

Package ‘SCCI’

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Type Package

Title Stochastic Complexity-Based Conditional Independence Test for Discrete Data

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Description

An efficient implementation of SCCI using 'Rcpp'. SCCI is short for the Stochastic Complexity-based Conditional Independence criterium (Marx and Vreeken, 2019). SCCI is an asymptotically unbiased and L2 consistent estimator of (conditional) mutual information for discrete data.

License GPL (>= 2)

Imports Rcpp (>= 0.12.13)

LinkingTo Rcpp

Suggests pcalg, Rgraphviz

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conditionalShannonEntropy

Conditional Shannon Entropy

Description

Calculates the Shannon entropy of a discrete random variable X conditioned on a discrete (possibly multivariate) random variable Y .

Usage

```
conditionalShannonEntropy(x, y)
```

Arguments

<code>x</code>	A discrete vector.
<code>y</code>	A data frame.

Examples

```
set.seed(1)
x = round((runif(1000, min=0, max=5)))
Y = data.frame(round((runif(1000, min=0, max=5))), round((runif(1000, min=0, max=5))))
conditionalShannonEntropy(x=x,y=Y) ## 2.411972
```

conditionalStochasticComplexity

Conditional Stochastic Complexity for Multinomials

Description

Calculates the Stochastic Complexity of a discrete random variable X conditioned on a discrete (possibly multivariate) random variable Y . Variants for both factorized NML (fNML, Silander et al. 2008) and quotient NML (qNML, Silander et al. 2018) are included.

Usage

```
conditionalStochasticComplexity(x, y, score="fNML")
```

Arguments

<code>x</code>	A discrete vector.
<code>y</code>	A discrete vector or a data frame containing multiple discrete vectors to condition X on.
<code>score</code>	Default: fNML, optionally qNML can be passed.

References

Tomi Silander, Janne Leppä-aho, Elias Jääsaari, Teemu Roos; Quotient normalized maximum likelihood criterion for learning bayesian network structures, Proceedings of the 21nd International Conference on Artificial Intelligence and Statistics (AISTATS), PMLR, 2018

Tomi Silander, Teemu Roos, Petri Kontkanen and Petri Myllymäki; Factorized Normalized Maximum Likelihood Criterion for Learning Bayesian Network Structures, Proceedings of the 4th European Workshop on Probabilistic Graphical Models, 2008

Examples

```
set.seed(1)
x = round((runif(1000, min=0, max=5)))
Y = data.frame(round((runif(1000, min=0, max=5))), round((runif(1000, min=0, max=5))))
conditionalStochasticComplexity(x=x,y=Y,score="fNML") ## 2779.477
```

pSCCI	<i>Stochastic Complexity-based Conditional Independence Criterium (p-value)</i>
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Description

This is an adapted version of *SCCI* for which the output can be interpreted as a p-value. For this, we adapted *SCCI* such that if $SCCI = 0$ (X is independent of Y given Z) it gives a p-value greater than 0.01 and for $SCCI > 0$ (X is not independent of Y given Z) gives a p-value smaller or equal to 0.01. Note that we just transformed the output of *SCCI* and do not obtain a real p-value. In essence, we define the artificial p-value as follows. Let v the output of *SCCI* divided by the number of samples n . $p = 2^{-(6.643855-v)}$, which is equal to 0.01000001 if $v = 0$. Further, $p \leq 0.01$ for $SCCI \geq 0.000001$. We restrict the p-values to be between 0 and 1.

Unlike *SCCI*, *pSCCI* is currently only instantiated with fNML.

pSCCI can be used directly in the PC algorithm developed by Spirtes et al. (2000), which was implemented in the 'pcalg' R-package by Kalisch et al. (2012), as shown in the example.

Usage

```
pSCCI(x, y, S, suffStat)
```

Arguments

x	Position of x variabe (integer).
y	Position of y variabe (integer).
S	Vector of the position of zero or more conditioning variables (integer).
suffStat	This format was adapted such that it can be used in the PC algorithm and other algorithms from the 'pcalg' package. <i>SCCI</i> only need the filed "dm" that contains the data matrix.

