Package 'HMC'

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Title High-Dimensional Mean Comparison with Projection and Cross-Fitting

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Description Provides interpretable high-dimensional mean comparison methods (HMC). For example, users can apply these methods to assess the difference in gene expression between two treatment groups. It is not a gene-by-gene comparison. Instead, the methods focus on the interplay between features and identify those that are predictive of the group label. The tests are valid frequentist procedures and yield sparse estimates indicating which features contribute to the group differences.

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anchored_lasso_testing

Anchored test for two-sample mean comparison.

Description

Anchored test for two-sample mean comparison.

Usage

```
anchored_lasso_testing(
  sample_1,
  sample_2,
  pca_method = "sparse_pca",
  mean_method = "lasso",
  lasso_tuning_method = "min",
  num_latent_factor = 1,
  n_folds = 5,
  verbose = TRUE
)
```

sample_1	Group 1 sample. Each row is a subject and each column corresponds to a feature.
sample_2	Group 2 sample. Each row is a subject and each column corresponds to a feature.
pca_method	Methods used to estimate principle component The default is "sparse_pca", us- ing sparse PCA from package PMA. Other choices are "dense_pca"—the regular PCA; and "hard"— hard-thresholding PCA, which also induces sparsity.

mean_method	Methods used to estimate the discriminant direction. Default is logistic Lasso "lasso". Can also take value "lasso_no_truncation"	
lasso_tuning_me	thod	
	Method for Lasso penalty hyperparameter tuning. Default is "min", the mini- mizer of cross-validation error; users can also use "1se" for more sparse solu- tions.	
num_latent_factor		
	The principle component that lasso coefficient anchors at. The default is $PC1 = 1$.	
n_folds	Number of splits when performing cross-fitting. The default is 5, if computational time allows, you can try to set it to 10.	
verbose	Print information to the console. Default is TRUE.	

A list of test statistics.

test_statistics	5	
	Test statistics. Each entry corresponds to the test result of one principle component.	
standard_error	Estimated standard error of test_statistics_before_studentization.	
test_statistics_before_studentization		
	Similar to test_statistics but does not have variance $= 1$.	
split_data	Intermediate quantities needed for further assessment and interpretation of the test results.	

check_data_for_folds Check that data has enough rows for cross-validation folds

Description

Validates that the input data has at least as many rows as the number of desired folds.

Usage

```
check_data_for_folds(data, n_folds)
```

Arguments

data	A data frame or matrix.
n_folds	Integer. The number of folds to check for.

Value

NULL (called for its side effect). Throws an error if the number of rows is too small.

Examples

```
check_data_for_folds(matrix(1:20, nrow = 5), n_folds = 5)
## Not run:
check_data_for_folds(matrix(1:4, nrow = 2), n_folds = 5) # This will throw an error
## End(Not run)
```

check_non_null_and_identical_colnames

Check non-null and consistent column names across datasets

Description

Ensures all input datasets have non-null, non-empty, and identical column names.

Usage

check_non_null_and_identical_colnames(data_list)

Arguments

data_list A list of matrices or data frames to be checked.

NULL (called for side-effect). Throws an error if validation fails.

Examples

```
d1 <- data.frame(a = 1:2, b = 3:4)
d2 <- data.frame(a = 5:6, b = 7:8)
check_non_null_and_identical_colnames(list(d1, d2))
```

```
collect_active_features_proj
```

Collect active features and groups based on projection directions

Description

Identifies consistently non-zero features across cross-validation folds using a voting scheme and returns active groups if a grouping vector is provided.

Usage

```
collect_active_features_proj(
  test_result,
  voting_method = c("majority_voting"),
  group = NULL,
  group_threshold = 1
)
```

Arguments

test_result	A result object from mean_comparison_anchor() containing fold_data.	
voting_method	Character. Method to determine active features. Only "majority_voting" is currently supported.	
group	Optional grouping vector with feature names. Must match the feature dimension of classifier_coef.	
group_threshold		
	Integer. Minimum number of active features required to declare a group active. Default is 1.	

