

# Package ‘LSTS’

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**Type** Package

**Title** Locally Stationary Time Series

**Version** 2.1

**Description** A set of functions that allow stationary analysis and locally stationary time series analysis.

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**BugReports** <https://github.com/pachadotdev/LSTS/issues/>

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**RdMacros** Rdpack

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## Contents

block.smooth.periodogram . . . . .	2
Box.Ljung.Test . . . . .	3
hessian . . . . .	4

LS.kalman . . . . .	5
LS.summary . . . . .	7
LS.whittle . . . . .	8
LS.whittle.loglik . . . . .	11
LS.whittle.loglik.sd . . . . .	12
LS.whittle.loglik.theta . . . . .	13
malleco . . . . .	14
periodogram . . . . .	15
smooth.periodogram . . . . .	16
spectral.density . . . . .	17
ts.diag . . . . .	18

## Index 20

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block.smooth.periodogram

*Smooth Periodogram by Blocks*

---

### Description

Plots the contour plot of the smoothing periodogram of a time series, by blocks or windows.

### Usage

```
block.smooth.periodogram(
  y,
  x = NULL,
  N = NULL,
  S = NULL,
  p = 0.25,
  spar.freq = 0,
  spar.time = 0
)
```

### Arguments

y	(type: numeric) data vector
x	(type: numeric) optional vector, if x = NULL then the function uses $(1, \dots, n)$ where n is the length of y.
N	(type: numeric) value corresponding to the length of the window to compute periodogram. If N=NULL then the function will use $N = \text{trunc}(n^{0.8})$ , see Dahlhaus and Giraitis (1998) where $n$ is the length of the y vector.
S	(type: numeric) value corresponding to the lag with which will be taking the blocks or windows to calculate the periodogram.
p	(type: numeric) value used if it is desired that S is proportional to N. By default $p=0.25$ , if S and N are not entered.
spar.freq	(type: numeric) smoothing parameter, typically (but not necessarily) in $(0, 1]$ .
spar.time	(type: numeric) smoothing parameter, typically (but not necessarily) in $(0, 1]$ .

**Details**

The number of windows of the function is  $m = \text{trunc}((n - N)/S + 1)$ , where `trunc` truncates the entered value and  $n$  is the length of the vector  $y$ . All windows are of the same length  $N$ , if this value isn't entered by user then is computed as  $N = \text{trunc}(n^{0.8})$  (Dahlhaus). `LSTS_spb` computes the periodogram in each of the  $M$  windows and then smoothes it two times with `smooth.spline` function; the first time using `spar.freq` parameter and the second time with `spar.time`. These windows overlap between them.

**Value**

A ggplot object.

**References**

For more information on theoretical foundations and estimation methods see Dahlhaus R, others (1997). "Fitting time series models to nonstationary processes." *The annals of Statistics*, **25**(1), 1–37. Dahlhaus R, Giraitis L (1998). "On the optimal segment length for parameter estimates for locally stationary time series." *Journal of Time Series Analysis*, **19**(6), 629–655.

**See Also**

`arima.sim`

**Examples**

```
block.smooth.periodogram(malleco)
```

---

Box.Ljung.Test

*Ljung-Box Test Plot*


---

**Description**

Plots the p-values Ljung-Box test.

**Usage**

```
Box.Ljung.Test(z, lag = NULL, main = NULL)
```

**Arguments**

<code>z</code>	(type: numeric) data vector
<code>lag</code>	(type: numeric) the number of periods for the autocorrelation
<code>main</code>	(type: character) a title for the returned plot

## Details

The Ljung-Box test is used to check if exists autocorrelation in a time series. The statistic is

$$q = n(n+2) \cdot \sum_{j=1}^h \hat{\rho}(j)^2 / (n-j)$$

with  $n$  the number of observations and  $\hat{\rho}(j)$  the autocorrelation coefficient in the sample when the lag is  $j$ . `LSTS_lbt` computes  $q$  and returns the p-values graph with lag  $j$ .

## Value

A ggplot object.

## References

For more information on theoretical foundations and estimation methods see Brockwell PJ, Davis RA, Calder MV (2002). *Introduction to time series and forecasting*, volume 2. Springer. Ljung GM, Box GE (1978). “On a measure of lack of fit in time series models.” *Biometrika*, **65**(2), 297–303.

