

# Package ‘LoTTA’

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**Type** Package

**Title** Bayesian Inference in Regression Discontinuity Designs

**Version** 0.1.0

**Description** Implementation of the LoTTA (Local Trimmed Taylor Approximation) model described in ``Bayesian Regression Discontinuity Design with Unknown Cutoff'' by Kowalska, van de Wiel, van der Pas (2024) <[doi:10.48550/arXiv.2406.11585](https://doi.org/10.48550/arXiv.2406.11585)>.

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Bin_data	<i>Function that splits the data into bins and computes the average in each bin</i>
----------	---

---

**Description**

Function that splits the data into bins and computes the average in each bin

**Usage**

Bin\_data(y, x, c = NULL, binsize = 0.2)

**Arguments**

- |         |   |
|---------|---|
| y       | • is the outcome data   |
| x       | • is the score data   |
| c       | • specifies the cutoff point, set to NULL if the binning of the data should be independent from c |
| binsize | • length of the interval that is one bin  |

**Value**

list with elements y\_bin: list of average values of y in each bin, x\_bin: list of middle points for each bin

---

BIN\_outcome\_function\_sample

*Function that evaluates the binary outcome function in a domain x, given the coefficients*

---

**Description**

Function that evaluates the binary outcome function in a domain x, given the coefficients

**Usage**

```
BIN_outcome_function_sample(coef_s, x, d_x, s_x)
```

**Arguments**

- |        |   |
|--------|---|
| coef_s | • list with the function coefficients             |
| x      | • points at which the function is evaluated       |
| d_x    | • shifting parameter that was used to normalize x |
| s_x    | • scaling parameter that was used to normalize x  |

**Value**

list with the values of the function

---

bounds

*function that finds maximum widow size to search for a cutoff*

---

**Description**

function that finds maximum widow size to search for a cutoff

**Usage**

```
bounds(x, ns = 25)
```

**Arguments**

- |    |  |
|----|--|
| x  | • score data   |
| ns | • minimum number of data points on each side of the cutoff to which cubic parts are fitted |

**Value**

list with ubl - minimum value of the window's left boundary point, ubr - maximum value of the window's right boundary point

---

CONT\_outcome\_function\_sample

*Function that evaluates the continuous outcome function in a domain  $x$ , given the coefficients*

---

**Description**

Function that evaluates the continuous outcome function in a domain  $x$ , given the coefficients

**Usage**

CONT\_outcome\_function\_sample(coef\_s, x, d\_x, s\_x, mu\_y, sd\_y)

**Arguments**

coef_s	• list with the function coefficients
x	• points at which the function is evaluated
d_x	• shifting parameter that was used to normalize $x$
s_x	• scaling parameter that was used to normalize $x$
mu_y	• shifting parameter that was used to normalize $y$
sd_y	• scaling parameter that was used to normalize $y$

**Value**

list with the values of the function

---

Initial_CONT_BIN	<i>function that samples initial values for fuzzy LoTTA model with a continuous prior and binary outcomes</i>
------------------	---

---

**Description**

function that samples initial values for fuzzy LoTTA model with a continuous prior and binary outcomes

**Usage**

Initial\_CONT\_BIN(x, t, y, C\_start, clb, cub, lb, ubr, ubl, s, jlb = 0.2)

**Arguments**

x	• score data
t	• treatment data
y	• outcome data
C_start	• posterior samples of cutoff location obtained through "cutoff_initial_CONT.txt"
clb	• left end of an interval on which the prior is supported
cub	• right end of an interval on which the prior is supported
lb	• minimum window size
ubr	• maximum value of the window's right boundary point
ubl	• minimum value of the window's left boundary point
s	• seed
jlb	• minimum jump size

**Value**

list with initial parameters values for LoTTA model with continuous score and binary outcomes, and .RNG.seed value

---

Initial_CONT_CONT	<i>function that samples initial values for fuzzy LoTTA model with a continuous prior and continuous outcomes</i>
-------------------	---

---

**Description**

function that samples initial values for fuzzy LoTTA model with a continuous prior and continuous outcomes

**Usage**

```
Initial_CONT_CONT(x, t, y, C_start, clb, cub, lb, ubr, ubl, s, jlb = 0.2)
```

**Arguments**

x	• score data
t	• treatment data
y	• outcome data
C_start	• posterior samples of cutoff location obtained through "cutoff_initial_CONT.txt"
clb	• left end of an interval on which the prior is supported
cub	• right end of an interval on which the prior is supported
lb	• minimum window size
ubr	• maximum value of the window's right boundary point
ubl	• minimum value of the window's left boundary point
s	• seed
jlb	• minimum jump size

**Value**

list with initial parameters values for LoTTA model with continuous score and continuous outcomes, and .RNG.seed value

---

Initial_DIS_BIN	<i>function that samples initial values for LoTTA with a discrete prior and binary outcomes</i>
-----------------	---

---

**Description**

function that samples initial values for LoTTA with a discrete prior and binary outcomes

**Usage**

```
Initial_DIS_BIN(x, t, y, Ct_start, cstart, grid, lb, ubr, ubl, s, jlb = 0.2)
```

**Arguments**

x	• score data
t	• treatment data
y	• outcome data
Ct_start	• posterior samples of cutoff location (categorized by natural numbers) obtained through "cutoff_initial_DIS.txt"
cstart	• the first point with a positive prior mass
grid	• distance between two consecutive points with nonzero prior mass
lb	• minimum window size (grid size in case of discrete score)
ubr	• maximum value of the window's right boundary point
ubl	• minimum value of the window's left boundary point
s	• seed
jlb	• minimum jump size

**Value**

list with initial parameters values for LoTTA model with discrete score and binary outcomes, and .RNG.seed value

---

Initial_DIS_CONT	<i>function that samples initial values for fuzzy LoTTA model with a discrete prior and binary outcomes</i>
------------------	---

---

## Description

function that samples initial values for fuzzy LoTTA model with a discrete prior and binary outcomes

## Usage

```
Initial_DIS_CONT(x, t, y, Ct_start, cstart, grid, lb, ubr, ubl, s, jlb = 0.2)
```

## Arguments

x	• score data
t	• treatment data
y	• outcome data
Ct_start	• posterior samples of cutoff location (categorized by natural numbers) obtained through "cutoff_initial_dis.txt" c
cstart	• the first point with a positive prior mass
grid	• distance between two consecutive points with nonzero prior mass
lb	• minimum window size (grid size in case of discrete score)
ubr	• maximum value of the window's right boundary point
ubl	• minimum value of the window's left boundary point
s	• seed
jlb	• minimum jump size

## Value

list with initial parameters values for LoTTA model with discrete score and continuous outcomes, and .RNG.seed value

---

Initial_FUZZy_BIN	<i>function that samples initial values for fuzzy LoTTA model with a known cutoff and binary outcomes</i>
-------------------	---

---

### Description

function that samples initial values for fuzzy LoTTA model with a known cutoff and binary outcomes

### Usage

```
Initial_FUZZy_BIN(x, t, y, c, lb, ubr, ubl, s, jlb = 0.2)
```

### Arguments

x	• score data
t	• treatment data
y	• outcome data
c	• cutoff location
lb	• minimum window size
ubr	• maximum value of the window's right boundary point
ubl	• minimum value of the window's left boundary point
s	• seed
jlb	• minimum jump size

### Value

list with initial parameters values for fuzzy LoTTA model with a known cutoff and binary outcomes, and .RNG.seed value

---

Initial_FUZZy_CONT	<i>function that samples initial values for fuzzy LoTTA model with a known cutoff and continuous outcomes</i>
--------------------	---

---

### Description

function that samples initial values for fuzzy LoTTA model with a known cutoff and continuous outcomes

### Usage

```
Initial_FUZZy_CONT(x, t, y, c, lb, ubr, ubl, s, jlb = 0.2)
```



**Arguments**

x	• score data
t	• treatment data
y	• outcome data
c	• cutoff value
lb	• minimum window size
ubr	• maximum value of the window's right boundary point
ubl	• minimum value of the window's left boundary point
s	• seed
jlb	• minimum jump size

**Value**

list with initial parameters values for LoTTA model with continuous score and continuous outcomes, and .RNG.seed value

---

Initial_SHARP_BIN	<i>function that samples initial values for sharp LoTTA model with binary outcomes</i>
-------------------	--

---

**Description**

function that samples initial values for sharp LoTTA model with binary outcomes

**Usage**

```
Initial_SHARP_BIN(x, y, c, lb, ubr, ubl, s)
```

**Arguments**

x	• score data
y	• outcome data
c	• cutoff location
lb	• minimum window size
ubr	• maximum value of the window's right boundary point
ubl	• minimum value of the window's left boundary point
s	• seed

**Value**

list with initial parameters values for sharp LoTTA model with binary outcomes, and .RNG.seed value

---

Initial_SHARP_CONT	<i>function that samples initial values for sharp LoTTA model with continuous outcomes</i>
--------------------	--

---

### Description

function that samples initial values for sharp LoTTA model with continuous outcomes

### Usage

```
Initial_SHARP_CONT(x, y, c, lb, ubr, ubl, s)
```

### Arguments

x	• score data
y	• outcome data
c	• cutoff location
lb	• minimum window size
ubr	• maximum value of the window's right boundary point
ubl	• minimum value of the window's left boundary point
s	• seed

### Value

list with initial parameters values for sharp LoTTA model with continuous outcomes, and .RNG.seed value

---

Initial_treatment_c	<i>function that samples initial values for the treatment model with a known cutoff</i>
---------------------	---

---

### Description

function that samples initial values for the treatment model with a known cutoff

### Usage

```
Initial_treatment_c(x, t, c, lb, ubr, ubl, s, jlb = 0.2)
```

**Arguments**

x	• score data
t	• treatment data
c	• cutoff location
lb	• minimum window size
ubr	• maximum value of the window's right boundary point
ubl	• minimum value of the window's left boundary point
s	• seed
jlb	• minimum jump size

**Value**

list with initial parameters values for LoTTA model with continuous score and .RNG.seed value

---

Initial\_treatment\_CONT

*function that samples initial values for the treatment model with a continuous prior*

---

**Description**

function that samples initial values for the treatment model with a continuous prior

**Usage**

```
Initial_treatment_CONT(x, t, C_start, clb, cub, lb, ubr, ubl, s, jlb = 0.2)
```

**Arguments**

x	• score data
t	• treatment data
C_start	• posterior samples of cutoff location obtained through "cutoff_initial_CONT.txt"
clb	• left end of an interval on which the prior is supported
cub	• right end of an interval on which the prior is supported
lb	• minimum window size
ubr	• maximum value of the window's right boundary point
ubl	• minimum value of the window's left boundary point
s	• seed
jlb	• minimum jump size

**Value**

list with initial parameters values for LoTTA model with continuous score and .RNG.seed value

---

`Initial_treatment_DIS` *function that samples initial values for the treatment model with a discrete prior*

---

### Description

function that samples initial values for the treatment model with a discrete prior

### Usage

```
Initial_treatment_DIS(x, t, Ct_start, cstart, grid, lb, ubr, ubl, s, jlb = 0.2)
```

### Arguments

<code>x</code>	• score data
<code>t</code>	• treatment data
<code>Ct_start</code>	• posterior samples of cutoff location (categorized by natural numbers) obtained through "cutoff_initial_dis.txt"
<code>cstart</code>	• the first point with a positive prior mass
<code>grid</code>	• distance between two consecutive points with nonzero prior mass
<code>lb</code>	• minimum window size (grid size in case of discrete score)
<code>ubr</code>	• maximum value of the window's right boundary point
<code>ubl</code>	• minimum value of the window's left boundary point
<code>s</code>	• seed
<code>jlb</code>	• minimum jump size

### Value

list with initial parameters values for treatment model with discrete score and .RNG.seed value

---

`invlogit` *inverse logit function*

---

### Description

inverse logit function

### Usage

```
invlogit(x)
```

### Arguments

<code>x</code>	• score data
----------------	--------------

**Value**

value of inverse logit function at x

---

logit	<i>logit function</i>
-------	-----------------------

---

**Description**

logit function

**Usage**

logit(x)

**Arguments**

x                      • score data

**Value**

value of logit function at x

---

LoTTA_fuzzy_BIN	<i>LoTTA_fuzzy_BIN</i>
-----------------	------------------------

---

**Description**

Function that fits LoTTA model to the fuzzy RD data with binary outcomes with an either known or unknown/suspected cutoff. It supports two types of priors on the cutoff location: a scaled beta distribution of the form  $\text{beta}(\alpha, \beta)(\text{cub} - \text{clb}) + \text{clb}$  and a discrete distribution with the support of the form  $\text{cstart} + \text{grid } i$  for  $i = 0, \dots, (\text{cend} - \text{cstart}) / \text{grid}$ . The score does NOT have to be normalized beforehand. We recommend NOT to transform the data before imputing it into the function, except for initial trimming of the score which should be done beforehand. The further trimming for the sensitivity analysis can be done through the function, which ensures that the data is normalized before the trimming.