Value

If group is provided, returns a list with:

active_features Character vector of consistently non-zero features.

active_groups Character vector of active groups.

If group is NULL, returns a character vector of active features only.

```
combine_folds_mean_diff
```

Combine fold-level test statistics from cross-validation

Description

Aggregates fold-level test statistics and variances to compute an overall test statistic and p-value.

Usage

```
combine_folds_mean_diff(fold_data, verbose = FALSE)
```

Arguments

fold_data	A list of results from process_fold_mean_diff(), one for each fold.
verbose	Logical. Whether to print diagnostic messages. Default is FALSE.

Value

A list containing:

p_value Two-sided p-value for the overall test statistic.

test_statistic Standardized test statistic.

fold_data Original input list, for reference or diagnostics.

compute_predictive_contributions

Compute predictive contributions of feature groups

Description

Analyzes the relative contribution of grouped features to the overall discriminant signal, based on averaged Lasso coefficients across cross-validation folds.

Usage

```
compute_predictive_contributions(result, group, group_threshold = 5)
```

result	A result object returned by mean_comparison_anchor(), containing fold_data with classifier coefficients.	
group	A grouping vector indicating group membership of features. Must be the same length as the number of features.	
group_threshold		
	Integer. Minimum number of active features required in a group for it to be considered active. Default is 5.	

Details

The function identifies active groups based on cross-validated non-zero coefficients, then decomposes the total L2 norm of the average coefficient vector across groups.

Value

A data frame with two columns:

group Group name or label.

score Proportion of total predictive signal attributable to that group.

See Also

collect_active_features_proj

<pre>debiased_pc_testing</pre>	Debiased one-step test for two-sample mean comparison. A small p-
	value tells us not only there is difference in the mean vectors, but can
	also indicates which principle component the difference aligns with.

Description

Debiased one-step test for two-sample mean comparison. A small p-value tells us not only there is difference in the mean vectors, but can also indicates which principle component the difference aligns with.

Usage

```
debiased_pc_testing(
   sample_1,
   sample_2 = NULL,
   pca_method = "sparse_pca",
   mean_method = "naive",
   num_latent_factor = 1,
   n_folds = 5,
   verbose = TRUE
)
```

sample_1	Group 1 sample. Each row is a subject and each column corresponds to a feature.
sample_2	Group 2 sample. Each row is a subject and each column corresponds to a feature.
pca_method	Methods used to estimate principle component The default is "sparse_pca", us- ing sparse PCA from package PMA. Other choices are "dense_pca"—the regular PCA; and "hard"— hard-thresholding PCA, which also induces sparsity.

mean_method	Methods used to estimate the mean vector. Default is sample mean "naive". There is also a hard-thresholding sparse estiamtor "hard".
num_latent_fact	or
	Number of principle to be estimated/tested. Default is 1.
n_folds	Number of splits when performing cross-fitting. The default is 5, if computational time allows, you can try to set it to 10.
verbose	Print information to the console. Default is TRUE.
verbose	Print information to the console. Default is TRUE.

A list of test statistics.

test_statistics	5
	Test statistics. Each entry corresponds to the test result of one principle component.
standard_error	Estimated standard error of test_statistics_before_studentization.
test_statistics	s_before_studentization
	Similar to test_statistics but does not have variance $= 1$.
split_data	Intermediate quantities needed for further assessment and interpretation of the test results.

```
sample_size_1 <- sample_size_2 <- 300</pre>
true_mean_1 <- matrix(c(rep(1, 10), rep(0, 90)), ncol = 1)</pre>
true_mean_2 <- matrix(c(rep(1.5, 10), rep(0, 90)), ncol = 1)</pre>
pc1 <- c(rep(1, 10), rep(0, 90))</pre>
pc1 <- pc1/norm(pc1, type = '2')</pre>
simulation_covariance <- 10 * pc1 %*% t(pc1)</pre>
simulation_covariance <- simulation_covariance + diag(1, 100)</pre>
sample_1 <- data.frame(MASS::mvrnorm(sample_size_1,</pre>
                                 mu = true_mean_1,
                                 Sigma = simulation_covariance))
 sample_2 <- data.frame(MASS::mvrnorm(sample_size_2,</pre>
                                 mu = true_mean_2,
                                 Sigma = simulation_covariance))
 result <- debiased_pc_testing(sample_1, sample_2)</pre>
 result$test_statistics
 ##these are test statistics. Each one of them corresponds to one PC.
 summarize_pc_name(result, latent_fator_index = 1) #shows which features contribute to PC1
 extract_pc(result) # extract the estimated leading PCs.
```