## See Also

[periodogram](#)

## Examples

```
Box.Ljung.Test(malleco, lag = 5)
```

---

hessian

*Hessian Matrix*

---

## Description

Numerical approximation of the Hessian of a function.

## Usage

```
hessian(f, x0, ...)
```

## Arguments

<code>f</code>	(type: numeric) name of function that defines log likelihood (or negative of it).
<code>x0</code>	(type: numeric) scalar or vector of parameters that give the point at which you want the hessian estimated (usually will be the mle).
<code>...</code>	Additional arguments to be passed to the function.

**Details**

Computes the numerical approximation of the Hessian of  $f$ , evaluated at  $x_0$ . Usually needs to pass additional parameters (e.g. data). N.B. this uses no numerical sophistication.

**Value**

An  $n \times n$  matrix of 2nd derivatives, where  $n$  is the length of  $x_0$ .

**See Also**

[arima.sim](#)

**Examples**

```
# Variance of the maximum likelihood estimator for mu parameter in
# gaussian data
loglik <- function(series, x, sd = 1) {
  -sum(log(dnorm(series, mean = x, sd = sd)))
}
sqrt(c(var(malleco) / length(malleco), diag(solve(hessian(
  f = loglik, x = mean(malleco), series = malleco,
  sd = sd(malleco)
))))))
```

---

LS.kalman

*Kalman filter for locally stationary processes*


---

**Description**

This function run the state-space equations for expansion infinite of moving average in processes LS-ARMA or LS-ARFIMA.

**Usage**

```
LS.kalman(
  series,
  start,
  order = c(p = 0, q = 0),
  ar.order = NULL,
  ma.order = NULL,
  sd.order = NULL,
  d.order = NULL,
  include.d = FALSE,
  m = NULL
)
```

## Arguments

<code>series</code>	(type: numeric) univariate time series.
<code>start</code>	(type: numeric) numeric vector, initial values for parameters to run the model.
<code>order</code>	(type: numeric) vector corresponding to ARMA model entered.
<code>ar.order</code>	(type: numeric) AR polynomial order.
<code>ma.order</code>	(type: numeric) MA polynomial order.
<code>sd.order</code>	(type: numeric) polynomial order noise scale factor.
<code>d.order</code>	(type: numeric) d polynomial order, where d is the ARFIMA parameter.
<code>include.d</code>	(type: numeric) logical argument for ARFIMA models. If <code>include.d=FALSE</code> then the model is an ARMA process.
<code>m</code>	(type: numeric) truncation order of the MA infinity process. By default $m = 0.25n^{0.8}$ where n the length of series.

## Details

The model fit is done using the Whittle likelihood, while the generation of innovations is through Kalman Filter. Details about `ar.order`, `ma.order`, `sd.order` and `d.order` can be viewed in [LS.whittle](#).

## Value

A list with:

<code>residuals</code>	standard residuals.
<code>fitted_values</code>	model fitted values.
<code>delta</code>	variance prediction error.

## References

For more information on theoretical foundations and estimation methods see Brockwell PJ, Davis RA, Calder MV (2002). *Introduction to time series and forecasting*, volume 2. Springer. Palma W (2007). *Long-memory time series: theory and methods*, volume 662. John Wiley & Sons. Palma W, Olea R, Ferreira G (2013). “Estimation and forecasting of locally stationary processes.” *Journal of Forecasting*, **32**(1), 86–96.

## Examples

```
fit_kalman <- LS.kalman(malleco, start(malleco))
```

**Description**

Produces a summary of the results to Whittle estimator to Locally Stationary Time Series ([LS.whittle](#) function).

**Usage**

```
LS.summary(object)
```

**Arguments**

object (type: list) the output of [LS.whittle](#) function

**Details**

Calls the output from [LS.whittle](#) and computes the standard error and p-values to provide a detailed summary.

**Value**

A list with the following components:

summary	a resume table with estimate, std. error, z-value and p-value of the model.
aic	AIC of the model.
npar	number of parameters in the model.

**See Also**

[LS.whittle](#)

**Examples**

```
fit_whittle <- LS.whittle(  
  series = malleco, start = c(1, 1, 1, 1),  
  order = c(p = 1, q = 0), ar.order = 1, sd.order = 1, N = 180, n.ahead = 10  
)  
LS.summary(fit_whittle)
```

LS.whittle

*Whittle estimator to Locally Stationary Time Series***Description**

This function computes Whittle estimator to LS-ARMA and LS-ARFIMA models.