**Usage**

```
LoTTA_fuzzy_BIN(  
  x,  
  t,  
  y,  
  c_prior,  
  jlb = 0.2,  
  ci = 0.95,
```

```

trimmed = NULL,
outcome_prior = list(pr = 1e-04),
n_min = 25,
param = c("c", "j", "kl", "kr", "eff", "a0l", "a1l", "a2l", "a3l", "a0r", "a1r", "a2r",
"a3r", "b1lt", "a1lt", "a2lt", "b2lt", "b1rt", "a1rt", "a2rt", "b2rt", "k1t", "k2t"),
normalize = TRUE,
n.chains = 4,
burnin = 10000,
sample = 1000,
adapt = 500,
inits = NULL,
method = "parallel",
seed = NULL,
...
)

```

### Arguments

x	• is the score data
t	• is the treatment allocation data
y	• is the binary outcome data
c_prior	• specifies the cutoff prior in case of the unknown cutoff or the cutoff point if the cutoff is known. Takes as value a number if the cutoff is known or a list of values otherwise. For a continuous prior the list requires the following elements: clb - left end of the interval cub - right end of the interval in which the scaled and translated beta distribution is defined, alpha (optional) - shape parameter, default value = 1, beta (optional) - shape parameter, default value = 1. For a discrete prior the list requires the following elements: cstart - first point with positive prior mass, cend - last point with positive prior mass, grid - distance between the consecutive points in the support weights (optional) - vector of weights assigned to each point in the support, default is vector of 1's (uniform distribution)
jlb	• minimum jump size
ci	• specifies the probability level 1-alpha for the highest posterior density intervals; default is ci = 0.95
trimmed	• takes as a value NULL or a vector of two values. It specifies potential trimming of the data. If set to NULL no trimming is applied to the data. If a list of two values is provided the data is trimmed to include data points with the score x in between those values; default is trimmed=NULL
outcome_prior	• takes as a value a list with elements 'pr'. 'pr' specifies precision in the normal priors on the coefficients in the outcome function; default is list('pr'=0.0001)
n_min	• specifies the minimum number of data points to which a cubic part of the outcome function is fit to ensure stability of the sampling procedure; default is n_min=25
param	• takes as a value a vector with names of the parameters that are to be sampled; default is the list of all parameters

normalize	<ul style="list-style-type: none"> <li>• specifies if the data is to be normalized. The data is normalized as follows. If the prior is continuous: <math>x\_normalized=(x-d)/s</math>, where <math>d=(\min(x)+\max(x))*0.5</math> and <math>s=\max(x)-\min(x)</math>. If the prior is discrete: <math>x\_normalized=x/s</math>, where <math>s=10^m</math>, where <math>m</math> is chosen so that <math>lmax(abs(x))-1l</math> is minimal. The priors inside the model are specified for the normalized data, in extreme cases not normalizing the data may lead to unreliable results; default is normalize=TRUE</li> </ul>
n.chains	<ul style="list-style-type: none"> <li>• specifies the number of chains in the MCMC sampler; default is n.chains=4</li> </ul>
burnin	<ul style="list-style-type: none"> <li>• specifies the number of burnin iterations without the adaptive iterations; default is burnin=5000</li> </ul>
sample	<ul style="list-style-type: none"> <li>• specifies the number of samples per chain; default is samples=5000</li> </ul>
adapt	<ul style="list-style-type: none"> <li>• specifies the number of adaptive iterations in the MCMC sampler; default is adapt=1000</li> </ul>
inits	<ul style="list-style-type: none"> <li>• initial values for the sampler. By default the initial values are sampled inside the function. To run LoTTA with a method other than "parallel" inits must be set to NA or to a user defined value. If the user wants to provide its own values please refer to run.jags manual; default inits=NULL</li> </ul>
method	<ul style="list-style-type: none"> <li>• set to default as 'parallel', which allows to sample the chains in parallel reducing computation time. To read more about possible method values type ?run.jags; default method='parallel'</li> </ul>
seed	<ul style="list-style-type: none"> <li>• specifies the seed for replicability purposes; default is seed=NULL</li> </ul>
...	<ul style="list-style-type: none"> <li>• other arguments of run.jags function. For more details type ?run.jags</li> </ul>

## Value

The function returns the list with the elements:

- Effect\_estimate: contains a list with MAP estimate and HDI of the treatment effect, the cutoff location (if unknown) and the discontinuity size in the treatment probability function (compliance rate at c) on the original, unnormalized scale;
- JAGS\_output: contains output of the run.jags function for the normalized data if normalize=TRUE, based on this output mixing of the chains can be assessed;
- Samples: contains posterior samples of the treatment effect (eff), cutoff location (c) if unknown, and compliance rate (j);
- Normalized\_data: contains a list of the normalized data (if normalized=TRUE) and the parameters used to normalize the data (see arg normalize);
- Priors: contains a list of the priors' parameters ;
- Inits contains the list of initial values and .RNG.seed value

## Examples

```
# functions to generate the data

ilogit <- function(x) {
  return(1 / (1 + exp(-x)))
}
```

```

fun_prob55 <- function(x) {
  P = rep(0, length(x))
  P[x >= 0.] = ilogit((8.5 * x[x >= 0.] - 1.5)) / 10.5 + 0.65 - 0.0007072
  P[x < 0.] = (x[x < 0.] + 1)^4 / 15 + 0.05
  return(P)
}

sample_prob55 <- function(x) {
  P = rep(0, length(x))
  P[x >= 0.] = ilogit((8.5 * x[x >= 0.] - 1.5)) / 10.5 + 0.65 - 0.0007072
  P[x < 0.] = (x[x < 0.] + 1)^4 / 15 + 0.05
  t = rep(0, length(x))
  for (j in 1:length(x)) {
    t[j] = sample(c(1, 0), 1, prob = c(P[j], 1 - P[j]))
  }
  return(t)
}

funB <- function(x) {
  y = x
  x2 = x[x >= 0]
  x1 = x[x < 0]
  y[x < 0] = 1 / (1 + exp(-2 * x1)) - 0.5 + 0.4
  y[x >= 0] = (log(x2 * 2 + 1) - 0.15 * x2^2) * 0.6 - 0.20 + 0.4
  return(y)
}

funB_sample_binary <- function(x) {
  y = x
  P = funB(x)
  for (j in 1:length(x)) {
    y[j] = sample(c(1, 0), 1, prob = c(P[j], 1 - P[j]))
  }
  return(y)
}

## Toy example - for the function check only! ##
N=100
x = sort(runif(N, -1, 1))
t = sample_prob55(x)
y = funB_sample_binary(x)
c_prior=0 # known cutoff c=0

# running LoTTA model on fuzzy RDD with binary outcomes;
out = LoTTA_fuzzy_BIN(x,t,y,c_prior,burnin = 50,sample = 50,adapt=10,n.chains=1
,method = 'simple',inits = NA)

## Use case example ##

N=500
x = sort(runif(N, -1, 1))
t = sample_prob55(x)

```



```

y = funB_sample_binary(x)
# comment out to try different priors:
  c_prior=list(clb=-0.25,cub=0.25) # uniform prior on the interval [-0.25,0.25]
# c_prior=list(cstart=-0.25,cend=0.25,grid=0.05) # uniform discrete prior
# on -0.25, -0.2, ..., 0.25
# c_prior=0 # known cutoff c=0

# running LoTTA model on fuzzy RDD with binary outcomes and unknown cutoff;
# cutoff = 0, compliance rate = 0.55, treatment effect = -0.3636364
# remember to check convergence and adjust burnin, sample and adapt if needed
out = LoTTA_fuzzy_BIN(x,t,y,c_prior,burnin = 10000,sample = 5000,adapt=1000)

# print effect estimate:
out$Effect_estimate
# print JAGS output to asses convergence (the output is for normalized data)
out$JAGS_output
# plot posterior fit of the outcome function
LoTTA_plot_outcome(out,nbins = 60)
# plot posterior fit of the treatment probablity function
LoTTA_plot_treatment(out,nbins = 60)
# plot dependence of the treatment effect on the cutoff location
LoTTA_plot_effect(out)

```

---

LoTTA\_fuzzy\_CONT

*LoTTA\_fuzzy\_CONT*


---

## Description

Function that fits LoTTA model to the fuzzy RD data with continuous outcomes with an either known or unknown/suspected cutoff. It supports two types of priors on the cutoff location: a scaled beta distribution of the form  $\text{beta}(\alpha, \beta)(\text{cub} - \text{clb}) + \text{clb}$  and a discrete distribution with the support of the form  $\text{cstart} + \text{grid} \cdot i$  for  $i = 0, \dots, (\text{cend} - \text{cstart}) / \text{grid}$ . The score does NOT have to be normalized beforehand. We recommend NOT to transform the data before imputing it into the function, except for initial trimming of the score which should be done beforehand. The further trimming for the sensitivity analysis can be done through the function, which ensures that the data is normalized before the trimming.

