general structure above. Each data element is a tibble with confidence regions for a single variable or interaction. For an explanation of the columns, see vignette('ale-statistics').

what = 'ale' (default) and stats = 'conf_sig' Identical structure as stats = 'conf_regions' except that the elements are filtered for the terms (variables or interactions) that have statistically significant confidence regions exceeding the threshold of the inner ALER band, specifically, at least obj@params\$aler_alpha[2] of the rows of data. See vignette("ale-statistics") for details.

Examples

```
# See examples at ALE() for a demonstration of how to use the get() method.
```

get.ALEPlots	<i>get method for ALEPlots objects</i>
--------------	--

Description

Retrieve specific plots from a `ALEPlots` object. Unlike `subset.ALEPlots()` which returns an `ALEPlots` object with the subsetting `x_cols` variables and interactions, this `get.ALEPlots()` method returns a list of `ggplot2::ggplot` objects as specified in the return value description. To retain special `ALEPlots` behaviour like plotting, printing, and summarizing multiple plots, use `subset.ALEPlots()` instead.

See `get.ALE()` for explanation of parameters not described here.

Arguments

<code>obj</code>	<code>ALEPlots</code> object from which to retrieve ALE elements.
<code>type</code>	<code>character(1)</code> . What type of ALEPlots to retrieve: 'ale' for standard ALE plots or 'effect' for ALE effects plots. See <code>cats</code> argument for options for categorical plots.
<code>cats</code>	<code>character</code> . The categories (one or more) of a categorical outcome variable to retrieve. To retrieve all categories as individual category plots, leave <code>cats</code> at the default <code>NULL</code> . For categorical plots that combine all categories, specify <code>cats = ".all"</code> . (Don't forget the "." in ".all", which avoids naming conflicts with legitimate categories that might be named "all".) For such all-category plots, <code>type</code> must be set to "overlay" or "facet" for the specific desired type of categorical plot.

Value

A list of `ggplot` objects as described in the documentation for the return value of `get.ALE()`. This is different from `subset.ALEPlots()`, which returns an `ALEPlots` object with the subsetting `x_cols` variables and interactions.

get.ModelBoot	<i>get method for ModelBoot objects</i>
---------------	---

Description

Retrieve specific ALE elements from a `ModelBoot` object. This method is similar to `get.ALE()` except that the user may specify what type of ALE data to retrieve (see the argument definition for details).

See `get.ALE()` for explanation of parameters not described here.

Arguments

obj	ModelBoot object from which to retrieve ALE elements.
type	character(1). The type of ModelBoot ALE elements to retrieve: 'single' for the ALE calculated on the full data set or 'boot' for the bootstrapped ALE data (based on full-model bootstrapping). The default 'auto' will retrieve 'boot' if it is available and 'single' otherwise.

Value

See [get.ALE\(\)](#)

invert_probs	<i>Invert ALE Probabilities</i>
--------------	---------------------------------

Description

Inverts the predicted probabilities in an ALE object to reflect complementary outcomes (i.e., $1 - p$). This is particularly useful when the model probability predictions are opposite to what is desired for easy interpretability. With [invert_probs\(\)](#), there is no need to change the original data or retrain the model; the ALE data, p-values, and subsequent ALE plots will reflect the desired inverted probabilities.

Usage

```
invert_probs(ale_obj, rename_y_col = NULL, force = FALSE)
```

Arguments

ale_obj	An object of class ALE.
rename_y_col	character(1). If provided, renames the y outcome column. When probabilities are inverted, the name of the outcome column often needs to change for more intuitive interpretability. The default NULL does not change the outcome column name.
force	logical(1). If TRUE, inverts probabilities even if they have already been inverted once before (reverting them). The default FALSE will error if probabilities have already been inverted.

Details

This function inverts the ALE y-values (i.e., `.y`, `.y_mean`, `.y_median`, etc.) for all terms, including the main ALE effects, bootstrap data, and ALE statistics (`aler_min`, `aler_max`, etc.). It also updates the `y_col` name and `y_summary` column names if `rename_y_col` is provided.

If the ALE object has already been inverted (`probs_inverted = TRUE`), the function throws an error by default. To force reinversion (i.e., revert to original probabilities), set `force = TRUE`.