References

Markus Kalisch, Martin Mächler, Diego Colombo, Marloes H. Maathuis, Peter Bühlmann; Causal inference using graphical models with the R package pcalg, Journal of Statistical Software, 2012

Alexander Marx and Jilles Vreeken; Testing Conditional Independence on Discrete Data using Stochastic Complexity, Proceedings of the 22nd International Conference on Artificial Intelligence and Statistics (AISTATS), PMLR, 2019

Peter Spirtes, Clark N. Glymour, Richard Scheines, David Heckerman, Christopher Meek, Gregory Cooper and Thomas Richardson; Causation, Prediction, and Search, MIT press, 2000

Examples

```
set.seed(1)
x = round((runif(1000, min=0, max=5)))
y = round((runif(1000, min=0, max=5)))
Z = data.frame(round((runif(1000, min=0, max=5))), round((runif(1000, min=0, max=5))))
## create data matrix
data_matrix = as.matrix(data.frame(x,y,S1=Z[,1], S2=Z[,2]))
suffStat = list(dm=data_matrix)
pSCCI(x=1,y=2,S=c(3,4),suffStat=suffStat) ## 0.01000001

### Using SCI within the PC algorithm
if(require(pcalg)){
  ## Load data
  data(gmD)
  V <- colnames(gmD$x)
  ## define sufficient statistics
  suffStat <- list(dm = gmD$x, nlev = c(3,2,3,4,2), adaptDF = FALSE)
  ## estimate CPDAG
  pc.D <- pc(suffStat,
             ## independence test: SCCI using FNML
             indepTest = pSCCI, alpha = 0.01, labels = V, verbose = TRUE)
}
if (require(pcalg) & require(Rgraphviz)) {
  ## show estimated CPDAG
  par(mfrow = c(1,2))
  plot(pc.D, main = "Estimated CPDAG")
  plot(gmD$g, main = "True DAG")
}
```

regret

Multinomial Regret Term

Description

Calculates the multinomial regret term for a discrete random variable with domain size k and sample size n (see Silander et al. 2018). Note that we use the logarithm to basis 2 to calculate the result. To compare the results to Silander et al. (2018), we need to multiply the result with $\log(2)$ to compare the results.

Usage

```
regret(n,k)
```

Arguments

n	Integer (sample size)
k	Integer (domain size)

References

Tomi Silander, Janne Leppä-aho, Elias Jääsaari, Teemu Roos; Quotient normalized maximum likelihood criterion for learning bayesian network structures, Proceedings of the 21nd International Conference on Artificial Intelligence and Statistics (AISTATS), PMLR, 2018

Examples

```
regret(50,10)          ## 19.1
regret(50,10) * log(2)  ## 13.24 (see Silander et al. 2018)
```

SCCI

Stochastic Complexity-based Conditional Independence Criterium

Description

Calculates whether two random variables X and Y are independent given a set of variables Z using *SCCI*. A score of 0 denotes that independence holds and values greater than 0 mean that X is not independent of Y given Z . For details on *SCCI*, we refer to Marx and Vreeken (AISTATS, 2019). If you use *SCCI* in your work, please cite Marx and Vreeken (AISTATS, 19).

The output of *SCCI*(..) is the difference in *number of bits* between conditioning X only on Z and conditioning on Z and Y . For the variant of *SCCI* that gives outputs that can be interpreted as p-values, please refer to pSCCI.

Usage

```
SCCI(x, y, Z, score="fNML", sym=FALSE)
```

Arguments

x	A discrete vector.
y	A discrete vector.
Z	A data frame consisting of zero or more columns of discrete vectors.
score	Default: fNML, optionally qNML can be passed.
sym	sym can be true or false

References

Alexander Marx and Jilles Vreeken; Testing Conditional Independence on Discrete Data using Stochastic Complexity, Proceedings of the 22nd International Conference on Artificial Intelligence and Statistics (AISTATS), PMLR, 2019

Examples

```
set.seed(1)
x = round((runif(1000, min=0, max=5)))
y = round((runif(1000, min=0, max=5)))
Z = data.frame(round((runif(1000, min=0, max=5))), round((runif(1000, min=0, max=5))))
SCCI(x=x,y=y,Z=Z,score="fNML",sym=FALSE) ## 0
```

shannonEntropy	<i>Shannon Entropy</i>
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Description

Calculates the Shannon entropy over data of a discrete random variable X .

Usage

```
shannonEntropy(x)
```

Arguments

`x` A discrete vector.

Examples

```
set.seed(1)
x = round((runif(1000, min=0, max=5)))
shannonEntropy(x=x) ## 2.522265
```

stochasticComplexity	<i>Stochastic Complexity for Multinomials</i>
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Description

Efficient implementation of the exact computation of stochastic complexity for multinomials (Sillander et al. 2008) for data over a discrete random variable X .

Usage

```
stochasticComplexity(x)
```

Arguments

x A discrete vector.

References

Tomi Silander, Teemu Roos, Petri Kontkanen and Petri Myllymäki; Factorized Normalized Maximum Likelihood Criterion for Learning Bayesian Network Structures, Proceedings of the 4th European Workshop on Probabilistic Graphical Models, 2008

Examples

```
set.seed(1)
x = round((runif(1000, min=0, max=5)))
stochasticComplexity(x=x) ## 2544.698
```

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