## Usage

```

LoTTA_fuzzy_CONT(
  x,
  t,
  y,
  c_prior,
  jlb = 0.2,
  ci = 0.95,
  trimmed = NULL,

```

```

outcome_prior = list(pr = 1e-04, shape = 0.01, scale = 0.01),
n_min = 25,
param = c("c", "j", "kl", "kr", "eff", "a0l", "a1l", "a2l", "a3l", "a0r", "a1r", "a2r",
"a3r", "b1lt", "a1lt", "a2lt", "b2lt", "b1rt", "a1rt", "a2rt", "b2rt", "k1t", "k2t",
"tau1r", "tau2r", "tau1l", "tau2l"),
normalize = TRUE,
n.chains = 4,
burnin = 10000,
sample = 1000,
adapt = 500,
inits = NULL,
method = "parallel",
seed = NULL,
...
)

```

### Arguments

x	• is the score data
t	• is the treatment allocation data
y	• is the binary outcome data
c_prior	• specifies the cutoff prior in case of the unknown cutoff or the cutoff point if the cutoff is known. Takes as value a number if the cutoff is known or a list of values otherwise. For a continuous prior the list requires the following elements: clb - left end of the interval cub - right end of the interval in which the scaled and translated beta distribution is defined, alpha (optional) - shape parameter, default value = 1, beta (optional) - shape parameter, default value = 1. For a discrete prior the list requires the following elements: cstart - first point with positive prior mass, cend - last point with positive prior mass, grid - distance between the consecutive points in the support weights (optional) - vector of weights assigned to each point in the support, default is vector of 1's (uniform distribution)
jlb	• minimum jump size
ci	• specifies the probability level 1-alpha for the highest posterior density intervals; default is ci = 0.95
trimmed	• takes as a value NULL or a vector of two values. It specifies potential trimming of the data. If set to NULL no trimming is applied to the data. If a list of two values is provided the data is trimmed to include data points with the score x in between those values; default is trimmed=NULL
outcome_prior	• takes as a value a list with elements 'pr' and 'shape', 'scale'. 'pr' specifies precision in the normal priors on the coefficients in the outcome function. 'shape' and 'scale' specify the shape and scale parameters in the gamma prior on the precision of the error terms; default is list('pr'=0.0001,'shape'=0.01,'scale'=0.01)
n_min	• specifies the minimum number of data points to which a cubic part of the outcome function is fit to ensure stability of the sampling procedure; default is n_min=25

param	<ul style="list-style-type: none"> <li>• takes as a value a vector with names of the parameters that are to be sampled; default is the list of all parameters</li> </ul>
normalize	<ul style="list-style-type: none"> <li>• specifies if the data is to be normalized. The data is normalized as follows. If the prior is continuous: <math>x\_normalized=(x-d)/s</math>, where <math>d=(\min(x)+\max(x))*0.5</math> and <math>s=\max(x)-\min(x)</math>, If the prior is discrete: <math>x\_normalized=x/s</math>, where <math>s=10^m</math>, where <math>m</math> is chosen so that <math>\lvert \max(\text{abs}(x))-1 \rvert</math> is minimal. The outcome data is normalized as follows: <math>y\_normalized=(y-\mu)/sd</math>, where <math>\mu=\text{mean}(y)</math> and <math>sd=\text{sd}(y)</math>. The priors inside the model are specified for the normalized data, in extreme cases not normalizing the data may lead to unreliable results; default is <code>normalize=TRUE</code></li> </ul>
n.chains	<ul style="list-style-type: none"> <li>• specifies the number of chains in the MCMC sampler; default is <code>n.chains=4</code></li> </ul>
burnin	<ul style="list-style-type: none"> <li>• specifies the number of burnin iterations without the adaptive iterations; default is <code>burnin=5000</code></li> </ul>
sample	<ul style="list-style-type: none"> <li>• specifies the number of samples per chain; default is <code>samples=5000</code></li> </ul>
adapt	<ul style="list-style-type: none"> <li>• specifies the number of adaptive iterations in the MCMC sampler; default is <code>adapt=1000</code></li> </ul>
inits	<ul style="list-style-type: none"> <li>• initial values for the sampler. By default the initial values are sampled inside the function. To run LoTTA with a method other than "parallel" inits must be set to NA or to a user defined value. If the user wants to provide its own values please refer to run.jags manual; default <code>inits=NULL</code></li> </ul>
method	<ul style="list-style-type: none"> <li>• set to default as 'parallel', which allows to sample the chains in parallel reducing computation time. To read more about possible method values type <code>?run.jags</code>; default <code>method='parallel'</code></li> </ul>
seed	<ul style="list-style-type: none"> <li>• specifies the seed for replicability purposes; default is <code>seed=NULL</code></li> </ul>
...	<ul style="list-style-type: none"> <li>• other arguments of run.jags function. For more details type <code>?run.jags</code></li> </ul>

## Value

The function returns the list with the elements:

- **Effect\_estimate**: contains a list with MAP estimate and HDI of the treatment effect, the cutoff location (if unknown) and the discontinuity size in the treatment probability function (compliance rate at  $c$ ) on the original, unnormalized scale;
- **JAGS\_output**: contains output of the run.jags function for the normalized data if `normalize=TRUE`, based on this output mixing of the chains can be assessed;
- **Samples**: contains posterior samples of the treatment effect ( $\text{eff}$ ), cutoff location ( $c$ ) if unknown, and compliance rate ( $j$ );
- **Normalized\_data**: contains a list of the normalized data (if `normalize=TRUE`) and the parameters used to normalize the data (see arg `normalize`);
- **Priors**: contains a list of the priors' parameters ;
- **Inits** contains the list of initial values and `.RNG.seed` value

**Examples**

```

# functions to generate the data

ilogit <- function(x) {
  return(1 / (1 + exp(-x)))
}

fun_prob55 <- function(x) {
  P = rep(0, length(x))
  P[x >= 0.] = ilogit((8.5 * x[x >= 0.] - 1.5)) / 10.5 + 0.65 - 0.0007072
  P[x < 0.] = (x[x < 0.] + 1)^4 / 15 + 0.05
  return(P)
}

sample_prob55 <- function(x) {
  P = rep(0, length(x))
  P[x >= 0.] = ilogit((8.5 * x[x >= 0.] - 1.5)) / 10.5 + 0.65 - 0.0007072
  P[x < 0.] = (x[x < 0.] + 1)^4 / 15 + 0.05
  t = rep(0, length(x))
  for (j in 1:length(x)) {
    t[j] = sample(c(1, 0), 1, prob = c(P[j], 1 - P[j]))
  }
  return(t)
}

funB <- function(x) {
  y = x
  x2 = x[x >= 0]
  x1 = x[x < 0]
  y[x < 0] = 1 / (1 + exp(-2 * x1)) - 0.5 + 0.4
  y[x >= 0] = (log(x2 * 2 + 1) - 0.15 * x2^2) * 0.6 - 0.20 + 0.4
  return(y)
}

funB_sample <- function(x) {
  y = funB(x) + rnorm(length(x), 0, 0.1)
  return(y)
}

## Toy example - for the function check only! ##
N=100
x = sort(runif(N, -1, 1))
t = sample_prob55(x)
y = funB_sample(x)
c_prior=0 # known cutoff c=0

# running LoTTA model on fuzzy RDD with continuous outcomes;
out = LoTTA_fuzzy_CONT(x,t,y,c_prior,burnin = 50,sample = 50,adapt=10,n.chains=1
,method = 'simple',inits = NA)

## Use case example ##

```

```

N=500
x = sort(runif(N, -1, 1))
t = sample_prob55(x)
y = funB_sample(x)
# comment out to try different priors:
c_prior=list(clb=-0.25,cub=0.25) # uniform prior on the interval [-0.25,0.25]
# c_prior=list(cstart=-0.25,cend=0.25,grid=0.05) # uniform discrete prior
# on -0.25, -0.2, ..., 0.25
# c_prior=0 # known cutoff c=0

# running LoTTA model on fuzzy RDD with continuous outcomes and unknown cutoff;
# cutoff = 0, compliance rate = 0.55, treatment effect = -0.3636364
# remember to check convergence and adjust burnin, sample and adapt if needed
out = LoTTA_fuzzy_CONT(x,t,y,c_prior,burnin = 10000,sample = 5000,adapt=1000)

# print effect estimate:
out$Effect_estimate
# print JAGS output to asses convergence (the output is for normalized data)
out$JAGS_output
# plot posterior fit of the outcome function
LoTTA_plot_outcome(out)
# plot posterior fit of the treatment probability function
LoTTA_plot_treatment(out,nbins = 60)
# plot dependence of the treatment effect on the cutoff location
LoTTA_plot_effect(out,nbins = 5)

```

---

LoTTA\_plot\_effect

*LoTTA\_plot\_effect*


---

## Description

Function that visualizes the impact of the cutoff location on the treatment effect estimate. It plots two figures. The bottom figure depicts the posterior density of the cutoff location. The top figure depicts the box plot of the treatment effect given the cutoff point. If the prior on the cutoff location was discrete each box corresponds to a distinct cutoff point. If the prior was continuous each box correspond to an interval of cutoff values (the number of intervals can be changed through nbins).

## Usage

```

LoTTA_plot_effect(
  LoTTA_posterior,
  nbins = 10,
  probs = c(0.025, 0.975),
  x_lab = "Cutoff location",
  y_lab1 = "Treatment effect",
  y_lab2 = "Density of cutoff location",
  title = "Cutoff location vs. Treatment effect",

```

```

axis.text = element_text(family = "sans", size = 10),
text = element_text(family = "serif"),
plot.theme = theme_classic(base_size = 14),
plot.title = element_text(hjust = 0.5),
...
)

```

## Arguments

LoTTA_posterior	<ul style="list-style-type: none"> <li>output of one of the LoTTA functions (LoTTA_fuzzy_CONT, LoTTA_fuzzy_BIN) with all parameters sampled (the default option in those functions)</li> </ul>
nbins	<ul style="list-style-type: none"> <li>number of bins to aggregate the values of the posterior cutoff location</li> </ul>
probs	<ul style="list-style-type: none"> <li>list of two quantiles that limit the range of cutoff values displayed on the plots</li> </ul>
x_lab	<ul style="list-style-type: none"> <li>label of the x-axis</li> </ul>
y_lab1	<ul style="list-style-type: none"> <li>label of the y-axis of the bottom plot</li> </ul>
y_lab2	<ul style="list-style-type: none"> <li>label of the y-axis of the top plot</li> </ul>
title	<ul style="list-style-type: none"> <li>title of the plot</li> </ul>
axis.text	<ul style="list-style-type: none"> <li>can be any value that is accepted in the argument <i>axis.text</i> in the <i>theme</i> function of ggplot2 package, refer to ggplot2 manual for the possible values; by default is changes font to a serif one axis.text=element_text(family = "sans",size = 10)</li> </ul>
text	<ul style="list-style-type: none"> <li>can be any value that is accepted in the argument <i>text</i> in the <i>theme</i> function of ggplot2 package, refer to ggplot2 manual for the possible values; by default is changes font to a serif one text=element_text(family='serif')</li> </ul>
plot.theme	<ul style="list-style-type: none"> <li>ggplot2 plot theme (see <a href="https://ggplot2.tidyverse.org/reference/ggtheme.html">https://ggplot2.tidyverse.org/reference/ggtheme.html</a>) possibly with additional arguments, it takes the default value plot.theme=theme_classic(base_size = 14),</li> </ul>
plot.title	<ul style="list-style-type: none"> <li>can be any value that is accepted in the argument <i>plot.title</i> in the <i>theme</i> function of ggplot2 package, refer to ggplot2 manual for the possible values; by default it centers the plot title plot.title = element_text(hjust = 0.5)</li> </ul>
...	<ul style="list-style-type: none"> <li>other arguments of the <i>theme</i> function, refer to ggplot2 manual</li> </ul>

## Value

ggplot2 object

## Examples

```

# functions to generate the data

ilogit <- function(x) {
  return(1 / (1 + exp(-x)))
}

```

```

fun_prob55 <- function(x) {
  P = rep(0, length(x))
  P[x >= 0.] = ilogit((8.5 * x[x >= 0.] - 1.5)) / 10.5 + 0.65 - 0.0007072
  P[x < 0.] = (x[x < 0.] + 1)^4 / 15 + 0.05
  return(P)
}

sample_prob55 <- function(x) {
  P = rep(0, length(x))
  P[x >= 0.] = ilogit((8.5 * x[x >= 0.] - 1.5)) / 10.5 + 0.65 - 0.0007072
  P[x < 0.] = (x[x < 0.] + 1)^4 / 15 + 0.05
  t = rep(0, length(x))
  for (j in 1:length(x)) {
    t[j] = sample(c(1, 0), 1, prob = c(P[j], 1 - P[j]))
  }
  return(t)
}

funB <- function(x) {
  y = x
  x2 = x[x >= 0]
  x1 = x[x < 0]
  y[x < 0] = 1 / (1 + exp(-2 * x1)) - 0.5 + 0.4
  y[x >= 0] = (log(x2 * 2 + 1) - 0.15 * x2^2) * 0.6 - 0.20 + 0.4
  return(y)
}

funB_sample <- function(x) {
  y = funB(x) + rnorm(length(x), 0, 0.1)
  return(y)
}

## Use case example ##

N=500
x = sort(runif(N, -1, 1))
t = sample_prob55(x)
y = funB_sample(x)
# comment out to try different priors:
c_prior=list(clb=-0.25,cub=0.25) # uniform prior on the interval [-0.25,0.25]
# c_prior=list(cstart=-0.25,cend=0.25,grid=0.05) # uniform discrete prior
# on -0.25, -0.2, ..., 0.25
# c_prior=0 # known cutoff c=0

# running LoTTA model on fuzzy RDD with continuous outcomes and unknown cutoff;
# cutoff = 0, compliance rate = 0.55, treatment effect = -0.3636364
# remember to check convergence and adjust burnin, sample and adapt if needed
out = LoTTA_fuzzy_CONT(x,t,y,c_prior,burnin = 10000,sample = 5000,adapt=1000)

# print effect estimate:
out$Effect_estimate
# print JAGS output to asses convergence (the output is for normalized data)
out$JAGS_output