**Usage**

```
LS.whittle(
  series,
  start,
  order = c(p = 0, q = 0),
  ar.order = NULL,
  ma.order = NULL,
  sd.order = NULL,
  d.order = NULL,
  include.d = FALSE,
  N = NULL,
  S = NULL,
  include.taper = TRUE,
  control = list(),
  lower = -Inf,
  upper = Inf,
  m = NULL,
  n.ahead = 0
)
```

**Arguments**

<code>series</code>	(type: numeric) univariate time series.
<code>start</code>	(type: numeric) numeric vector, initial values for parameters to run the model.
<code>order</code>	(type: numeric) vector corresponding to ARMA model entered.
<code>ar.order</code>	(type: numeric) AR polinomial order.
<code>ma.order</code>	(type: numeric) MA polinomial order.
<code>sd.order</code>	(type: numeric) polinomial order noise scale factor.
<code>d.order</code>	(type: numeric) d polinomial order, where d is the ARFIMA parameter.
<code>include.d</code>	(type: numeric) logical argument for ARFIMA models. If <code>include.d=FALSE</code> then the model is an ARMA process.
<code>N</code>	(type: numeric) value corresponding to the length of the window to compute periodogram. If <code>N=NULL</code> then the function will use $N = \text{trunc}(n^{0.8})$ , see Dahlhaus (1998) where $n$ is the length of the y vector.
<code>S</code>	(type: numeric) value corresponding to the lag with which will go taking the blocks or windows.



include.taper	(type: logical) logical argument that by default is TRUE. See <a href="#">periodogram</a> .
control	(type: list) A list of control parameters. More details in <a href="#">nlminb</a> .
lower	(type: numeric) lower bound, replicated to be as long as start. If unspecified, all parameters are assumed to be lower unconstrained.
upper	(type: numeric) upper bound, replicated to be as long as start. If unspecified, all parameters are assumed to be upper unconstrained.
m	(type: numeric) truncation order of the MA infinity process, by default $m = 0.25n^{0.8}$ . Parameter used in LSTS_kalman.
n.ahead	(type: numeric) The number of steps ahead for which prediction is required. By default is zero.

### Details

This function estimates the parameters in models: LS-ARMA

$$\Phi(t/T, B) Y_{t,T} = \Theta(t/T, B) \sigma(t/T) \varepsilon_t$$

and LS-ARFIMA

$$\Phi(t/T, B) Y_{t,T} = \Theta(t/T, B) (1 - B)^{-d(t/T)} \sigma(t/T) \varepsilon_t,$$

with infinite moving average expansion

$$Y_{t,T} = \sigma(t/T) \sum_{j=0}^{\infty} \psi(t/T) \varepsilon_t,$$

for  $t = 1, \dots, T$ , where for  $u = t/T \in [0, 1]$ ,  $\Phi(u, B) = 1 + \phi_1(u)B + \dots + \phi_p(u)B^p$  is an autoregressive polynomial,  $\Theta(u, B) = 1 + \theta_1(u)B + \dots + \theta_q(u)B^q$  is a moving average polynomial,  $d(u)$  is a long-memory parameter,  $\sigma(u)$  is a noise scale factor and  $\{\varepsilon_t\}$  is a Gaussian white noise sequence with zero mean and unit variance. This class of models extends the well-known ARMA and ARFIMA process, which is obtained when the components  $\Phi(u, B)$ ,  $\Theta(u, B)$ ,  $d(u)$  and  $\sigma(u)$  do not depend on  $u$ . The evolution of these models can be specified in terms of a general class of functions. For example, let  $\{g_j(u)\}$ ,  $j = 1, 2, \dots$ , be a basis for a space of smoothly varying functions and let  $d_\theta(u)$  be the time-varying long-memory parameter in model LS-ARFIMA. Then we could write  $d_\theta(u)$  in terms of the basis  $\{g_j(u) = u^j\}$  as follows  $d_\theta(u) = \sum_{j=0}^k \alpha_j g_j(u)$  for unknown values of  $k$  and  $\theta = (\alpha_0, \alpha_1, \dots, \alpha_k)'$ . In this situation, estimating  $\theta$  involves determining  $k$  and estimating the coefficients  $\alpha_0, \alpha_1, \dots, \alpha_k$ . LS.whittle optimizes [LS.whittle.loglik](#) as objective function using [nlminb](#) function, for both LS-ARMA (`include.d=FALSE`) and LS-ARFIMA (`include.d=TRUE`) models. Also computes Kalman filter with [LS.kalman](#) and this values are given in `var.coef` in the output.