This operation is only permitted if the y-summary probabilities are all in the $[0, 1]$ interval.

Value

An updated ALE object with all probabilities and relevant statistics inverted.

Examples

```
# Binary model
setosa <- iris |>
  dplyr::mutate(setosa = Species == "setosa") |>
  dplyr::select(~Species)

ale_obj <- glm(setosa ~ ., data = setosa, family = binomial()) |>
  ALE()

# Invert the predicted probabilities
ale_inverted <- invert_probs(ale_obj)

# Revert back to original by inverting again
ale_reverted <- invert_probs(ale_inverted, force = TRUE)
```

ModelBoot

Statistics and ALE data for a bootstrapped model

Description

A ModelBoot S7 object contains full-model bootstrapped statistics and ALE data for a trained model. Full-model bootstrapping (as distinct from data-only bootstrapping) retrains a model for each bootstrap iteration. Thus, it can be rather slow, though it is much more reliable. However, for obtaining bootstrapped ALE data, plots, and statistics, full-model bootstrapping as provided by ModelBoot is only necessary for models that have not been developed by cross-validation. For cross-validated models, it is sufficient (and much faster) to create a regular [ALE()] object with bootstrapping by setting the `boot_it` argument in its constructor. In fact, full-model bootstrapping with ModelBoot is often infeasible for slow machine-learning models trained on large datasets, which should rather be cross-validated to assure their reliability. However, for models that have not been cross-validated, full-model bootstrapping with ModelBoot is necessary for reliable results. Further details follow below; see also `vignette('ale-statistics')`.

Usage

```
ModelBoot(
  model,
  data = NULL,
  ...,
  model_call_string = NULL,
  model_call_string_vars = character(),
  parallel = "all",
```

```

model_packages = NULL,
y_col = NULL,
positive = TRUE,
pred_fun = function(object, newdata, type = pred_type) {
  stats::predict(object =
    object, newdata = newdata, type = type)
},
pred_type = "response",
boot_it = 100,
boot_alpha = 0.05,
boot_centre = "mean",
seed = 0,
output_model_stats = TRUE,
output_model_coefs = TRUE,
output_ale = TRUE,
output_boot_data = FALSE,
ale_options = list(),
ale_p = "auto",
tidy_options = list(),
glance_options = list(),
silent = FALSE
)

```

Arguments

<code>model</code>	Required. See documentation for ALE()
<code>data</code>	dataframe. Dataset to be bootstrapped. This must be the same data on which the model was trained. If not provided, <code>ModelBoot()</code> will try to detect it automatically. For non-standard models, data should be provided.
<code>...</code>	not used. Inserted to require explicit naming of subsequent arguments.
<code>model_call_string</code>	character(1). If NULL (default), the <code>ModelBoot</code> tries to automatically detect and construct the call for bootstrapped datasets. If it cannot, the function will fail early. In that case, a character string of the full call for the model must be provided that includes <code>boot_data</code> as the data argument for the call. See examples.
<code>model_call_string_vars</code>	character. Names of variables included in <code>model_call_string</code> that are not columns in data. If any such variables exist, they must be specified here or else parallel processing may produce an error. If parallelization is disabled with <code>parallel = 0</code> , then this is not a concern. See documentation for the <code>model_packages</code> argument in ALE() .
<code>parallel, model_packages</code>	See documentation for ALE()
<code>y_col, pred_fun, pred_type</code>	See documentation for ALE() . Used to calculate bootstrapped performance measures. If left at their default values, then the relevant performance measures are calculated only if these arguments can be automatically detected. Otherwise, they should be specified.