```

```
# plot posterior fit of the outcome function
LoTTA_plot_outcome(out,nbins = 60)
# plot posterior fit of the treatment probability function
LoTTA_plot_treatment(out,nbins = 60)
# plot dependence of the treatment effect on the cutoff location
LoTTA_plot_effect(out)
```

---

LoTTA\_plot\_effect\_CONT

*Function that visualizes the impact of the cutoff location on the treatment effect estimate. It plots two figures. The bottom figure depicts the posterior density of the cutoff location. The top figure depicts the box plot of the treatment effect given the cutoff point. If the prior on the cutoff location was discrete each box corresponds to a distinct cutoff point. If the prior was continuous each box corresponds to an interval of cutoff values (the number of intervals can be changed through nbins).*

---

## Description

Function that visualizes the impact of the cutoff location on the treatment effect estimate. It plots two figures. The bottom figure depicts the posterior density of the cutoff location. The top figure depicts the box plot of the treatment effect given the cutoff point. If the prior on the cutoff location was discrete each box corresponds to a distinct cutoff point. If the prior was continuous each box corresponds to an interval of cutoff values (the number of intervals can be changed through nbins).

## Usage

```
LoTTA_plot_effect_CONT(
  LoTTA_posterior,
  nbins = 10,
  probs = c(0.025, 0.975),
  x_lab = "Cutoff location",
  y_lab1 = "Treatment effect",
  y_lab2 = "Density of cutoff location",
  title = "Cutoff location vs. Treatment effect",
  axis.text = element_text(family = "sans", size = 10),
  text = element_text(family = "serif"),
  plot.theme = theme_classic(base_size = 14),
  plot.title = element_text(hjust = 0.5),
  ...
)
```



**Arguments**

LoTTA_posterior	<ul style="list-style-type: none"> <li>• output of one of the LoTTA functions (LoTTA_fuzzy_CONT, LoTTA_fuzzy_BIN) with all parameters sampled (the default option in those functions)</li> </ul>
nbins	<ul style="list-style-type: none"> <li>• number of bins to aggregate the input data</li> </ul>
probs	<ul style="list-style-type: none"> <li>• list of two quantiles that limit the range of cutoff values displayed on the plots</li> </ul>
x_lab	<ul style="list-style-type: none"> <li>• label of the x-axis</li> </ul>
y_lab1	<ul style="list-style-type: none"> <li>• label of the y-axis of the bottom plot</li> </ul>
y_lab2	<ul style="list-style-type: none"> <li>• label of the y-axis of the top plot</li> </ul>
title	<ul style="list-style-type: none"> <li>• title of the plot</li> </ul>
axis.text	<ul style="list-style-type: none"> <li>• can be any value that is accepted in the argument <i>axis.text</i> in the <i>theme</i> function of ggplot2 package, refer to ggplot2 manual for the possible values; by default is changes font to a serif one <code>axis.text=element_text(family = "sans",size = 10)</code></li> </ul>
text	<ul style="list-style-type: none"> <li>• can be any value that is accepted in the argument <i>text</i> in the <i>theme</i> function of ggplot2 package, refer to ggplot2 manual for the possible values; by default is changes font to a serif one <code>text=element_text(family='serif')</code></li> </ul>
plot.theme	<ul style="list-style-type: none"> <li>• ggplot2 plot theme (see <a href="https://ggplot2.tidyverse.org/reference/ggtheme.html">https://ggplot2.tidyverse.org/reference/ggtheme.html</a>) possibly with additional arguments, it takes the default value <code>plot.theme=theme_classic(base_size = 14)</code>,</li> </ul>
plot.title	<ul style="list-style-type: none"> <li>• can be any value that is accepted in the argument <i>plot.title</i> in the <i>theme</i> function of ggplot2 package, refer to ggplot2 manual for the possible values; by default it centers the plot title <code>plot.title = element_text(hjust = 0.5)</code></li> </ul>
...	<ul style="list-style-type: none"> <li>• other arguments of the <i>theme</i> function, refer to ggplot2 manual</li> </ul>

**Value**

ggplot2 object

---

**LoTTA\_plot\_effect\_DIS** *Function that visualizes the impact of the cutoff location on the treatment effect estimate. It plots two figures. The bottom figure depicts the posterior density of the cutoff location. The top figure depicts the box plot of the treatment effect given the cutoff point. If the prior on the cutoff location was discrete each box corresponds to a distinct cutoff point. If the prior was continuous each box correspond to an interval of cutoff values (the number of intervals can be changed through nbins).*

---

## Description

Function that visualizes the impact of the cutoff location on the treatment effect estimate. It plots two figures. The bottom figure depicts the posterior density of the cutoff location. The top figure depicts the box plot of the treatment effect given the cutoff point. If the prior on the cutoff location was discrete each box corresponds to a distinct cutoff point. If the prior was continuous each box correspond to an interval of cutoff values (the number of intervals can be changed through nbins).

## Usage

```
LoTTA_plot_effect_DIS(
  LoTTA_posterior,
  probs = c(0.025, 0.975),
  x_lab = "Cutoff location",
  y_lab1 = "Treatment effect",
  y_lab2 = "Density of cutoff location",
  title = "Cutoff location vs. Treatment effect",
  axis.text = element_text(family = "sans", size = 10),
  text = element_text(family = "serif"),
  plot.theme = theme_classic(base_size = 14),
  plot.title = element_text(hjust = 0.5),
  ...
)
```

## Arguments

LoTTA_posterior	<ul style="list-style-type: none"> <li>• output of one of the LoTTA functions (LoTTA_fuzzy_CONT, LoTTA_fuzzy_BIN) with all parameters sampled (the default option in those functions)</li> </ul>
probs	<ul style="list-style-type: none"> <li>• list of two quantiles that limit the range of cutoff values displayed on the plots</li> </ul>
x_lab	<ul style="list-style-type: none"> <li>• label of the x-axis</li> </ul>
y_lab1	<ul style="list-style-type: none"> <li>• label of the y-axis of the bottom plot</li> </ul>
y_lab2	<ul style="list-style-type: none"> <li>• label of the y-axis of the top plot</li> </ul>
title	<ul style="list-style-type: none"> <li>• title of the plot</li> </ul>
axis.text	<ul style="list-style-type: none"> <li>• can be any value that is accepted in the argument <i>axis.text</i> in the <i>theme</i> function of ggplot2 package, refer to ggplot2 manual for the possible values; by default is changes font to a serif one axis.text=element_text(family = "sans",size = 10)</li> </ul>
text	<ul style="list-style-type: none"> <li>• can be any value that is accepted in the argument <i>text</i> in the <i>theme</i> function of ggplot2 package, refer to ggplot2 manual for the possible values; by default is changes font to a serif one text=element_text(family='serif')</li> </ul>
plot.theme	<ul style="list-style-type: none"> <li>• ggplot2 plot theme (see <a href="https://ggplot2.tidyverse.org/reference/ggtheme.html">https://ggplot2.tidyverse.org/reference/ggtheme.html</a>) possibly with additional arguments, it takes the default value plot.theme=theme_classic(base_size = 14),</li> </ul>
plot.title	<ul style="list-style-type: none"> <li>• can be any value that is accepted in the argument <i>plot.title</i> in the <i>theme</i> function of ggplot2 package, refer to ggplot2 manual for the possible values; by default it centers the plot title plot.title = element_text(hjust = 0.5)</li> </ul>

... • other arguments of the *theme* function, refer to ggplot2 manual

## Value

ggplot2 object

---

LoTTA_plot_outcome	<i>LoTTA_plot_outcome</i>
--------------------	---------------------------

---

## Description

Function that plots the median (or another quantile) of the LoTTA posterior outcome function along with the quantile-based credible interval. The function is plotted on top of the binned input data. To bin the data, the score data is divided into bins of fixed length, then the average outcome in each bin is calculated. The average outcomes are plotted against the average values of the score in the corresponding bins. The data is binned separately on each side of the cutoff, the cutoff is marked on the plot with a dotted line. In case of an unknown cutoff, the MAP estimate is used.

## Usage

```
LoTTA_plot_outcome(
  LoTTA_posterior,
  nbins = 100,
  probs = c(0.025, 0.5, 0.975),
  n_eval = 200,
  col_line = "#E69F00",
  size_line = 0.1,
  alpha_interval = 0.35,
  col_dots = "gray",
  size_dots = 3,
  alpha_dots = 0.6,
  col_cutoff = "black",
  title = "Outcome function",
  subtitle = NULL,
  y_lab = "",
  x_lab = expression(paste(italic("x"), " - score")),
  plot.theme = theme_classic(base_size = 14),
  legend.position = "none",
  name_legend = "Legend",
  labels_legend = "median outcome fun.",
  text = element_text(family = "serif"),
  legend.text = element_text(size = 14),
  plot.title = element_text(hjust = 0.5),
  plot.subtitle = element_text(hjust = 0.5),
  ...
)
```

**Arguments**

LoTTA_posterior	<ul style="list-style-type: none"> <li>output of one of the LoTTA functions (LoTTA_sharp_CONT, LoTTA_fuzzy_CONT, LoTTA_sharp_BIN, LoTTA_fuzzy_BIN) with all the parameters sampled (the default option in those functions)</li> </ul>
nbins	<ul style="list-style-type: none"> <li>number of bins to aggregate the input data</li> </ul>
probs	<ul style="list-style-type: none"> <li>list of three quantiles, the first and the last one define the quantile-based credible interval, the middle value defines the quantile of the posterior function to plot; by default the quantiles correspond to the median posterior function and 95% credible interval probs=c(0.025,0.5,0.975)</li> </ul>
n_eval	<ul style="list-style-type: none"> <li>n_eval*range(x) is the number of points at which each posterior function is evaluated, the higher number means slower computing time and a smoother plot; default n_eval=200</li> </ul>
col_line	<ul style="list-style-type: none"> <li>the color of the line and the band</li> </ul>
size_line	<ul style="list-style-type: none"> <li>thickness of the line</li> </ul>
alpha_interval	<ul style="list-style-type: none"> <li>alpha value of the band, lower values correspond to a more transparent color</li> </ul>
col_dots	<ul style="list-style-type: none"> <li>color of the dots that correspond to the binned data</li> </ul>
size_dots	<ul style="list-style-type: none"> <li>size of the dots that correspond to the binned data</li> </ul>
alpha_dots	<ul style="list-style-type: none"> <li>transparency of the dots that correspond to the binned data, lower values correspond to a more transparent color</li> </ul>
col_cutoff	<ul style="list-style-type: none"> <li>color of the dotted line at the cutoff</li> </ul>
title	<ul style="list-style-type: none"> <li>title of the plot</li> </ul>
subtitle	<ul style="list-style-type: none"> <li>subtitle of the plot</li> </ul>
y_lab	<ul style="list-style-type: none"> <li>label of the y-axis</li> </ul>
x_lab	<ul style="list-style-type: none"> <li>label of the x-axis</li> </ul>
plot.theme	<ul style="list-style-type: none"> <li>ggplot2 plot theme (see <a href="https://ggplot2.tidyverse.org/reference/ggtheme.html">https://ggplot2.tidyverse.org/reference/ggtheme.html</a>) possibly with additional arguments, it takes the default value plot.theme=theme_classic(base_size = 14),</li> </ul>
legend.position	<ul style="list-style-type: none"> <li>position of the legend, refer to ggplot2 manual for the possible values; by default legend is not printed legend.position='none'</li> </ul>
name_legend	<ul style="list-style-type: none"> <li>title of the legend</li> </ul>
labels_legend	<ul style="list-style-type: none"> <li>the label of the plotted function in the legend</li> </ul>
text	<ul style="list-style-type: none"> <li>can be any value that is accepted in the argument <i>text</i> in the <i>theme</i> function of ggplot2 package, refer to ggplot2 manual for the possible values; by default is changes font to a serif one text=element_text(family='serif')</li> </ul>
legend.text	<ul style="list-style-type: none"> <li>can be any value that is accepted in the argument <i>legend.text</i> in the <i>theme</i> function of ggplot2 package, refer to ggplot2 manual for the possible values; by default is changes font size to the legend to 14 legend.text=element_text(size = 14)</li> </ul>
plot.title	<ul style="list-style-type: none"> <li>can be any value that is accepted in the argument <i>plot.title</i> in the <i>theme</i> function of ggplot2 package, refer to ggplot2 manual for the possible values; by default it centers the plot title plot.title = element_text(hjust = 0.5)</li> </ul>