estimate_leading_pc Estimate the leading principal component

Description

Estimates the leading principal component of the input matrix using dense or sparse PCA.

Usage

```
estimate_leading_pc(control, pca_method = c("dense_pca", "sparse_pca"))
```

Arguments

control	A matrix or data frame. Each row is a sample, and each column is a feature.
pca_method	Character. PCA method to use. Options are "dense_pca" (default) or "sparse_pca".

Details

For low-dimensional settings (\leq 30 features), the method automatically switches to dense PCA. For sparse PCA, the function uses the PMA::SPC.cv cross-validation method.

Value

A normalized numeric vector representing the leading principal component direction.

Examples

```
## Not run:
X <- matrix(rnorm(100), nrow = 20)
estimate_leading_pc(X, pca_method = "dense_pca")
## End(Not run)
```

estimate_nuisance_parameter_lasso
The function for nuisance parameter_nuisance pa

The function for nuisance parameter estimation in anchored_lasso_testing().

Description

The function for nuisance parameter estimation in anchored_lasso_testing().

Usage

```
estimate_nuisance_parameter_lasso(
    nuisance_sample_1,
    nuisance_sample_2,
    pca_method = "sparse_pca",
    mean_method = "lasso",
    lasso_tuning_method = "min",
    num_latent_factor = 1,
    local_environment = local_environment,
    verbose = TRUE
)
```

Arguments

nuisance_sampl	e_1	
	Group 1 sample. Each row is a subject and each column corresponds to a feature.	
nuisance_sampl	e_2	
	Group 2 sample. Each row is a subject and each column corresponds to a feature.	
pca_method	Methods used to estimate principle component The default is "sparse_pca", us- ing sparse PCA from package PMA. Other choices are "dense_pca"—the regular PCA; and "hard"— hard-thresholding PCA, which also induces sparsity.	
mean_method	Methods used to estimate the discriminant direction. Default is logistic Lasso "lasso". Can also take value "lasso_no_truncation"	
lasso_tuning_method		
	Method for Lasso penalty hyperparameter tuning. Default is "min", the mini- mizer of cross-validation error; users can also use "1se" for more sparse solu- tions.	
num_latent_fac	tor	
	The principle component that lasso coefficient anchors at. The default is $PC1 = 1$.	
local_environment		
	An environment for hyperparameters shared between folds.	
verbose	Print information to the console. Default is TRUE.	

Value

A list of estimated nuisance quantities.

estimate_leading_pc

Leading principle components

estimate_mean_1

Sample mean for group 1

estimate_mean_2

Sample mean for group 1

estimate_lasso_beta

Logistic Lasso regression coefficients.

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estimate_projection_direction

Anchored projection direction. It is similar to PC1 when signal is weak but similar to estimate_optimal_direction when the signal is moderately large.

estimate_optimal_direction

Discriminant direction.

estimate_nuisance_pc The function for nuisance parameter estimation in simple_pc_testing() and debiased_pc_testing().

Description

The function for nuisance parameter estimation in simple_pc_testing() and debiased_pc_testing().