### Value

A list with the following components:

coef	The best set of parameters found.
var.coef	covariance matrix approximated for maximum likelihood estimator $\hat{\theta}$ of $\theta := (\theta_1, \dots, \theta_k)'$ . This matrix is approximated by $H^{-1}/n$ , where $H$ is the Hessian matrix $[\partial^2 \ell(\theta) / \partial \theta_i \partial \theta_j]_{i,j=1}^k$ .

loglik	log-likelihood of coef, calculated with <a href="#">LS.whittle</a> .
aic	Akaike's 'An Information Criterion', for one fitted model LS-ARMA or LS-ARFIMA. The formula is $-2L + 2k/n$ , where $L$ represents the log-likelihood, $k$ represents the number of parameters in the fitted model and $n$ is equal to the length of the series.
series	original time serie.
residuals	standard residuals.
fitted.values	model fitted values.
pred	predictions of the model.
se	the estimated standard errors.
model	A list representing the fitted model.

### See Also

[nlminb](#), [LS.kalman](#)

### Examples

```
# Analysis by blocks of phi and sigma parameters
N <- 200
S <- 100
M <- trunc((length(malleco) - N) / S + 1)
table <- c()
for (j in 1:M) {
  x <- malleco[(1 + S * (j - 1)):(N + S * (j - 1))]
  table <- rbind(table, nlminb(
    start = c(0.65, 0.15), N = N,
    objective = LS.whittle.loglik,
    series = x, order = c(p = 1, q = 0)
  )$par)
}
u <- (N / 2 + S * (1:M - 1)) / length(malleco)
table <- as.data.frame(cbind(u, table))
colnames(table) <- c("u", "phi", "sigma")
# Start parameters
phi <- smooth.spline(table$phi, spar = 1, tol = 0.01)$y
fit.1 <- nls(phi ~ a0 + a1 * u, start = list(a0 = 0.65, a1 = 0.00))
sigma <- smooth.spline(table$sigma, spar = 1)$y
fit.2 <- nls(sigma ~ b0 + b1 * u, start = list(b0 = 0.65, b1 = 0.00))
fit_whittle <- LS.whittle(
  series = malleco, start = c(coef(fit.1), coef(fit.2)), order = c(p = 1, q = 0),
  ar.order = 1, sd.order = 1, N = 180, n.ahead = 10
)
```

---

LS.whittle.loglik      *Locally Stationary Whittle log-likelihood Function*


---

## Description

This function computes Whittle estimator for LS-ARMA and LS-ARFIMA models, in data with mean zero. If mean is not zero, then it is subtracted to data.

## Usage

```
LS.whittle.loglik(
  x,
  series,
  order = c(p = 0, q = 0),
  ar.order = NULL,
  ma.order = NULL,
  sd.order = NULL,
  d.order = NULL,
  include.d = FALSE,
  N = NULL,
  S = NULL,
  include.taper = TRUE
)
```

## Arguments

x	(type: numeric) parameter vector.
series	(type: numeric) univariate time series.
order	(type: numeric) vector corresponding to ARMA model entered.
ar.order	(type: numeric) AR polynomial order.
ma.order	(type: numeric) MA polynomial order.
sd.order	(type: numeric) polynomial order noise scale factor.
d.order	(type: numeric) d polynomial order, where d is the ARFIMA parameter.
include.d	(type: numeric) logical argument for ARFIMA models. If include.d=FALSE then the model is an ARMA process.
N	(type: numeric) value corresponding to the length of the window to compute periodogram. If N=NULL then the function will use $N = \text{trunc}(n^{0.8})$ , see Dahlhaus (1998) where $n$ is the length of the y vector.
S	(type: numeric) value corresponding to the lag with which will go taking the blocks or windows.
include.taper	(type: logical) logical argument that by default is TRUE. See <a href="#">periodogram</a> .