- `plot.subtitle` • can be any value that is accepted in the argument *plot.subtitle* in the *theme* function of *ggplot2* package, refer to *ggplot2* manual for the possible values; by default it centers the plot subtitle `plot.title = element_text(hjust = 0.5)`
- `...` • other arguments of the *theme* function, refer to *ggplot2* manual

## Value

*ggplot2* object

## Examples

```
# functions to generate the data

ilogit <- function(x) {
  return(1 / (1 + exp(-x)))
}

funB <- function(x) {
  y = x
  x2 = x[x >= 0]
  x1 = x[x < 0]
  y[x < 0] = 1 / (1 + exp(-2 * x1)) - 0.5 + 0.4
  y[x >= 0] = (log(x2 * 2 + 1) - 0.15 * x2^2) * 0.6 - 0.20 + 0.4
  return(y)
}

funB_sample <- function(x) {
  y = funB(x) + rnorm(length(x), 0, 0.1)
  return(y)
}

## Toy example - for the function check only! ##
# data generation
N=100
set.seed(1234)
x = sort(runif(N, -1, 1))
y = funB_sample(x)
c = 0

# running LoTTA function on sharp RDD with continuous outcomes;
out = LoTTA_sharp_CONT(x, y, c, normalize=FALSE, burnin = 100, sample = 100, adapt = 100,
n.chains=1, seed = NULL, method = 'simple', inits = NA)
# plot the outcome
LoTTA_plot_outcome(out, n_eval = 100)

## Use case example ##
# data generation
N=500 # try different dataset size
x = sort(runif(N, -1, 1))
y = funB_sample(x)
c = 0
# plot the data
plot(x, y)
```

```
# running LoTTA function on sharp RDD with continuous outcomes;
# cutoff = 0, treatment effect = -0.2
# remember to check convergence and adjust burnin, sample and adapt if needed
out = LoTTA_sharp_CONT(x, y, c, burnin = 10000, sample = 5000, adapt = 1000, n.chains=4)
# print effect estimate:
out$Effect_estimate
# print JAGS output to asses convergence (the output is for normalized data)
out$JAGS_output
# plot posterior fit
LoTTA_plot_outcome(out)
```

---

**LoTTA\_plot\_treatment**    *Function that plots the median (or another quantile) of the LoTTA posterior treatment probability function along with the quantile-based credible interval. The function is plotted on top of the binned input data. To bin the data, the score data is divided into bins of fixed length, then the proportion of treated is calculated in each bin. The proportions are plotted against the average values of the score in the corresponding bins. The data is binned separately on each side of the cutoff, the cutoff is marked on the plot with a dotted line. In case of an unknown cutoff, the MAP estimate is used.*

---

## Description

Function that plots the median (or another quantile) of the LoTTA posterior treatment probability function along with the quantile-based credible interval. The function is plotted on top of the binned input data. To bin the data, the score data is divided into bins of fixed length, then the proportion of treated is calculated in each bin. The proportions are plotted against the average values of the score in the corresponding bins. The data is binned separately on each side of the cutoff, the cutoff is marked on the plot with a dotted line. In case of an unknown cutoff, the MAP estimate is used.

## Usage

```
LoTTA_plot_treatment(
  LoTTA_posterior,
  nbins = 100,
  probs = c(0.025, 0.5, 0.975),
  n_eval = 200,
  col_line = "#E69F00",
  size_line = 0.1,
  alpha_interval = 0.35,
  col_dots = "gray",
  size_dots = 3,
  alpha_dots = 0.6,
  col_cutoff = "black",
  title = "Treatment probability function",
  subtitle = NULL,
```

```

y_lab = "",
x_lab = expression(paste(italic("x"), " - score")),
plot.theme = theme_classic(base_size = 14),
legend.position = "none",
name_legend = "Legend",
labels_legend = "median treatment prob. fun.",
text = element_text(family = "serif"),
legend.text = element_text(size = 14),
plot.title = element_text(hjust = 0.5),
plot.subtitle = element_text(hjust = 0.5),
...
)

```

## Arguments

LoTTA_posterior	<ul style="list-style-type: none"> <li>output of one of the LoTTA functions (LoTTA_fuzzy_CONT, LoTTA_fuzzy_BIN, LoTTA_treatment) with all the parameters sampled (the default option in those functions)</li> </ul>
nbins	<ul style="list-style-type: none"> <li>number of bins to aggregate the input data</li> </ul>
probs	<ul style="list-style-type: none"> <li>list of three quantiles, the first and the last one define the quantile-based credible interval, the middle value defines the quantile of the posterior function to plot; by default the quantiles correspond to the median posterior function and 95% credible interval probs=c(0.025,0.5,0.975)</li> </ul>
n_eval	<ul style="list-style-type: none"> <li>n_eval*range(x) is the number of points at which each posterior function is evaluated, the higher number means slower computing time and a smoother plot; default n_eval=200</li> </ul>
col_line	<ul style="list-style-type: none"> <li>the color of the line and the band</li> </ul>
size_line	<ul style="list-style-type: none"> <li>thickness of the line</li> </ul>
alpha_interval	<ul style="list-style-type: none"> <li>alpha value of the band, lower values correspond to a more transparent color</li> </ul>
col_dots	<ul style="list-style-type: none"> <li>color of the dots that correspond to the binned data</li> </ul>
size_dots	<ul style="list-style-type: none"> <li>size of the dots that correspond to the binned data</li> </ul>
alpha_dots	<ul style="list-style-type: none"> <li>transparency of the dots that correspond to the binned data, lower values correspond to a more transparent color</li> </ul>
col_cutoff	<ul style="list-style-type: none"> <li>color of the dotted line at the cutoff</li> </ul>
title	<ul style="list-style-type: none"> <li>title of the plot</li> </ul>
subtitle	<ul style="list-style-type: none"> <li>subtitle of the plot</li> </ul>
y_lab	<ul style="list-style-type: none"> <li>label of the y-axis</li> </ul>
x_lab	<ul style="list-style-type: none"> <li>label of the x-axis</li> </ul>
plot.theme	<ul style="list-style-type: none"> <li>ggplot2 plot theme (see <a href="https://ggplot2.tidyverse.org/reference/ggtheme.html">https://ggplot2.tidyverse.org/reference/ggtheme.html</a>) possibly with additional arguments, it takes the default value plot.theme=theme_classic(base_size = 14),</li> </ul>
legend.position	<ul style="list-style-type: none"> <li>position of the legend, refer to ggplot2 manual for the possible values; by default legend is not printed legend.position='none'</li> </ul>

name_legend	• title of the legend
labels_legend	• the label of the plotted function in the legend
text	• can be any value that is accepted in the argument <i>text</i> in the <i>theme</i> function of ggplot2 package, refer to ggplot2 manual for the possible values; by default is changes font to a serif one <code>text=element_text(family='serif')</code>
legend.text	• can be any value that is accepted in the argument <i>legend.text</i> in the <i>theme</i> function of ggplot2 package, refer to ggplot2 manual for the possible values; by default is changes font size to the legend to 14 <code>legend.text=element_text(size = 14)</code>
plot.title	• can be any value that is accepted in the argument <i>plot.title</i> in the <i>theme</i> function of ggplot2 package, refer to ggplot2 manual for the possible values; by default it centers the plot title <code>plot.title = element_text(hjust = 0.5)</code>
plot.subtitle	• can be any value that is accepted in the argument <i>plot.subtitle</i> in the <i>theme</i> function of ggplot2 package, refer to ggplot2 manual for the possible values; by default it centers the plot subtitle <code>plot.title = element_text(hjust = 0.5)</code>
...	• other arguments of the <i>theme</i> function, refer to ggplot2 manual

## Value

ggplot2 object

## Examples

```
# functions to generate the data

ilogit <- function(x) {
  return(1 / (1 + exp(-x)))
}

fun_prob55 <- function(x) {
  P = rep(0, length(x))
  P[x >= 0.] = ilogit((8.5 * x[x >= 0.] - 1.5)) / 10.5 + 0.65 - 0.0007072
  P[x < 0.] = (x[x < 0.] + 1)^4 / 15 + 0.05
  return(P)
}

sample_prob55 <- function(x) {
  P = rep(0, length(x))
  P[x >= 0.] = ilogit((8.5 * x[x >= 0.] - 1.5)) / 10.5 + 0.65 - 0.0007072
  P[x < 0.] = (x[x < 0.] + 1)^4 / 15 + 0.05
  t = rep(0, length(x))
  for (j in 1:length(x)) {
    t[j] = sample(c(1, 0), 1, prob = c(P[j], 1 - P[j]))
  }
  return(t)
}
```



```

## Toy example - for the function check only! ##
N=100
x = sort(runif(N, -1, 1))
t = sample_prob55(x)
c_prior=0 # known cutoff

# running LoTTA treatment-only model;
out = LoTTA_treatment(x,t,c_prior,burnin = 50, sample = 50, adapt = 10,n.chains=1
                      ,method = 'simple',inits = NA)
# plot posterior fit of the treatment probability function
LoTTA_plot_treatment(out,nbins = 60)

## Use case example ##

N=500
x = sort(runif(N, -1, 1))
t = sample_prob55(x)

# comment out to try different priors:
c_prior=list(clb=-0.25,cub=0.25) # uniform prior on the interval [-0.25,0.25]
# c_prior=list(cstart=-0.25,cend=0.25,grid=0.05) # uniform discrete prior
# on -0.25, -0.2, ..., 0.25
# c_prior=0 # known cutoff c=0

# running LoTTA treatment-only model;
# cutoff = 0, compliance rate = 0.55
# remember to check convergence and adjust burnin, sample and adapt if needed
out = LoTTA_treatment(x,t,c_prior,burnin = 10000,sample = 5000,adapt=1000)

# print effect estimate:
out$Effect_estimate
# print JAGS output to assess convergence (the output is for normalized data)
out$JAGS_output
# plot posterior fit of the treatment probability function
LoTTA_plot_treatment(out,nbins = 60)

```

---

LoTTA\_sharp\_BIN

*LoTTA\_sharp\_BIN*


---

## Description

Function that fits LoTTA model to the sharp RD data with binary outcomes. The score does NOT have to be normalized beforehand. We recommend NOT to transform the data before imputing it into the function, except for initial trimming of the score which should be done beforehand. The further trimming for the sensitivity analysis can be done through the function, which ensures that the data is normalized before the trimming.