positive	any single atomic value. If the model represented by <code>model</code> or <code>model_call_string</code> is a binary classification model, <code>positive</code> specifies the 'positive' value of <code>y_col</code> (the target outcome), that is, the value of interest that is considered TRUE; any other value of <code>y_col</code> is considered FALSE. This argument is ignored if the model is not a binary classification model. For example, if 2 means TRUE and 1 means FALSE, then set <code>positive = 2</code> .
boot_it	non-negative integer(1). Number of bootstrap iterations for full-model bootstrapping. For bootstrapping of ALE values, see details to verify if ALE() with bootstrapping is not more appropriate than ModelBoot() . If <code>boot_it = 0</code> , then the model is run as normal once on the full data with no bootstrapping.
boot_alpha	numeric(1) from 0 to 1. Alpha for percentile-based confidence interval range for the bootstrap intervals; the bootstrap confidence intervals will be the lowest and highest $(1 - 0.05) / 2$ percentiles. For example, if <code>boot_alpha = 0.05</code> (default), the intervals will be from the 2.5 and 97.5 percentiles.
boot_centre	character(1) in <code>c('mean', 'median')</code> . When bootstrapping, the main estimate for the ALE y value is considered to be <code>boot_centre</code> . Regardless of the value specified here, both the mean and median will be available.
seed	integer. Random seed. Supply this between runs to assure identical bootstrap samples are generated each time on the same data. See documentation for ALE() for further details.
output_model_stats	logical(1). If TRUE (default), return overall model statistics using broom::glance() (if available for <code>model</code>) and bootstrap-validated statistics if <code>boot_it > 0</code> .
output_model_coefs	logical(1). If TRUE (default), return model coefficients using broom::tidy() (if available for <code>model</code>).
output_ale	logical(1). If TRUE (default), return ALE data and statistics.
output_boot_data	logical(1). If TRUE, return the full raw data for each bootstrap iteration, specifically, the bootstrapped models and the model row indices. Default FALSE does not return this large, detailed data.
ale_options, tidy_options, glance_options	list of named arguments. Arguments to pass to the ALE() constructor when <code>ale = TRUE</code> , broom::tidy() when <code>model_coefs = TRUE</code> , or broom::glance() when <code>model_stats = TRUE</code> , respectively, beyond (or overriding) their defaults. Note: to obtain p-values for ALE statistics, see the <code>ale_p</code> argument.
ale_p	Same as the <code>p_values</code> argument for the ALE() constructor; see documentation there. This argument overrides the <code>p_values</code> element of the <code>ale_options</code> argument.
silent	See documentation for ALE()

Value

An object of class ALE with properties `model_stats`, `model_coefs`, `ale`, `model_stats`, `boot_data`, and `params`.

Properties

model_stats tibble of bootstrapped results from `broom::glance()`. NULL if `model_stats` argument is FALSE. In general, only `broom::glance()` results that make sense when bootstrapped are included, such as `df` and `adj.r.squared`. Results that are incomparable across bootstrapped datasets (such as `aic`) are excluded. In addition, certain model performance measures are included; these are bootstrap-validated with the .632 correction (Efron & Tibshirani 1986) (NOT the .632+ correction):

- For regression (numeric prediction) models:
 - `mae`: mean absolute error (MAE)
 - `sa_mae`: standardized accuracy of the MAE referenced on the mean absolute deviation
 - `rmse`: root mean squared error (RMSE)
 - `sa_rmse`: standardized accuracy of the RMSE referenced on the standard deviation
- For binary or categorical classification (probability) models:
 - `auc`: area under the ROC curve

model_coefs A tibble of bootstrapped results from `broom::tidy()`. NULL if `model_coefs` argument is FALSE.

ale A list of bootstrapped ALE results using default `ALE()` settings unless if overridden with `ale_options`. NULL if `ale` argument is FALSE. Elements are:

- * ``single``: an ``ALE`` object of ALE calculations on the full dataset without bootstrapping.
- * ``boot``: a list of bootstrapped ALE data and statistics. This element is not an ``ALE`` object; it u

boot_data A tibble of bootstrap results. Each row represents a bootstrap iteration. NULL if `boot_data` argument is FALSE. The columns are:

- * ``it``: the specific bootstrap iteration from 0 to ``boot_it`` iterations. Iteration 0 is the result.
- * ``row_idx``: the row indexes for the bootstrapped sample for that iteration. To save space, the r
- * ``model``: the model object trained on that iteration.
- * ``ale``: the results of ``ALE()`` on that iteration.
- * ``tidy``: the results of ``broom::tidy(model)`` on that iteration.
- * ``stats``: the results of ``broom::glance(model)`` on that iteration.
- * ``perf``: performance measures on the entire dataset. These are the measures specified above for r

params Parameters used to calculate bootstrapped data. Most of these repeat the arguments passed to `ModelBoot()`. These are either the values provided by the user or used by default if the user did not change them but the following additional objects created internally are also provided:

- * ``y_cats``: same as ``ALE@params$y_cats`` (see documentation there).
- * ``y_type``: same as ``ALE@params$y_type`` (see documentation there).
- * ``model``: same as ``ALE@params$model`` (see documentation there).
- * ``data``: same as ``ALE@params$data`` (see documentation there).