### Details

The estimation of the time-varying parameters can be carried out by means of the Whittle log-likelihood function proposed by Dahlhaus (1997),

$$L_n(\theta) = \frac{1}{4\pi} \frac{1}{M} \int_{-\pi}^{\pi} \left\{ \log f_{\theta}(u_j, \lambda) + \frac{I_N(u_j, \lambda)}{f_{\theta}(u_j, \lambda)} \right\} d\lambda$$

where  $M$  is the number of blocks,  $N$  the length of the series per block,  $n = S(M - 1) + N$ ,  $S$  is the shift from block to block,  $u_j = t_j/n$ ,  $t_j = S(j - 1) + N/2$ ,  $j = 1, \dots, M$  and  $\lambda$  the Fourier frequencies in the block  $(2\pi k/N, k = 1, \dots, N)$ .

### References

For more information on theoretical foundations and estimation methods see Brockwell PJ, Davis RA, Calder MV (2002). *Introduction to time series and forecasting*, volume 2. Springer. Palma W, Olea R, others (2010). “An efficient estimator for locally stationary Gaussian long-memory processes.” *The Annals of Statistics*, **38**(5), 2958–2997.

### See Also

[nlminb](#), [LS.kalman](#)

---

LS.whittle.loglik.sd    *Locally Stationary Whittle Log-likelihood sigma*

---

### Description

This function calculates log-likelihood with known  $\theta$ , through LS.whittle.loglik function.

### Usage

```
LS.whittle.loglik.sd(
  x,
  series,
  order = c(p = 0, q = 0),
  ar.order = NULL,
  ma.order = NULL,
  sd.order = NULL,
  d.order = NULL,
  include.d = FALSE,
  N = NULL,
  S = NULL,
  include.taper = TRUE,
  theta.par = numeric()
)
```

**Arguments**

x	(type: numeric) parameter vector.
series	(type: numeric) univariate time series.
order	(type: numeric) vector corresponding to ARMA model entered.
ar.order	(type: numeric) AR polynomial order.
ma.order	(type: numeric) MA polynomial order.
sd.order	(type: numeric) polynomial order noise scale factor.
d.order	(type: numeric) d polynomial order, where d is the ARFIMA parameter.
include.d	(type: numeric) logical argument for ARFIMA models. If include.d=FALSE then the model is an ARMA process.
N	(type: numeric) value corresponding to the length of the window to compute periodogram. If N=NULL then the function will use $N = \text{trunc}(n^{0.8})$ , see Dahlhaus (1998) where $n$ is the length of the y vector.
S	(type: numeric) value corresponding to the lag with which will go taking the blocks or windows.
include.taper	(type: logical) logical argument that by default is TRUE. See <a href="#">periodogram</a> .
theta.par	(type: numeric) vector with the known parameters of the model.

**Details**

This function computes [LS.whittle.loglik](#) with x as  $x = c(\text{theta.par}, x)$ .

---

LS.whittle.loglik.theta

*Locally Stationary Whittle Log-likelihood theta*

---

**Description**

Calculate the log-likelihood with  $\sigma$  known, through LS.whittle.loglik function.

**Usage**

```
LS.whittle.loglik.theta(
  x,
  series,
  order = c(p = 0, q = 0),
  ar.order = NULL,
  ma.order = NULL,
  sd.order = NULL,
  d.order = NULL,
  include.d = FALSE,
  N = NULL,
  S = NULL,
  include.taper = TRUE,
  sd.par = 1
)
```

**Arguments**

<code>x</code>	(type: numeric) parameter vector.
<code>series</code>	(type: numeric) univariate time series.
<code>order</code>	(type: numeric) vector corresponding to ARMA model entered.
<code>ar.order</code>	(type: numeric) AR polynomial order.
<code>ma.order</code>	(type: numeric) MA polynomial order.
<code>sd.order</code>	(type: numeric) polynomial order noise scale factor.
<code>d.order</code>	(type: numeric) d polynomial order, where d is the ARFIMA parameter.
<code>include.d</code>	(type: numeric) logical argument for ARFIMA models. If <code>include.d=FALSE</code> then the model is an ARMA process.
<code>N</code>	(type: numeric) value corresponding to the length of the window to compute periodogram. If <code>N=NULL</code> then the function will use $N = \text{trunc}(n^{0.8})$ , see Dahlhaus (1998) where $n$ is the length of the $y$ vector.
<code>S</code>	(type: numeric) value corresponding to the lag with which will go taking the blocks or windows.
<code>include.taper</code>	(type: logical) logical argument that by default is TRUE. See <a href="#">periodogram</a> .
<code>sd.par</code>	(type: numeric) value corresponding to known variance.