Usage

```
estimate_nuisance_pc(
   nuisance_sample_1,
   nuisance_sample_2 = NULL,
   pca_method = "sparse_pca",
   mean_method = "naive",
   num_latent_factor = 1,
   local_environment = NA
)
```

nuisance_sample_1			
	Group 1 sample. Each row is a subject and each column corresponds to a feature.		
nuisance_sampl	e_2		
	Group 2 sample. Each row is a subject and each column corresponds to a feature.		
pca_method	Methods used to estimate principle component The default is "sparse_pca", us- ing sparse PCA from package PMA. Other choices are "dense_pca"—the regular PCA; and "hard"— hard-thresholding PCA, which also induces sparsity.		
mean_method	Methods used to estimate the mean vector. Default is sample mean "naive". There is also a hard-thresholding sparse estiamtor "hard".		
num_latent_factor			
	Number of principle to be estimated/tested. Default is 1.		
local_environment			
	A environment for hyperparameters shared between folds.		

A list of estimated nuisance quantities.

estimate_leading_pc Leading principle components estimate_mean_1 Sample mean for group 1 estimate_mean_2 Sample mean for group 1 estimate_eigenvalue Eigenvalue for each principle compoenent. estimate_noise_variance Noise variance, I need this to construct block-diagonal estimates of the covariance matrix.

evaluate_influence_function_multi_factor Calculate the test statistics on the left-out samples. Called in debiased_pc_testing().

Description

Calculate the test statistics on the left-out samples. Called in debiased_pc_testing().

Usage

```
evaluate_influence_function_multi_factor(
    cross_fitting_sample_1,
    cross_fitting_sample_2 = NULL,
    nuisance_collection,
    num_latent_factor = 1
)
```

Arguments

cross_fitting_sample_1 Group 1 sample. Each row is a subject and each column corresponds to a feature. cross_fitting_sample_2 Group 2 sample. Each row is a subject and each column corresponds to a feature. nuisance_collection A collection of nuisance quantities estimated using "nuisance" samples. It is the output of estimate_nuisance_pc(). num_latent_factor

Number of principle components to be considered.

A list of test statistics. inner_product_1 Simple inner products for sample 1. inner_product_2 Simple inner products for sample 2. influence_eigenvector_each_subject_1 Debiased test statistics, sample 1. influence_eigenvector_each_subject_2 Debiased test statistics, sample 1. for_variance_subject_1 Statistics for variance calculation, sample 1. for_variance_subject_2 Statistics for variance calculation, sample 2.

evaluate_pca_lasso_plug_in

Calculate the test statistics on the left-out samples. Called in anchored_lasso_testing().

Description

Calculate the test statistics on the left-out samples. Called in anchored_lasso_testing().

Usage

```
evaluate_pca_lasso_plug_in(
    cross_fitting_sample_1,
    cross_fitting_sample_2,
    nuisance_collection,
    mean_method = "lasso"
)
```

cross_fitting_:	sample_1
	Group 1 sample. Each row is a subject and each column corresponds to a feature.
cross_fitting_	sample_2
	Group 2 sample. Each row is a subject and each column corresponds to a feature.
nuisance_colle	ction
	A collection of nuisance quantities estimated using "nuisance" samples. It is the output of estimate_nuisance_pc().
mean_method	Methods used to estimate the discriminant direction. Default is logistic Lasso "lasso". Can also take value "lasso_no_truncation"

```
A list of test statistics.

influence_each_subject_1

Test statistics for sample 1.

influence_each_subject_1

Test statistics for sample 2.

for_variance_each_subject_1

Statistics for variance calculation, sample 1.

for_variance_each_subject_2

Statistics for variance calculation, sample 2.
```

evaluate_pca_plug_in Calculate the test statistics on the left-out samples. Called in simple_pc_testing().

Description

Calculate the test statistics on the left-out samples. Called in simple_pc_testing().

Usage

```
evaluate_pca_plug_in(
    cross_fitting_sample_1,
    cross_fitting_sample_2 = NULL,
    nuisance_collection
)
```

Arguments

```
cross_fitting_sample_1
Group 1 sample. Each row is a subject and each column corresponds to a feature.
cross_fitting_sample_2
Group 2 sample. Each row is a subject and each column corresponds to a feature.
nuisance_collection
A collection of nuisance quantities estimated using "nuisance" samples. It is the
output of estimate_nuisance_pc().
```

Value

```
A list of test statistics.

influence_each_subject_1

Statistics for sample 1.

influence_each_subject_2

Statistics for sample 2.
```

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extract_lasso_coef Extract the lasso estimate from the output of anchored_lasso_testing().