Full-model bootstrapping

No modelling results, with or without ALE, should be considered reliable without appropriate validation. For ALE, both the trained model itself and the ALE that explains the trained model must

be validated. ALE must be validated by bootstrapping. The trained model might be validated either by cross-validation or by bootstrapping. For ALE that explains trained models that have been developed by cross-validation, it is sufficient to bootstrap just the training data. That is what the ALE object does with its `boot_it` argument. However, unvalidated models must be validated by bootstrapping them along with the calculation of ALE; this is what the ModelBoot object does with its `boot_it` argument.

`ModelBoot()` carries out full-model bootstrapping to validate models. Specifically, it:

- Creates multiple bootstrap samples (default 100; the user can specify any number);
- Creates a model on each bootstrap sample;
- Calculates overall model statistics, variable coefficients, and ALE values for each model on each bootstrap sample;
- Calculates the mean, median, and lower and upper confidence intervals for each of those values across all bootstrap samples.

References

Okoli, Chitu. 2023. "Statistical Inference Using Machine Learning and Classical Techniques Based on Accumulated Local Effects (ALE)." arXiv. doi:10.48550/arXiv.2310.09877.<

Efron, Bradley, and Robert Tibshirani. "Bootstrap methods for standard errors, confidence intervals, and other measures of statistical accuracy." Statistical science (1986): 54-75. doi:10.1214/ss/1177013815

Examples

```
# attitude dataset
attitude

## ALE for generalized additive models (GAM)
## GAM is tweaked to work on the small dataset.
gam_attitude <- mgcv::gam(rating ~ complaints + privileges + s(learning) +
                        raises + s(critical) + advance,
                        data = attitude)

summary(gam_attitude)

# Full model bootstrapping

# For speed, these examples use retrieve_rds() to load pre-created objects
# from an online repository.
# To run the code yourself, execute the code blocks directly.
serialized_objects_site <- "https://github.com/tripartio/ale/raw/main/download"

# Create ALE data
mb_gam_attitude <- retrieve_rds(
  # For speed, load a pre-created object by default.
  c(serialized_objects_site, 'mb_gam_attitude.0.5.2.rds'),
  {
    # To run the code yourself, execute this code block directly.
```

```

# For standard models like lm that store their data,
# there is no need to specify the data argument.
# 100 bootstrap iterations by default.
ModelBoot(gam_attitude)
}
)

## If the model is not standard, supply model_call_string with 'data = boot_data'
## in the string instead of the actual dataset name (in addition to the actual dataset
## as the 'data' argument directly to the `ModelBoot` constructor).
# mb_gam_attitude <- ModelBoot(
#   gam_attitude,
#   data = attitude, # the actual dataset
#   model_call_string = 'mgcv::gam(
#     rating ~ complaints + privileges + s(learning) +
#     raises + s(critical) + advance,
#     data = boot_data # required for model_call_string
#   )'
# )

# Model statistics and coefficients
mb_gam_attitude@model_stats
mb_gam_attitude@model_coefs

# Plot ALE
plot(mb_gam_attitude)

# Retrieve ALE data
get(mb_gam_attitude, type = 'boot') # bootstrapped
get(mb_gam_attitude, type = 'single') # full (unbootstrapped) model
# See get.ALE() for other options

```

plot.ALE

plot method for ALE objects

Description

This plot method simply calls the constructor for an ALEPlots object.

Arguments

x	ALE object.
...	Arguments passed to ALEPlots()

plot.ALEPlots	<i>Plot method for ALEPlots object</i>
---------------	--

Description

Plot an ALEPlots object.