**Usage**

```

LoTTA_sharp_BIN(
  x,
  y,
  c,
  ci = 0.95,
  trimmed = NULL,
  outcome_prior = list(pr = 1e-04),
  n_min = 25,
  param = c("eff", "a0l", "a1l", "a2l", "a3l", "a0r", "a1r", "a2r", "a3r", "kl", "kr"),
  normalize = TRUE,
  n.chains = 4,
  burnin = 5000,
  sample = 5000,
  adapt = 1000,
  inits = NULL,
  method = "parallel",
  seed = NULL,
  ...
)

```

**Arguments**

x	• is the score data
y	• is the binary outcome data
c	• specifies the cutoff point
ci	• specifies the probability level $1-\alpha$ for the highest posterior density intervals; default is $ci = 0.95$
trimmed	• takes as a value NULL or a vector of two values. It specifies potential trimming of the data. If set to NULL no trimming is applied to the data. If a list of two values is provided the data is trimmed to include data points with the score x in between those values; default is <code>trimmed=NULL</code>
outcome_prior	• takes as a value a list with elements 'pr'. 'pr' specifies precision in the normal priors on the coefficients in the outcome function; default is <code>list('pr'=0.0001)</code>
n_min	• specifies the minimum number of data points to which a cubic part of the outcome function is fit to ensure stability of the sampling procedure; default is <code>n_min=25</code>
param	• takes as a value a vector with names of the parameters that are to be sampled; default is the list of all parameters
normalize	• specifies if the data is to be normalized. The data is normalized as follows. $x_{\text{normalized}} = (x-d)/s$ , where $d = (\min(x) + \max(x)) * 0.5$ and $s = \max(x) - \min(x)$ . The priors inside the model are specified for the normalized data, in extreme cases not normalizing the data may lead to unreliable results; default is <code>normalize=TRUE</code>
n.chains	• specifies the number of chains in the MCMC sampler; default is <code>n.chains=4</code>

burnin	<ul style="list-style-type: none"> <li>specifies the number of burnin iterations without the adaptive iterations; default is burnin=5000</li> </ul>
sample	<ul style="list-style-type: none"> <li>specifies the number of samples per chain; default is samples=5000</li> </ul>
adapt	<ul style="list-style-type: none"> <li>specifies the number of adaptive iterations in the MCMC sampler; default is adapt=1000</li> </ul>
inits	<ul style="list-style-type: none"> <li>initial values for the sampler. By default the initial values are sampled inside the function. To run LoTTA with a method other than "parallel" inits must be set to NA or to a user defined value. If the user wants to provide its own values please refer to run.jags manual; default inits=NULL</li> </ul>
method	<ul style="list-style-type: none"> <li>set to default as 'parallel', which allows to sample the chains in parallel reducing computation time. To read more about possible method values type ?run.jags; default method='parallel'</li> </ul>
seed	<ul style="list-style-type: none"> <li>specifies the seed for replicability purposes; default is seed=NULL</li> </ul>
...	<ul style="list-style-type: none"> <li>other arguments of run.jags function. For more details type ?run.jags</li> </ul>

## Value

The function returns the list with the elements:

- Effect\_estimate: contains a list with MAP estimate and HDI of the treatment effect on the original, unnormalized scale;
- JAGS\_output: contains output of the run.jags function for the normalized data if normalize=TRUE, based on this output mixing of the chains can be assessed;
- Samples: contains posterior samples of the treatment effect (eff);
- Normalized\_data: contains a list of the normalized data (if normalized=TRUE) and the parameters used to normalize the data (see arg normalize);
- Priors: contains a list of the outcome prior parameters ;
- Inits contains the list of initial values and .RNG.seed value

## Examples

```
# functions to generate the data

ilogit <- function(x) {
  return(1 / (1 + exp(-x)))
}

fun_prob55 <- function(x) {
  P = rep(0, length(x))
  P[x >= 0.] = ilogit((8.5 * x[x >= 0.] - 1.5)) / 10.5 + 0.65 - 0.0007072
  P[x < 0.] = (x[x < 0.] + 1)^4 / 15 + 0.05
  return(P)
}

sample_prob55 <- function(x) {
  P = rep(0, length(x))
  P[x >= 0.] = ilogit((8.5 * x[x >= 0.] - 1.5)) / 10.5 + 0.65 - 0.0007072
```

```

P[x < 0.] = (x[x < 0.] + 1)^4 / 15 + 0.05
t = rep(0, length(x))
for (j in 1:length(x)) {
  t[j] = sample(c(1, 0), 1, prob = c(P[j], 1 - P[j]))
}
return(t)
}

## Toy example - for the function check only! ##
# data generation
N=100
x = sort(runif(N, -1, 1))
y = sample_prob55(x)
c = 0

# running LoTTA model on a sharp RDD with a binary outcome
out = LoTTA_sharp_BIN(x, y, c, burnin = 50, sample = 50, adapt = 10, n.chains=1
,method = 'simple', inits = NA)

## Use case example ##

# data generation
N=1000 # try different dataset size
x = sort(runif(N, -1, 1))
y = sample_prob55(x)
c = 0

# running LoTTA function on sharp RDD with binary outcomes;
# cutoff = 0, treatment effect = 0.55
# remember to check convergence and adjust burnin, sample and adapt if needed
out = LoTTA_sharp_BIN(x, y, c, burnin = 10000, sample = 5000, adapt = 1000, n.chains=4)
# print effect estimate:
out$Effect_estimate
# print JAGS output to asses convergence (the output is for normalized data)
out$JAGS_output
# plot posterior fit
LoTTA_plot_outcome(out, nbins = 60)

```

---

LoTTA\_sharp\_CONT

LoTTA\_sharp\_CONT

---

## Description

Function that fits LoTTA model to the sharp RD data with continuous outcomes. The data does NOT have to be normalized beforehand. We recommend NOT to transform the data before imputing it into the function, except for initial trimming which should be done beforehand. The further trimming for the sensitivity analysis can be done through the function, which ensures that the data is normalized before the trimming.

**Usage**

```

LoTTA_sharp_CONT(
  x,
  y,
  c,
  ci = 0.95,
  trimmed = NULL,
  outcome_prior = list(pr = 1e-04, shape = 0.01, scale = 0.01),
  n_min = 25,
  param = c("eff", "a0l", "a1l", "a2l", "a3l", "a0r", "a1r", "a2r", "a3r", "tau1r",
    "tau2r", "tau1l", "tau2l", "k1", "kr"),
  normalize = TRUE,
  n.chains = 4,
  burnin = 10000,
  sample = 5000,
  adapt = 1000,
  inits = NULL,
  method = "parallel",
  seed = NULL,
  ...
)

```

**Arguments**

- |               |  |
|---------------|--|
| x             | • is the score data  |
| y             | • is the continuous outcome data   |
| c             | • specifies the cutoff point   |
| ci            | • specifies the probability level 1-alpha for the highest posterior density intervals; default is ci = 0.95  |
| trimmed       | • takes as a value NULL or a vector of two values. It specifies potential trimming of the data. If set to NULL no trimming is applied to the data. If a list of two values is provided the data is trimmed to include data points with the score x in between those values; default is trimmed=NULL  |
| outcome_prior | • takes as a value a list with elements 'pr' and 'shape', 'scale'. 'pr' specifies precision in the normal priors on the coefficients in the outcome function. 'shape' and 'scale' specify the shape and scale parameters in the gamma prior on the precision of the error terms; default is list('pr'= 0.0001, 'shape'= 0.01, 'scale'= 0.01) |
| n_min         | • specifies the minimum number of data points to which a cubic part of the outcome function is fit to ensure stability of the sampling procedure; default is n_min=25  |
| param         | • takes as a value a vector with names of the parameters that are to be sampled; default is the list of all parameters   |
| normalize     | • specifies if the data is to be normalized. The data is normalized as follows. $x\_normalized = (x - d) / s$ , where $d = (\min(x) + \max(x)) * 0.5$ and $s = \max(x) - \min(x)$ . $y\_normalized = (y - \mu) / sd$ , where $\mu = \text{mean}(y)$ and $sd = \text{sd}(y)$ . The  |

	priors inside the model are specified for the normalized data, in extreme cases not normalizing the data may lead to unreliable results; default is <code>normalize=TRUE</code>
<code>n.chains</code>	• specifies the number of chains in the MCMC sampler; default is <code>n.chains=4</code>
<code>burnin</code>	• specifies the number of burnin iterations without the adaptive iterations; default is <code>burnin=5000</code>
<code>sample</code>	• specifies the number of samples per chain; default is <code>samples=5000</code>
<code>adapt</code>	• specifies the number of adaptive iterations in the MCMC sampler; default is <code>adapt=1000</code>
<code>inits</code>	• initial values for the sampler. By default the initial values are sampled inside the function. To run LoTTA with a method other than "parallel" <code>inits</code> must be set to NA or to a user defined value. If the user wants to provide its own values please refer to <code>run.jags</code> manual; default <code>inits=NULL</code>
<code>method</code>	• set to default as 'parallel', which allows to sample the chains in parallel reducing computation time. To read more about possible method values type <code>?run.jags</code> ; default <code>method='parallel'</code>
<code>seed</code>	• specifies the seed for replicability purposes; default is <code>seed=NULL</code>
<code>...</code>	• other arguments of <code>run.jags</code> function. For more details type <code>?run.jags</code>

## Value

The function returns the list with the elements:

- `Effect_estimate`: contains a list with MAP estimate and HDI of the treatment effect on the original, unnormalized scale;
- `JAGS_output`: contains output of the `run.jags` function for the normalized data if `normalize=TRUE`, based on this output mixing of the chains can be assessed;
- `Samples`: contains posterior samples of the treatment effect (`eff`);
- `Normalized_data`: contains a list of the normalized data (if `normalized=TRUE`) and the parameters used to normalize the data (see arg `normalize`);
- `Priors`: contains a list of the outcome prior parameters ;
- `Init`s contains the list of initial values and `.RNG.seed` value

## Examples

```
# functions to generate the data

ilogit <- function(x) {
  return(1 / (1 + exp(-x)))
}

funB <- function(x) {
  y = x
  x2 = x[x >= 0]
  x1 = x[x < 0]
  y[x < 0] = 1 / (1 + exp(-2 * x1)) - 0.5 + 0.4
}
```

```

    y[x >= 0] = (log(x2 * 2 + 1) - 0.15 * x2^2) * 0.6 - 0.20 + 0.4
    return(y)
}

funB_sample <- function(x) {
  y = funB(x)+ rnorm(length(x), 0, 0.1)
  return(y)
}

## Toy example - for the function check only! ##
# data generation
N=100
set.seed(1234)
x = sort(runif(N, -1, 1))
y = funB_sample(x)
c = 0

# running LoTTA function on sharp RDD with continuous outcomes;
out = LoTTA_sharp_CONT(x, y, c, normalize=FALSE, burnin = 50, sample = 50, adapt = 10,
n.chains=1, seed = NULL, method = 'simple', inits = NA)

## Use case example ##
# data generation
N=500 # try different dataset size
x = sort(runif(N, -1, 1))
y = funB_sample(x)
c = 0
# plot the data
plot(x,y)
# running LoTTA function on sharp RDD with continuous outcomes;
# cutoff = 0, treatment effect = -0.2
# remember to check convergence and adjust burnin, sample and adapt if needed
out = LoTTA_sharp_CONT(x, y, c, burnin = 10000, sample = 5000, adapt = 1000, n.chains=4)
# print effect estimate:
out$Effect_estimate
# print JAGS output to asses convergence (the output is for normalized data)
out$JAGS_output
# plot posterior fit
LoTTA_plot_outcome(out)

```

---

LoTTA\_treatment

LoTTA\_treatment

---

## Description

Function that fits LoTTA treatment model to the fuzzy RD treatment data with an either known or unknown/suspected cutoff. It supports two types of priors on the cutoff location: a scaled beta distribution of the form  $\text{beta}(\alpha, \beta)(\text{cub} - \text{clb}) + \text{clb}$  and a discrete distribution with the support of the form  $\text{cstart} + \text{grid } i$  for  $i=0, \dots, (\text{cend} - \text{cstart})/\text{grid}$ . The score does NOT have to be normalized beforehand. We recommend NOT to transform the data before imputing it into the function, except

for initial trimming of the score which should be done beforehand. The further trimming for the sensitivity analysis can be done through the function, which ensures that the data is normalized before the trimming.