Description

Extract the lasso estimate from the output of anchored_lasso_testing().

Usage

```
extract_lasso_coef(testing_result)
```

Arguments

testing_result The output/test result list from anchored_lasso_testing().

Value

A list, whose elements are the estimated discriminant directions for each split—the length of the output list is the same as n_folds.

The discriminant vectors for each split.

extract_pc	Extract	the	principle	components	from	the	output	of	sim-
	ple_pc_	testing	g() and deb	iased_pc_testi	ng().				

Description

Extract the principle components from the output of simple_pc_testing() and debiased_pc_testing().

Usage

```
extract_pc(testing_result)
```

Arguments

testing_result The output/test result list from simple_pc_testing() or debiased_pc_testing().

Value

A list, whose elements are the estimated PC for each split—the length of the output list is the same as n_{f} folds.

The PC vectors for each split.

```
fit_lasso
```

Description

Performs Lasso or group Lasso logistic regression to distinguish between two groups of samples.

Usage

```
fit_lasso(
   control_train,
   treat_train,
   lambda_type = c("lambda.min", "lambda.1se"),
   classifier_method = c("lasso", "group_lasso"),
   group = NULL
)
```

Arguments

control_train	A matrix or data frame for the control group. Rows are samples, columns are features.
treat_train	A matrix or data frame for the treatment group. Rows are samples, columns are features.
lambda_type	Character. Type of lambda to use from cross-validation. Options are "lambda.min" (default) and "lambda.lse".
classifier_met	hod
	Character. Choice of classifier. "lasso" (default) or "group_lasso".
group	Optional grouping vector for group_lasso, same length as the number of columns in the input data.

Details

The function fits a logistic regression using either glmnet for Lasso or grpreg for group Lasso. Coefficients are soft-thresholded by the maximum coefficient times $n^{(-1/3)}$ where n is the effective sample size.

Value

A numeric vector of estimated regression coefficients (excluding intercept), thresholded for small values.

```
## Not run:
X1 <- matrix(rnorm(100), nrow = 10)
X2 <- matrix(rnorm(100), nrow = 10)
fit_lasso(X1, X2, classifier_method = "lasso")
```

End(Not run)

index_spliter Split indices into folds

Description

Randomly splits a given vector of indices into approximately equal-sized folds.

Usage

```
index_spliter(array, n_folds = 5)
```

Arguments

array	A vector of indices (e.g., $1:n$) to be split into folds.
n_folds	Integer. Number of folds. Default is 5.

Value

A list of length n_folds, each containing a subset of the shuffled indices.

Examples

index_spliter(1:10, n_folds = 3)

mean_comparison_anchor

High-dimensional two-sample mean comparison with anchored projection

Description

Performs a cross-validated, projection-based mean comparison between two high-dimensional groups using sparse or dense PCA and (group) Lasso classifiers.

Usage

```
mean_comparison_anchor(
    control,
    treatment,
    pca_method = c("dense_pca", "sparse_pca"),
    classifier_method = c("lasso", "group_lasso"),
    lambda_type = "lambda.1se",
    n_folds = 10,
    group = NULL,
    standardize_feature = TRUE,
    verbose = TRUE
)
```

Arguments

control	A matrix or data frame for the control group. Rows are samples; columns are features.		
treatment	A matrix or data frame for the treatment group. Rows are samples; columns are features.		
pca_method	Character. Method for estimating the projection direction. Options are "dense_pca" or "sparse_pca". Default is "sparse_pca".		
classifier_met	hod		
	Character. Classifier to guide the projection. Options are "lasso" or "group_lasso". Default is "lasso".		
lambda_type	Character. Regularization parameter choice in Lasso. Options are "lambda.min" or "lambda.lse". Default is "lambda.lse".		
n_folds	Integer. Number of cross-validation folds. Default is 10.		
group	Optional. A grouping vector (required for group_lasso), same length as the number of columns in control.		
standardize_fe	ature		
	Logical. Whether to standardize features using pooled mean and standard devi- ation. Default is TRUE.		
verbose	Logical. Whether to print messages during execution. Default is TRUE.		