Arguments

x	An object of class ALEPlots.
max_print	integer(1). The maximum number of plots that may be printed at a time. 1D plots and 2D are printed on separate pages, so this maximum applies separately to each dimension of ALE plots, not to all dimensions combined.
...	Arguments to pass to patchwork::wrap_plots()

Value

Invisibly returns x.

plot.ModelBoot	<i>plot method for ModelBoot objects</i>
----------------	--

Description

This plot method simply calls the constructor for an ALEPlots object.

Arguments

x	ModelBoot object.
...	Arguments passed to ALEPlots()

print.ALE	<i>print Method for ALE object</i>
-----------	------------------------------------

Description

Print an ALE object.

Arguments

x	An object of class ALE.
...	Additional arguments (currently not used).

Value

Invisibly returns x.

Examples

```
lm_cars <- stats::lm(mpg ~ ., mtcars)
ale_cars <- ALE(lm_cars, p_values = NULL)
print(ale_cars)
```

print.ALEPlots	<i>Print method for ALEPlots object</i>
----------------	---

Description

Print an ALEPlots object by calling plot().

Arguments

x	An object of class ALEPlots.
max_print	See documentation for plot.ALEPlots()
...	Additional arguments (currently not used).

Value

Invisibly returns x.

print.ModelBoot	<i>print method for ModelBoot object</i>
-----------------	--

Description

Print a ModelBoot object.

Arguments

x	An object of class ModelBoot.
...	Additional arguments (currently not used).

Value

Invisibly returns x.

Examples

```
lm_cars <- stats::lm(mpg ~ wt + gear, mtcars)
mb <- ModelBoot(lm_cars, boot_it = 2, ale_p = NULL)
print(mb)
```

resolve_x_cols	<i>Resolve x_cols and exclude_cols to their standardized format</i>
----------------	---

Description

Resolve x_cols and exclude_cols to their standardized format of x_cols to specify which 1D and 2D ALE elements are required. This specification is used throughout the ALE package. x_cols specifies the desired columns or interactions whereas exclude_cols optionally specifies any columns or interactions to remove from x_cols. The result is x_cols – exclude_cols, giving considerable flexibility in specifying the precise columns desired.

Usage

```
resolve_x_cols(x_cols, col_names, y_col, exclude_cols = NULL, silent = FALSE)
```

Arguments

<code>x_cols</code>	character, list, or formula. Columns and interactions requested in one of the special <code>x_cols</code> formats. <code>x_cols</code> variable names not found in <code>col_names</code> will error. See examples.
<code>col_names</code>	character. All the column names from a dataset. All values in <code>x_cols</code> must be contained among the values in <code>col_names</code> . For interaction terms in <code>x_cols</code> , e.g., <code>"a:b"</code> , the individual variable names must be contained in <code>col_names</code> , e.g., <code>c("a", "b")</code> .
<code>y_col</code>	character(1). The y outcome column. If found in any <code>x_cols</code> value, it will be silently removed.
<code>exclude_cols</code>	Same possible formats as <code>x_cols</code> . Columns and interactions to exclude from those requested in <code>x_cols</code> . <code>exclude_cols</code> values not found in <code>col_names</code> will be ignored with a message (which can be silenced with <code>silent</code>).
<code>silent</code>	logical(1). If TRUE, no message will be given; in particular, <code>x_cols</code> not found in <code>col_names</code> will be silently ignored. Default is FALSE. Regardless, warnings and errors are never silenced (e.g, invalid <code>x_cols</code> formats will still report errors).

Value

`x_cols` in canonical format, which is always a list with two elements, `d1` and `d2`. Each element is a character vector with each requested column for 1D ALE (`d1`) or 2D ALE interaction pair (`d2`). If either dimension is empty, its value is an empty character, `character()`.

See examples for details.