**Details**

This function computes [LS.whittle.loglik](#) with `x` as `x = c(x, sd.par)`.

---

malleco

Average Araucaria Araucana Tree Ring Width

---

**Description**

A ts object containing average annual ring width measured in milimeters for different Araucaria Araucana trees in the Malleco Region (Chile). The years of observation in this data cover the period 1242-1975.

**Format**

A time series object with 734 elements

**Author(s)**

National Oceanic and Atmospheric Administration (NOAA)

---

periodogram	<i>Periodogram function</i>
-------------	-----------------------------

---

### Description

This function computes the periodogram from a stationary time serie. Returns the periodogram, its graph and the Fourier frequency.

### Usage

```
periodogram(y, plot = TRUE, include.taper = FALSE)
```

### Arguments

y	(type: numeric) data vector
plot	(type: logical) logical argument which allows to plot the periodogram. Defaults to TRUE.
include.taper	(type: logical) logical argument which by default is FALSE. If include.taper=TRUE then y is multiplied by $0.5(1 - \cos(2\pi(n-1)/n))$ (cosine bell).

### Details

The tapered periodogram it is given by

$$I(\lambda) = \frac{|D_n(\lambda)|^2}{2\pi H_{2,n}(0)}$$

with  $D(\lambda) = \sum_{s=0}^{n-1} h\left(\frac{s}{N}\right) y_{s+1} e^{-i\lambda s}$ ,  $H_{k,n} = \sum_{s=0}^{n-1} h\left(\frac{s}{N}\right)^k e^{-i\lambda s}$  and  $\lambda$  are Fourier frequencies defined as  $2\pi k/n$ , with  $k = 1, \dots, n$ . The data taper used is the cosine bell function,  $h(x) = \frac{1}{2}[1 - \cos(2\pi x)]$ . If the series has missing data, these are replaced by the average of the data and  $n$  it is corrected by  $n-N$ , where  $N$  is the amount of missing values of serie. The plot of the periodogram is periodogram values vs.  $\lambda$ .

### Value

A list with with the periodogram and the lambda values.

### References

For more information on theoretical foundations and estimation methods see Brockwell PJ, Davis RA, Calder MV (2002). *Introduction to time series and forecasting*, volume 2. Springer. Dahlhaus R, others (1997). "Fitting time series models to nonstationary processes." *The annals of Statistics*, **25**(1), 1–37.

### See Also

[fft](#), [Mod](#), [smooth.spline](#).

## Examples

```
# AR(1) simulated
set.seed(1776)
ts.sim <- arima.sim(n = 1000, model = list(order = c(1, 0, 0), ar = 0.7))
per <- periodogram(ts.sim)
per$plot
```

---

smooth.periodogram	<i>Smoothing periodogram</i>
--------------------	------------------------------

---

## Description

This function returns the smoothing periodogram of a stationary time serie, its plot and its Fourier frequency.

## Usage

```
smooth.periodogram(y, plot = TRUE, spar = 0)
```

## Arguments

y	(type: numeric) data vector.
plot	(type: logical) logical argument which allows to plot the periodogram. Defaults to TRUE.
spar	(type: numeric) smoothing parameter, typically (but not necessarily) in (0, 1].

## Details

smooth.periodogram computes the periodogram from y vector and then smooth it with *smoothing spline* method, which basically approximates a curve using a cubic spline (see more details in [smooth.spline](#)).  $\lambda$  is the Fourier frequency obtained through [periodogram](#). It must have caution with the minimum length of y, because smooth.spline requires the entered vector has at least length 4 and the length of y does not equal to the length of the data of the periodogram that smooth.spline receives. If it presents problems with tol (**tolerance**), see [smooth.spline](#).

## Value

A list with with the smooth periodogram and the lambda values

## See Also

[smooth.spline](#), [periodogram](#)



**Examples**

```
# AR(1) simulated
require(ggplot2)
set.seed(1776)
ts.sim <- arima.sim(n = 1000, model = list(order = c(1, 0, 0), ar = 0.7))
per <- periodogram(ts.sim)
aux <- smooth.periodogram(ts.sim, plot = FALSE, spar = .7)
sm_p <- data.frame(x = aux$lambda, y = aux$smooth.periodogram)
sp_d <- data.frame(
  x = aux$lambda,
  y = spectral.density(ar = 0.7, lambda = aux$lambda)
)
g <- per$plot
g +
  geom_line(data = sm_p, aes(x, y), color = "#ff7f0e") +
  geom_line(data = sp_d, aes(x, y), color = "#d31244")
```

---

spectral.density	<i>Spectral Density</i>
------------------	-------------------------

---

**Description**

Returns theoretical spectral density evaluated in ARMA and ARFIMA processes.