Details

This function applies a projection-based method for high-dimensional mean testing. The projection direction is computed by anchoring the leading principal component with a regularized classifier (Lasso or group Lasso), and test statistics are aggregated across folds.

Value

A list with:

p_value Two-sided p-value for the overall test.

test_statistic Standardized test statistic.

fold_data Per-fold results, including projections and scores.

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normalize_and_split

See Also

```
process_fold_mean_diff, combine_folds_mean_diff, estimate_leading_pc, fit_lasso
```

Examples

```
## Not run:
X <- matrix(rnorm(200 * 100), nrow = 100)
Y <- matrix(rnorm(200 * 100), nrow = 100)
result <- mean_comparison_anchor(X, Y, pca_method = "dense_pca", classifier_method = "lasso")
## End(Not run)
```

normalize_and_split Normalize and split two datasets using pooled mean and standard deviation

Description

Combines two datasets, normalizes features using pooled mean and standard deviation, and returns the normalized datasets separately.

Usage

```
normalize_and_split(df1, df2)
```

Arguments

df1	A data frame or matrix. Typically group 1.
df2	A data frame or matrix. Typically group 2.

Value

A list with elements:

- df1 Normalized version of df1.
- df2 Normalized version of df2.

```
set.seed(123)
df1 <- matrix(rnorm(20), nrow = 5)
df2 <- matrix(rnorm(20), nrow = 5)
normalize_and_split(df1, df2)</pre>
```

```
process_fold_mean_diff
```

Process one cross-validation fold for mean difference testing

Description

Computes the test statistic, variance, and projection direction for one fold in a cross-validated comparison of two groups.

Usage

```
process_fold_mean_diff(
   fold_index,
   control,
   treatment,
   control_split_index,
   tr_split_index,
   pca_method,
   classifier_method,
   lambda_type,
   group,
   verbose
)
```

Arguments

fold_index	Integer index of the current fold.			
control	Matrix or data frame for the control group (rows = samples, columns = features).			
treatment	Matrix or data frame for the treatment group (rows = samples, columns = features).			
<pre>control_split_i</pre>	index			
	A list of row indices for each fold of the control group.			
<pre>tr_split_index</pre>	A list of row indices for each fold of the treatment group.			
pca_method	Character. PCA method to use. Options are "dense_pca" or "sparse_pca".			
classifier_meth	nod			
	Character. Classifier method. Options are "lasso" or "group_lasso".			
lambda_type	Character. Lambda selection method. Options are "lambda.min" or "lambda.lse".			
group	Optional grouping vector for group lasso.			
verbose	Logical. Whether to print progress messages.			

Value

A list containing the test statistic, its variance, scores for each group, the projection direction, and intermediate quantities.

simple_pc_testing Simple plug-in test for two-sample mean comparison.

Description

Simple plug-in test for two-sample mean comparison.

Usage

```
simple_pc_testing(
  sample_1,
  sample_2 = NULL,
  pca_method = "sparse_pca",
  mean_method = "naive",
  num_latent_factor = 1,
  n_folds = 5,
  verbose = TRUE
)
```

Arguments

sample_1	Group 1 sample. Each row is a subject and each column corresponds to a feature.			
sample_2	Group 2 sample. Each row is a subject and each column corresponds to a feature.			
pca_method	Methods used to estimate principle component The default is "sparse_pca", us- ing sparse PCA from package PMA. Other choices are "dense_pca"—the regular PCA; and "hard"— hard-thresholding PCA, which also induces sparsity.			
mean_method	Methods used to estimate the mean vector. Default is sample mean "naive". There is also a hard-thresholding sparse estiamtor "hard".			
num_latent_fact	or			
	Number of principle to be estimated/tested. Default is 1.			
n_folds	Number of splits when performing cross-fitting. The default is 5, if computational time allows, you can try to set it to 10.			
verbose	Print information to the console. Default is TRUE.			