`x_cols` format options

The `x_cols` argument determines which predictor variables and interactions are included in the analysis. It supports multiple input formats:

- **Character vector:** Users can explicitly specify 1D terms and 2D ALE interactions, e.g., `c("a", "b", "a:b", "a:c")`.
- **Formula (~):** Allows specifying variables and interactions in formula notation (e.g., `~ a + b + a:b`), which is automatically converted into a structured format. The outcome term is optional and will be ignored regardless. So, `~ a + b + a:b` produces results identical to whatever `~ a + b + a:b`.
- **List format:**
 - The basic list format is a list of character vectors named `d1` for 1D ALE terms, `d2` for 2D interactions, or both. For example, `list(d1 = c("a", "b"), d2 = c("a:b", "a:c"))`
 - **Boolean selection for an entire dimension:**
 - * `list(d1 = TRUE)` selects all available variables for 1D ALE, excluding `y_col`.
 - * `list(d2 = TRUE)` selects all possible 2D interactions among all columns in `col_names`, excluding `y_col`.
 - A character vector of 1D terms only named `d2_all` may be used to include all 2D interactions that include the specified 1D terms. For example, specifying `list(d2_all = "a")` would select `c("a:b", "a:c", "a:d")`, etc. This is in addition to any terms requested in the `d1` or `d2` elements.

- **NULL (or unspecified):** If `x_cols = NULL`, no variables are selected.

The function ensures all variables are valid and in `col_names`, providing informative messages unless `silent = TRUE`. And regardless of the specification format, the result will always be standardized in the format specified in the return value. Note that `y_col` is not removed if included in `x_cols`. However, a message alerts when it is included, in case it is a mistake.

Run examples for details.

Examples

```
## Sample data
set.seed(0)
df <- data.frame(
  y = runif(10),
  a = sample(letters[1:3], 10, replace = TRUE),
  b = rnorm(10),
  c = sample(1:5, 10, replace = TRUE)
)
col_names <- names(df)
y_col <- "y" # Assume 'y' is the outcome variable

## Examples with just x_cols to show different formats for specifying x_cols
## (same format for exclude_cols)

# Character vector: Simple ALE with no interactions
resolve_x_cols(c("a", "b"), col_names, y_col)

# Character string: Select just one 1D element
resolve_x_cols("c", col_names, y_col)

# list of 1- and 2-length character vectors: specify precise 1D and 2D elements desired
resolve_x_cols(c('a:b', "c", 'c:a', "b"), col_names, y_col)

# Formula: Converts to a list of individual elements
resolve_x_cols(~ a + b, col_names, y_col)

# Formula with interactions (1D and 2D).
# This format is probably more convenient if you know precisely which terms you want.
# Note that the outcome on the left-hand-side is always silently ignored.
resolve_x_cols(whatever ~ a + b + a:b + c:b, col_names, y_col)

# List specifying d1 (1D ALE)
resolve_x_cols(list(d1 = c("a", "b")), col_names, y_col)

# List specifying d2 (2D ALE)
resolve_x_cols(list(d2 = 'a:b'), col_names, y_col)

# List specifying both d1 and d2
resolve_x_cols(list(d1 = c("a", "b"), d2 = 'a:b'), col_names, y_col)

# d1 as TRUE (select all columns except y_col)
```

```

resolve_x_cols(list(d1 = TRUE), col_names, y_col)

# d2 as TRUE (select all possible 2D interactions)
resolve_x_cols(list(d2 = TRUE), col_names, y_col)

# d2_all: Request all 2D interactions involving a specific variable
resolve_x_cols(list(d2_all = "a"), col_names, y_col)

# NULL: No variables selected
resolve_x_cols(NULL, col_names, y_col)

## Examples of how exclude_cols are removed from x_cols to obtain various desired results

# Exclude one column from a simple character vector
resolve_x_cols(
  x_cols = c("a", "b", "c"),
  col_names = col_names,
  y_col = y_col,
  exclude_cols = "b"
)

# Exclude multiple columns
resolve_x_cols(
  x_cols = c("a", "b", "c"),
  col_names = col_names,
  y_col = y_col,
  exclude_cols = c("a", "c")
)

# Exclude an interaction term from a formula input
resolve_x_cols(
  x_cols = ~ a + b + a:b,
  col_names = col_names,
  y_col = y_col,
  exclude_cols = ~ a:b
)

# Exclude all columns from x_cols
resolve_x_cols(
  x_cols = c("a", "b", "c"),
  col_names = col_names,
  y_col = y_col,
  exclude_cols = c("a", "b", "c")
)

# Exclude non-existent columns (should be ignored)
resolve_x_cols(
  x_cols = c("a", "b"),
  col_names = col_names,
  y_col = y_col,
  exclude_cols = "z"
)