**Usage**

```
spectral.density(ar = numeric(), ma = numeric(), d = 0, sd = 1, lambda = NULL)
```

**Arguments**

ar	(type: numeric) AR vector. If the time serie doesn't have AR term then omit it. For more details see the examples.
ma	(type: numeric) MA vector. If the time serie doesn't have MA term then omit it. For more details see the examples.
d	(type: numeric) Long-memory parameter. If d is zero, then the process is ARMA(p,q).
sd	(type: numeric) Noise scale factor, by default is 1.
lambda	(type: numeric) $\lambda$ parameter on which the spectral density is calculated/computed. If lambda=NULL then it is considered a sequence between 0 and $\pi$ .

**Details**

The spectral density of an ARFIMA(p,d,q) processes is

$$f(\lambda) = \frac{\sigma^2}{2\pi} \cdot \left(2 \sin(\lambda/2)\right)^{-2d} \cdot \frac{\left|\theta\left(\exp\left(-i\lambda\right)\right)\right|^2}{\left|\phi\left(\exp\left(-i\lambda\right)\right)\right|^2}$$

With  $-\pi \leq \lambda \leq \pi$  and  $-1 < d < 1/2$ .  $|x|$  is the [Mod](#) of  $x$ . LSTS\_sd returns the values corresponding to  $f(\lambda)$ . When d is zero, the spectral density corresponds to an ARMA(p,q).

### Value

An unnamed vector of numeric class.

### References

For more information on theoretical foundations and estimation methods see Brockwell PJ, Davis RA, Calder MV (2002). *Introduction to time series and forecasting*, volume 2. Springer. Palma W (2007). *Long-memory time series: theory and methods*, volume 662. John Wiley & Sons.

### Examples

```
# Spectral Density AR(1)
require(ggplot2)
f <- spectral.density(ar = 0.5, lambda = malleco)
ggplot(data.frame(x = malleco, y = f)) +
  geom_line(aes(x = as.numeric(x), y = as.numeric(y))) +
  labs(x = "Frequency", y = "Spectral Density") +
  theme_minimal()
```

---

ts.diag

*Diagnostic Plots for Time Series fits*


---

### Description

Plot time-series diagnostics.

### Usage

```
ts.diag(x, lag = 10, band = qnorm(0.975)/sqrt(length(x)))
```

### Arguments

x	(type: numeric) residuals of the fitted time series model.
lag	(type: numeric) maximum lag at which to calculate the acf and Ljung-Box test. By default set to 10.
band	(type: numeric) absolute value for bandwidth in the the ACF plot. By default set to 'qnorm(0.975)/sqrt(n)' which approximates to 0.07 for malleco data (n = 734)

### Details

This function plot the residuals, the autocorrelation function of the residuals (ACF) and the p-values of the Ljung-Box Test for all lags up to lag.

**Value**

A ggplot object.

**See Also**

[Box.Ljung.Test](#)

**Examples**

```
ts.diag(malleco)
```

# Index

## \* **data**

malleco, [14](#)

arma.sim, [3](#), [5](#)

block.smooth.periodogram, [2](#)

Box.Ljung.Test, [3](#), [19](#)

fft, [15](#)

hessian, [4](#)

LS.kalman, [5](#), [9](#), [10](#), [12](#)

LS.summary, [7](#)

LS.whittle, [6](#), [7](#), [8](#), [10](#)

LS.whittle.loglik, [9](#), [11](#), [13](#), [14](#)

LS.whittle.loglik.sd, [12](#)

LS.whittle.loglik.theta, [13](#)

malleco, [14](#)

Mod, [15](#), [18](#)

nlminb, [9](#), [10](#), [12](#)

periodogram, [4](#), [9](#), [11](#), [13](#), [14](#), [15](#), [16](#)

smooth.periodogram, [16](#)

smooth.spline, [3](#), [15](#), [16](#)

spectral.density, [17](#)

trunc, [3](#)

ts.diag, [18](#)