Value

A list of test statistics.

test_statistics	
	Test statistics. Each entry corresponds to the test result of one principle component.
	Estimated standard error of test_statistics_before_studentization.
test_statistics	<pre>s_before_studentization</pre>
	Similar to test_statistics but does not have variance = 1 .
split_data	Intermediate quantities needed for further assessment and interpretation of the test results.

Examples

```
sample_size_1 <- sample_size_2 <- 300</pre>
true_mean_1 <- matrix(c(rep(1, 10), rep(0, 90)), ncol = 1)</pre>
true_mean_2 <- matrix(c(rep(1.5, 10), rep(0, 90)), ncol = 1)</pre>
pc1 <- c(rep(1, 10), rep(0, 90))</pre>
pc1 <- pc1/norm(pc1, type = '2')</pre>
simulation_covariance <- 10 * pc1 %*% t(pc1)</pre>
simulation_covariance <- simulation_covariance + diag(1, 100)</pre>
sample_1 <- data.frame(MASS::mvrnorm(sample_size_1,</pre>
                                        mu = true_mean_1,
                                        Sigma = simulation_covariance))
sample_2 <- data.frame(MASS::mvrnorm(sample_size_2,</pre>
                                        mu = true_mean_2,
                                        Sigma = simulation_covariance))
result <- simple_pc_testing(sample_1, sample_2)</pre>
result$test_statistics
##these are test statistics. Each one of them corresponds to one PC.
summarize_pc_name(result, latent_fator_index = 1) #shows which features contribute to PC1
extract_pc(result) # extract the estimated leading PCs.
```

summarize_feature_name

Summarize the features (e.g. genes) that contribute to the test result, *i.e. those features consistently show up in Lasso vectors.*

Description

Summarize the features (e.g. genes) that contribute to the test result, i.e. those features consistently show up in Lasso vectors.

Usage

```
summarize_feature_name(testing_result, method = "majority voting")
```

Arguments

testing_result The output/test result list from anchored_lasso_testing().

method How to combine the feature list across different splits. Default is 'majority voting'—features that show up more than 50% of the splits are considered active/useful. It can be 'union'—all the features pooled together; or 'intersection' only include features showing up in all splits.

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A list of names of features (your very original input data need to have column names!) that contribute to the test result. An empty list means there is barely any difference between the two groups.

Feature names that consistently showing up in the discriminant vectors.

<pre>summarize_pc_name</pre>	Summarize the features (e.g. genes) that contribute to the test result,
	i.e. those features consistently show up in the sparse principle compo-
	nents.

Description

Summarize the features (e.g. genes) that contribute to the test result, i.e. those features consistently show up in the sparse principle components.

Usage

```
summarize_pc_name(
  testing_result,
  latent_fator_index = 1,
  method = "majority voting"
)
```

Arguments

 $\texttt{testing_result} \ \ The \ output/test \ result \ list \ from \ simple_pc_testing() \ or \ debiased_pc_testing().$

latent_fator_index

Which principle component should the algorithm summarize? Default is PC1.

method How to combine the feature list across different splits. Default is 'majority voting'—features that show up more than 50% of the splits are considered active/useful. It can be 'union'—all the features pooled together; or 'intersection' only include features showing up in all splits.

Value

A list of names of features (your very original input data need to have column names!) that contribute to the test result.

Feature names that consistently showing up in the estimated PC vectors.

validate_and_convert_data

Validate and convert input data

Description

Checks whether the input is a matrix or data frame, and converts it to a matrix if valid.

Usage

validate_and_convert_data(data, name)

Arguments

data	A matrix or data frame.
name	A string used in error messages to identify the variable name.

Value

A numeric matrix.

```
validate_and_convert_data(data.frame(x = 1:3, y = 4:6), "example_data")
```

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