```

```

)

# Exclude one column from a list-based input
resolve_x_cols(
  x_cols = list(d1 = c("a", "b"), d2 = c("a:b", "a:c")),
  col_names = col_names,
  y_col = y_col,
  exclude_cols = list(d1 = "a")
)

# Exclude interactions only
resolve_x_cols(
  x_cols = list(d1 = c("a", "b", "c"), d2 = c("a:b", "a:c")),
  col_names = col_names,
  y_col = y_col,
  exclude_cols = list(d2 = 'a:b')
)

# Exclude everything, including interactions
resolve_x_cols(
  x_cols = list(d1 = c("a", "b", "c"), d2 = c("a:b", "a:c")),
  col_names = col_names,
  y_col = y_col,
  exclude_cols = list(d1 = c("a", "b", "c"), d2 = c("a:b", "a:c"))
)

# Exclude a column implicitly removed by y_col
resolve_x_cols(
  x_cols = c("y", "a", "b"),
  col_names = col_names,
  y_col = "y",
  exclude_cols = "a"
)

# Exclude entire 2D dimension from x_cols with d2 = TRUE
resolve_x_cols(
  x_cols = list(d1 = TRUE, d2 = c("a:b", "a:c")),
  col_names = col_names,
  y_col = y_col,
  exclude_cols = list(d1 = c("a"), d2 = TRUE)
)

```

retrieve_rds

Retrieve an R object from the first successful source among multiple attempts

Description

retrieve_rds() tries each argument in ...—in order—until one successfully yields a value, which is returned immediately. It supports two kinds of attempts:

1. **Character input interpreted as a remote RDS URL** (when `char_as_url = TRUE`, default): character vectors are collapsed with `'/'`, opened via a URL connection, and read with `readRDS()`.
2. **Arbitrary R expressions/code blocks**: captured unevaluated and then evaluated in the caller's environment; the resulting value is returned.

If an attempt fail, it tries the next listed attempt. If every attempt fails, the function aborts.

Usage

```
retrieve_rds(..., char_as_url = TRUE)
```

Arguments

- ... One or more *attempts* to obtain a value. Each attempt may be:
- a character vector representing the components of a URL to an `.rds` file (e.g., `c("https://host", "path", "file.rds")`) when `char_as_url = TRUE`; or
 - any R expression (including a `{ }` block) that, when evaluated, yields the desired value.

Attempts are tried **in order**. The first one that successfully produces a value causes an immediate return.

- `char_as_url` `logical(1)`. If `TRUE` (default), character attempts are treated as URL components: they are concatenated with `'/'`, opened via `base::url()`, and read using `base::readRDS()`. If `FALSE`, character inputs are not treated specially and will be evaluated as normal R expressions.

Details

- **Lazy capture of attempts**: Arguments in `...` are captured unevaluated using `rlang::enexprs()`, so code blocks passed in braces are not executed until `retrieve_rds()` chooses to evaluate them.
- **Evaluation environment**: Expressions are evaluated in the caller's environment via `rlang::eval_tidy()` with `env = rlang::caller_env()`, so symbols resolve exactly as if the code were written at the call site.
- **Character-as-URL behaviour** (enabled by default): the character vector is pasted with `'/'` separators (no leading/trailing slash normalization), passed to `base::url()`, then to `base::readRDS()`. Any error during this step is caught and skipped so that the next attempt can run.
- **Short-circuiting**: As soon as one attempt succeeds (either by reading an RDS over HTTP(S) or by evaluating an expression), its value is returned and no further attempts are processed.

Value

The first successfully retrieved/produced R object among the attempts in `...`. If none succeed, the function aborts.

Error handling

- URL/RDS failures are wrapped in tryCatch() and **do not** stop the procedure; the function proceeds to the next attempt.
- If all attempts fail, the function aborts.