### Usage

```
LoTTA_treatment(
  x,
  t,
  c_prior,
  jlb = 0.2,
  ci = 0.95,
  trimmed = NULL,
  n_min = 25,
  param = c("c", "j", "b1lt", "a1lt", "a2lt", "b2lt", "b1rt", "a1rt", "a2rt", "b2rt",
    "k1t", "k2t"),
  normalize = TRUE,
  n.chains = 4,
  burnin = 5000,
  sample = 1000,
  adapt = 500,
  inits = NULL,
  method = "parallel",
  seed = NULL,
  ...
)
```

### Arguments

<code>x</code>	• is the score data
<code>t</code>	• is the treatment allocation data
<code>c_prior</code>	• specifies the cutoff prior in case of the unknown cutoff or the cutoff point if the cutoff is known. Takes as value a number if the cutoff is known or a list of values otherwise. For a continuous prior the list requires the following elements: <code>clb</code> - left end of the interval <code>cub</code> - right end of the interval in which the scaled and translated beta distribution is defined, <code>alpha</code> (optional) - shape parameter, default value = 1, <code>beta</code> (optional) - shape parameter, default value = 1. For a discrete prior the list requires the following elements: <code>cstart</code> - first point with positive prior mass, <code>cend</code> - last point with positive prior mass, <code>grid</code> - distance between the consecutive points in the support weights (optional) - vector of weights assigned to each point in the support, default is vector of 1's (uniform distribution)
<code>jlb</code>	• minimum jump size
<code>ci</code>	• specifies the probability level $1-\alpha$ for the highest posterior density intervals; default is <code>ci = 0.95</code>
<code>trimmed</code>	• takes as a value <code>NULL</code> or a vector of two values. It specifies potential trimming of the data. If set to <code>NULL</code> no trimming is applied to the data. If



	a list of two values is provided the data is trimmed to include data points with the score $x$ in between those values; default is <code>trimmed=NULL</code>
<code>n_min</code>	<ul style="list-style-type: none"> <li>specifies the minimum number of data points to which a cubic part of the outcome function is fit to ensure stability of the sampling procedure; default is <code>n_min=25</code></li> </ul>
<code>param</code>	<ul style="list-style-type: none"> <li>takes as a value a vector with names of the parameters that are to be sampled; default is the list of all parameters</li> </ul>
<code>normalize</code>	<ul style="list-style-type: none"> <li>specifies if the data is to be normalized. The data is normalized as follows. If the prior is continuous: <math>x_{\text{normalized}}=(x-d)/s</math>, where <math>d=(\min(x)+\max(x))*0.5</math> and <math>s=\max(x)-\min(x)</math>, If the prior is discrete: <math>x_{\text{normalized}}=x/s</math>, where <math>s=10^m</math>, where <math>m</math> is chosen so that <math>l\max(\text{abs}(x))-1l</math> is minimal. The outcome data is normalized as follows: <math>y_{\text{normalized}}=(y-\mu)/sd</math>, where <math>\mu=\text{mean}(y)</math> and <math>sd=\text{sd}(y)</math>. The priors inside the model are specified for the normalized data, in extreme cases not normalizing the data may lead to unreliable results; default is <code>normalize=TRUE</code></li> </ul>
<code>n.chains</code>	<ul style="list-style-type: none"> <li>specifies the number of chains in the MCMC sampler; default is <code>n.chains=4</code></li> </ul>
<code>burnin</code>	<ul style="list-style-type: none"> <li>specifies the number of burnin iterations without the adaptive iterations; default is <code>burnin=5000</code></li> </ul>
<code>sample</code>	<ul style="list-style-type: none"> <li>specifies the number of samples per chain; default is <code>samples=5000</code></li> </ul>
<code>adapt</code>	<ul style="list-style-type: none"> <li>specifies the number of adaptive iterations in the MCMC sampler; default is <code>adapt=1000</code></li> </ul>
<code>inits</code>	<ul style="list-style-type: none"> <li>initial values for the sampler. By default the initial values are sampled inside the function. To run LoTTA with a method other than "parallel" <code>inits</code> must be set to NA or to a user defined value. If the user wants to provide its own values please refer to <code>run.jags</code> manual; default <code>inits=NULL</code></li> </ul>
<code>method</code>	<ul style="list-style-type: none"> <li>set to default as 'parallel', which allows to sample the chains in parallel reducing computation time. To read more about possible method values type <code>?run.jags</code>; default <code>method='parallel'</code></li> </ul>
<code>seed</code>	<ul style="list-style-type: none"> <li>specifies the seed for replicability purposes; default is <code>seed=NULL</code></li> </ul>
<code>...</code>	<ul style="list-style-type: none"> <li>other arguments of <code>run.jags</code> function. For more details type <code>?run.jags</code></li> </ul>

## Value

The function returns the list with the elements:

- `Effect_estimate`: contains a list with MAP estimate and HDI of the cutoff location (if unknown) and the discontinuity size in the treatment probability function (compliance rate at  $c$ ) on the original, unnormalized scale;
- `JAGS_output`: contains output of the `run.jags` function for the normalized data if `normalize=TRUE`, based on this output mixing of the chains can be assessed;
- `Samples`: contains posterior samples of the cutoff location ( $c$ ) if unknown, and compliance rate ( $j$ );
- `Normalized_data`: contains a list of the normalized data (if `normalize=TRUE`) and the parameters used to normalize the data (see arg `normalize`);
- `Priors`: contains a list of the priors' parameters ;
- `Inits` contains the list of initial values and `.RNG.seed` value

## Examples

```
# functions to generate the data

ilogit <- function(x) {
  return(1 / (1 + exp(-x)))
}

fun_prob55 <- function(x) {
  P = rep(0, length(x))
  P[x >= 0.] = ilogit((8.5 * x[x >= 0.] - 1.5)) / 10.5 + 0.65 - 0.0007072
  P[x < 0.] = (x[x < 0.] + 1)^4 / 15 + 0.05
  return(P)
}

sample_prob55 <- function(x) {
  P = rep(0, length(x))
  P[x >= 0.] = ilogit((8.5 * x[x >= 0.] - 1.5)) / 10.5 + 0.65 - 0.0007072
  P[x < 0.] = (x[x < 0.] + 1)^4 / 15 + 0.05
  t = rep(0, length(x))
  for (j in 1:length(x)) {
    t[j] = sample(c(1, 0), 1, prob = c(P[j], 1 - P[j]))
  }
  return(t)
}

## Toy example - for the function check only! ##
N=100
x = sort(runif(N, -1, 1))
t = sample_prob55(x)
c_prior=0 # known cutoff

# running LoTTA treatment-only model;
out = LoTTA_treatment(x,t,c_prior,burnin = 50, sample = 50, adapt = 10,n.chains=1
                      ,method = 'simple',inits = NA)

## Use case example ##

N=500
x = sort(runif(N, -1, 1))
t = sample_prob55(x)

# comment out to try different priors:
c_prior=list(clb=-0.25,cub=0.25) # uniform prior on the interval [-0.25,0.25]
# c_prior=list(cstart=-0.25,cend=0.25,grid=0.05) # uniform discrete prior
# on -0.25, -0.2, ..., 0.25
# c_prior=0 # known cutoff c=0

# running LoTTA treatment-only model;
# cutoff = 0, compliance rate = 0.55
# remember to check convergence and adjust burnin, sample and adapt if needed
```

```

out = LoTTA_treatment(x,t,c_prior,burnin = 10000,sample = 5000,adapt=1000)

# print effect estimate:
out$Effect_estimate
# print JAGS output to asses convergence (the output is for normalized data)
out$JAGS_output
# plot posterior fit of the treatment probablity function
LoTTA_plot_treatment(out,nbins = 60)

```

---

normalize_cont_x	<i>normalize continuous score function</i>
------------------	--

---

### Description

normalize continuous score function

### Usage

```
normalize_cont_x(x, trimmed = NULL, normalize = TRUE)
```

### Arguments

x	• score data
trimmed	• NULL by default, provide vector of score values to trim the data
normalize	• whether data is to be normalized

### Value

list with x - normalized score, d - parameter used to shift the score

---

normalize_cont_y	<i>normalize continuous outcome function</i>
------------------	--

---

### Description

normalize continuous outcome function

### Usage

```
normalize_cont_y(y, x, trimmed = NULL, normalize = TRUE)
```

**Arguments**

y	• outcome data
x	• score data
trimmed	• NULL by default, provide vector of values to trim the data
normalize	• whether data is to be normalized

**Value**

list with y - normalized outcome, mu - shift parameter, sd - scaling parameter

---

normalize_dis_x	<i>normalize discrete score function</i>
-----------------	--

---

**Description**

normalize discrete score function

**Usage**

```
normalize_dis_x(x, trimmed = NULL, normalize = TRUE)
```

**Arguments**

x	score data
trimmed	• NULL by default, provide vector of values to trim the data
normalize	• TRUE by default, whether data is to be normalized

**Value**

list with x - normalized score, s - parameter used to scale the score

---

optimal_k	<i>function that searches for initial parameters of outcome function to initiate the sampler</i>
-----------	--

---

**Description**

function that searches for initial parameters of outcome function to initiate the sampler

**Usage**

```
optimal_k(x, y, c, lb, ubr, ubl)
```

**Arguments**

- |     |  |
|-----|--|
| x   | • score data   |
| y   | • outcome data                                       |
| c   | • cutoff   |
| lb  | • minimum window size                                |
| ubr | • maximum value of the window's right boundary point |
| ubl | • minimum value of the window's left boundary point  |

**Value**

- a list with kl and kr and cubic functions parameters

---

optimal_k_bin	<i>function that searches for initial parameters of binary outcome function to initiate the sampler</i>
---------------	---

---

**Description**

function that searches for initial parameters of binary outcome function to initiate the sampler

**Usage**

```
optimal_k_bin(x, y, c, lb, ubr, ubl)
```

**Arguments**

- |     |  |
|-----|--|
| x   | • score data   |
| y   | • outcome data                                       |
| c   | • cutoff   |
| lb  | • minimum window size                                |
| ubr | • maximum value of the window's right boundary point |
| ubl | • minimum value of the window's left boundary point  |

**Value**

- a list with kl and kr and cubic functions parameters

---

plot_outcome_BIN	<i>Function that plots the median (or another quantile) of the posterior function with binary outcome along with the quantile-based credible interval. The function is plotted on top of the binned input data. To bin the data, the score data is divided into bins of fixed length, then the average outcome in each bin is calculated. The average outcomes are plotted against the average values of the score in the corresponding bins.</i>
------------------	---

---

## Description

Function that plots the median (or another quantile) of the posterior function with binary outcome along with the quantile-based credible interval. The function is plotted on top of the binned input data. To bin the data, the score data is divided into bins of fixed length, then the average outcome in each bin is calculated. The average outcomes are plotted against the average values of the score in the corresponding bins.

## Usage

```
plot_outcome_BIN(
  LoTTA_posterior,
  nbins = 100,
  probs = c(0.025, 0.5, 0.975),
  n_eval = 200,
  col_line = "#E69F00",
  size_line = 0.1,
  alpha_interval = 0.35,
  col_dots = "gray",
  size_dots = 3,
  alpha_dots = 0.6,
  col_cutoff = "black",
  title = "Outcome function",
  subtitle = NULL,
  y_lab = "",
  x_lab = expression(paste(italic("x"), " - score")),
  plot.theme = theme_classic(base_size = 14),
  legend.position = "none",
  name_legend = "Legend",
  labels_legend = "median outcome fun.",
  text = element_text(family = "serif"),
  legend.text = element_text(size = 14),
  plot.title = element_text(hjust = 0.5),
  plot.subtitle = element_text(hjust = 0.5),
  ...
)
```

**Arguments**

LoTTA_posterior	<ul style="list-style-type: none"> <li>• output of one of the LoTTA functions (LoTTA_sharp, LoTTA_fuzzy)</li> </ul>
nbins	<ul style="list-style-type: none"> <li>• number of bins to aggregate the input data</li> </ul>
probs	<ul style="list-style-type: none"> <li>• list of three quantiles, the first and the last one define the quantile-based credible interval, the middle value defines the quantile of the posterior function to plot; by default the quantiles correspond to the median posterior function and 95% credible interval probs=c(0.025,0.5,0.975)</li> </ul>
n_eval	<ul style="list-style-type: none"> <li>• <math>n\_eval \times \text{range}(x)</math> is the number of points at which each posterior function is evaluated, the higher number means slower computing time and a smoother plot; default n_eval=200</li> </ul>
col_line	<ul style="list-style-type: none"> <li>• the color of the line and the band</li> </ul>
size_line	<ul style="list-style-type: none"> <li>• thickness of the line</li> </ul>
alpha_interval	<ul style="list-style-type: none"> <li>• alpha value of the band, lower values correspond to a more transparent color</li> </ul>
col_dots	<ul style="list-style-type: none"> <li>• color of the dots that correspond to the binned data</li> </ul>
size_dots	<ul style="list-style-type: none"> <li>• size of the dots that correspond to the binned data</li> </ul>
alpha_dots	<ul style="list-style-type: none"> <li>• transparency of the dots that correspond to the binned data, lower values correspond to a more transparent color</li> </ul>
col_cutoff	<ul style="list-style-type: none"> <li>• color of the dotted line at the cutoff</li> </ul>
title	<ul style="list-style-type: none"> <li>• title of the plot</li> </ul>
subtitle	<ul style="list-style-type: none"> <li>• subtitle of the plot</li> </ul>
y_lab	<ul style="list-style-type: none"> <li>• label of the y-axis</li> </ul>
x_lab	<ul style="list-style-type: none"> <li>• label of the x-axis</li> </ul>
plot.theme	<ul style="list-style-type: none"> <li>• ggplot2 plot theme (see <a href="https://ggplot2.tidyverse.org/reference/ggtheme.html">https://ggplot2.tidyverse.org/reference/ggtheme.html</a>) possibly with additional arguments, it takes the default value plot.theme=theme_classic(base_size = 14),</li> </ul>
legend.position	<ul style="list-style-type: none"> <li>• position of the legend, refer to ggplot2 manual for the possible values; by default legend is not printed legend.position='none'</li> </ul>
name_legend	<ul style="list-style-type: none"> <li>• title of the legend</li> </ul>
labels_legend	<ul style="list-style-type: none"> <li>• the label of the plotted function in the legend</li> </ul>
text	<ul style="list-style-type: none"> <li>• can be any value that is accepted in the argument <i>text</i> in the <i>theme</i> function of ggplot2 package, refer to ggplot2 manual for the possible values; by default is changes font to a serif one text=element_text(family='serif')</li> </ul>
legend.text	<ul style="list-style-type: none"> <li>• can be any value that is accepted in the argument <i>legend.text</i> in the <i>theme</i> function of ggplot2 package, refer to ggplot2 manual for the possible values; by default is changes font size to the legend to 14 legend.text=element_text(size = 14)</li> </ul>
plot.title	<ul style="list-style-type: none"> <li>• can be any value that is accepted in the argument <i>plot.title</i> in the <i>theme</i> function of ggplot2 package, refer to ggplot2 manual for the possible values; by default it centers the plot title plot.title = element_text(hjust = 0.5)</li> </ul>

- `plot.subtitle` can be any value that is accepted in the argument `plot.subtitle` in the `theme` function of `ggplot2` package, refer to `ggplot2` manual for the possible values; by default it centers the plot subtitle `plot.title = element_text(hjust = 0.5)`
- `...` other arguments of the `theme` function, refer to `ggplot2` manual

### Value

`ggplot2` object

---

<code>plot_outcome_CONT</code>	<i>Function that plots the median (or another quantile) of the posterior function of a continuous outcome along with the quantile-based credible interval. The function is plotted on top of the binned input data. To bin the data, the score data is divided into bins of fixed length, then the average outcome in each bin is calculated. The average outcomes are plotted against the average values of the score in the corresponding bins.</i>
--------------------------------	---

---

### Description

Function that plots the median (or another quantile) of the posterior function of a continuous outcome along with the quantile-based credible interval. The function is plotted on top of the binned input data. To bin the data, the score data is divided into bins of fixed length, then the average outcome in each bin is calculated. The average outcomes are plotted against the average values of the score in the corresponding bins.

### Usage

```
plot_outcome_CONT(
  LoTTA_posterior,
  nbins = 100,
  probs = c(0.025, 0.5, 0.975),
  n_eval = 200,
  col_line = "#E69F00",
  size_line = 0.1,
  alpha_interval = 0.35,
  col_dots = "gray",
  size_dots = 3,
  alpha_dots = 0.6,
  col_cutoff = "black",
  title = "Outcome function",
  subtitle = NULL,
  y_lab = "",
  x_lab = expression(paste(italic("x"), " - score")),
  plot.theme = theme_classic(base_size = 14),
  legend.position = "none",
  name_legend = "Legend",
```



```

    labels_legend = "median outcome fun.",
    text = element_text(family = "serif"),
    legend.text = element_text(size = 14),
    plot.title = element_text(hjust = 0.5),
    plot.subtitle = element_text(hjust = 0.5),
    ...
)

```

## Arguments

LoTTA_posterior	<ul style="list-style-type: none"> <li>• output of one of the LoTTA functions (LoTTA_sharp, LoTTA_fuzzy)</li> </ul>
nbins	<ul style="list-style-type: none"> <li>• number of bins to aggregate the input data</li> </ul>
probs	<ul style="list-style-type: none"> <li>• list of three quantiles, the first and the last one define the quantile-based credible interval, the middle value defines the quantile of the posterior function to plot; by default the quantiles correspond to the median posterior function and 95% credible interval probs=c(0.025,0.5,0.975)</li> </ul>
n_eval	<ul style="list-style-type: none"> <li>• n_eval*range(x) is the number of points at which each posterior function is evaluated, the higher number means slower computing time and a smoother plot; default n_eval=200</li> </ul>
col_line	<ul style="list-style-type: none"> <li>• the color of the line and the band</li> </ul>
size_line	<ul style="list-style-type: none"> <li>• thickness of the line</li> </ul>
alpha_interval	<ul style="list-style-type: none"> <li>• alpha value of the band, lower values correspond to a more transparent color</li> </ul>
col_dots	<ul style="list-style-type: none"> <li>• color of the dots that correspond to the binned data</li> </ul>
size_dots	<ul style="list-style-type: none"> <li>• size of the dots that correspond to the binned data</li> </ul>
alpha_dots	<ul style="list-style-type: none"> <li>• transparency of the dots that correspond to the binned data, lower values correspond to a more transparent color</li> </ul>
col_cutoff	<ul style="list-style-type: none"> <li>• color of the dotted line at the cutoff</li> </ul>
title	<ul style="list-style-type: none"> <li>• title of the plot</li> </ul>
subtitle	<ul style="list-style-type: none"> <li>• subtitle of the plot</li> </ul>
y_lab	<ul style="list-style-type: none"> <li>• label of the y-axis</li> </ul>
x_lab	<ul style="list-style-type: none"> <li>• label of the x-axis</li> </ul>
plot.theme	<ul style="list-style-type: none"> <li>• ggplot2 plot theme (see <a href="https://ggplot2.tidyverse.org/reference/ggtheme.html">https://ggplot2.tidyverse.org/reference/ggtheme.html</a>) possibly with additional arguments, it takes the default value plot.theme=theme_classic(base_size = 14),</li> </ul>
legend.position	<ul style="list-style-type: none"> <li>• position of the legend, refer to ggplot2 manual for the possible values; by default legend is not printed legend.position='none'</li> </ul>
name_legend	<ul style="list-style-type: none"> <li>• title of the legend</li> </ul>
labels_legend	<ul style="list-style-type: none"> <li>• the label of the plotted function in the legend</li> </ul>
text	<ul style="list-style-type: none"> <li>• can be any value that is accepted in the argument <i>text</i> in the <i>theme</i> function of ggplot2 package, refer to ggplot2 manual for the possible values; by default is changes font to a serif one text=element_text(family='serif')</li> </ul>

legend.text	<ul style="list-style-type: none"> <li>can be any value that is accepted in the argument <i>legend.text</i> in the <i>theme</i> function of ggplot2 package, refer to ggplot2 manual for the possible values; by default is changes font size to the legend to 14 legend.text=element_text(size = 14)</li> </ul>
plot.title	<ul style="list-style-type: none"> <li>can be any value that is accepted in the argument <i>plot.title</i> in the <i>theme</i> function of ggplot2 package, refer to ggplot2 manual for the possible values; by default it centers the plot title plot.title = element_text(hjust = 0.5)</li> </ul>
plot.subtitle	<ul style="list-style-type: none"> <li>can be any value that is accepted in the argument <i>plot.subtitle</i> in the <i>theme</i> function of ggplot2 package, refer to ggplot2 manual for the possible values; by default it centers the plot subtitle plot.title = element_text(hjust = 0.5)</li> </ul>
...	<ul style="list-style-type: none"> <li>other arguments of the <i>theme</i> function, refer to ggplot2 manual</li> </ul>

**Value**

ggplot2 object

---

read_prior	<i>function that checks the type of a prior and whether it is correct</i>
------------	---

---

**Description**

function that checks the type of a prior and whether it is correct

**Usage**

```
read_prior(prior, minx, maxx, ubl, ubr, lb)
```

**Arguments**

prior	<ul style="list-style-type: none"> <li>list with prior parameters or a cutoff value</li> </ul>
minx	<ul style="list-style-type: none"> <li>minimum value of the score</li> </ul>
maxx	<ul style="list-style-type: none"> <li>maximum value of the score</li> </ul>
ubl	<ul style="list-style-type: none"> <li>minimum value of the window's left boundary point</li> </ul>
ubr	<ul style="list-style-type: none"> <li>maximum value of the window's right boundary point</li> </ul>
lb	<ul style="list-style-type: none"> <li>minimum window size</li> </ul>

**Value**

list with type of prior and prior parameters

---

`treatment_function_sample`

*Function that evaluates the treatment probability function in a domain x, given the coefficients*

---

**Description**

Function that evaluates the treatment probability function in a domain x, given the coefficients

**Usage**

```
treatment_function_sample(coef_s, x, d_x, s_x)
```

**Arguments**

- |                     |   |
|---------------------|---|
| <code>coef_s</code> | • list with the function coefficients             |
| <code>x</code>      | • points at which the function is evaluated       |
| <code>d_x</code>    | • shifting parameter that was used to normalize x |
| <code>s_x</code>    | • scaling parameter that was used to normalize x  |

**Value**

list with the values of the function

---

`trim_dis_y`

*Binary outcomes for trimmed score*

---

**Description**

Binary outcomes for trimmed score

**Usage**

```
trim_dis_y(y, x, trimmed = NULL)
```

**Arguments**

- |                      |  |
|----------------------|--|
| <code>y</code>       | • outcome data   |
| <code>x</code>       | • score data   |
| <code>trimmed</code> | • NULL by default, provide vector of values to trim the data |

**Value**

list with y - outcomes for trimmed score

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