See Also

`base::readRDS()`, `base::url()`, `rlang::enexprs()`, `rlang::eval_tidy()`, `rlang::caller_env()`, `cli::cli_abort()`

Examples

```
# Example 1: Try a remote RDS first; if it fails, run the code block.
# - With char_as_url = TRUE (default), the character vector is collapsed with "/",
#   opened as a URL, and read via readRDS().
# - If the URL works, the serialized object is returned immediately.
# - If it fails, the code block within curly quotes is evaluated in the
#   caller's environment and its value is returned (here it would assign and
#   return `ale_gam_diamonds`).
serialized_objects_site <- "https://github.com/tripartio/ale/raw/main/download"
retrieve_rds(
  c(serialized_objects_site, "ale_gam_diamonds.0.5.2.rds"),
  {
    ale_gam_diamonds <- "Code for generating an ALE object"
  }
)

# Example 2: First attempt fails as a URL, so the next expression (a literal) is returned.
# - "dodo" is treated as a URL (char_as_url = TRUE), which fails silently.
# - The next attempt (100L) is evaluated and returned.
retrieve_rds(
  "dodo",
  100L
)

# Example 3: Characters are NOT treated as URLs, so the first argument returns immediately.
# - With char_as_url = FALSE, 'dodo' is evaluated as a regular expression (a character)
#   and returned at once; later attempts are ignored.
retrieve_rds(
  'dodo',
  100L,
  char_as_url = FALSE
)
```

Description

Subset an ALEPlots object to produce another ALEPlots object only with the subsetted `x_cols` variables and interactions, as specified in the return value description.

See [get.ALE\(\)](#) for explanation of parameters not described here.

Arguments

<code>x</code>	An object of class ALEPlots.
<code>...</code>	not used. Inserted to require explicit naming of subsequent arguments.
<code>include_eff</code>	logical(1). <code>x_cols</code> and <code>exclude_cols</code> specify precisely which variables to include or exclude in the subset. However, multivariable plots like ALE effects plot are ambiguous because they cannot be subsetted to remove some existing variables. <code>include_eff = TRUE</code> (default) includes the ALE effects plot in the subset rather than dropping it, if it is available.

Value

An ALEPlots object reduced to cover only variables and interactions specified by `x_cols` and `exclude_cols`. This is different from [get.ALEPlots\(\)](#), which returns a list of ggplot objects and loses the special ALEPlots behaviour like plotting, printing, and summarizing multiple plots.

summary.ALEPlots	<i>summary method for ALEPlots object</i>
------------------	---

Description

Present concise summary information about an ALEPlots object.

Arguments

<code>object</code>	An object of class ALEPlots.
<code>...</code>	Not used

Value

Summary string.

var_cars*Multi-variable transformation of the mtcars dataset.*

Description

This is a transformation of the `mtcars` dataset from R to produce a small dataset with each of the fundamental datatypes: logical, factor, ordered, integer, double, and character. Most of the transformations are obvious, but a few are noteworthy:

- The row names (the car model) are saved as a character vector.
- For the unordered factors, the country and continent of the car manufacturer are obtained based on the row names (model).
- For the ordered factor, gears 3, 4, and 5 are encoded as 'three', 'four', and 'five', respectively. The text labels make it explicit that the variable is ordinal, yet the number names make the order crystal clear.

Here is the adaptation of the original description of the `mtcars` dataset:

The data was extracted from the 1974 *Motor Trend* US magazine, and comprises fuel consumption and 10 aspects of automobile design and performance for 32 automobiles (1973–74 models).

Usage

```
var_cars
```

Format

A tibble with 32 observations on 14 variables.

model character: Car model
mpg double: Miles/(US) gallon
cyl integer: Number of cylinders
disp double: Displacement (cu.in.)
hp double: Gross horsepower
drat double: Rear axle ratio
wt double: Weight (1000 lbs)
qsec double: 1/4 mile time
vs logical: Engine (0 = V-shaped, 1 = straight)
am logical: Transmission (0 = automatic, 1 = manual)
gear ordered: Number of forward gears
carb integer: Number of carburetors
country factor: Country of car manufacturer
continent factor: Continent of car manufacturer

Note

Henderson and Velleman (1981) comment in a footnote to Table 1: 'Hocking (original transcriber)'s noncrucial coding of the Mazda's rotary engine as a straight six-cylinder engine and the Porsche's flat engine as a V engine, as well as the inclusion of the diesel Mercedes 240D, have been retained to enable direct comparisons to be made with previous analyses.'

References

Henderson and Velleman (1981), Building multiple regression models interactively. *Biometrics*, **37**, 391–411.

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