Package 'Exact'

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```
Type Package
Title Unconditional Exact Test
Version 3.3
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Description Performs unconditional exact tests and power calculations for 2x2 contingency tables.
      For comparing two independent proportions, performs Barnard's test (1945)
      <doi:10.1038/156177a0> using the original CSM test (Barnard, 1947 <doi:10.1093/biomet/34.1-</p>
      2.123 > ),
      using Fisher's p-value referred to as Boschloo's test (1970) <doi:10.1111/j.1467-
      9574.1970.tb00104.x>,
      or using a Z-statistic (Suissa and Shuster, 1985, <doi:10.2307/2981892>).
      For comparing two binary proportions, performs unconditional exact test using McNemar's
      Z-statistic (Berger and Sidik, 2003, <doi:10.1191/0962280203sm312ra>),
      using McNemar's conditional p-value, using McNemar's Z-statistic with continuity correction,
      or using CSM test. Calculates confidence intervals for the difference in proportion.
      This package interacts with pre-computed data available through the ExactData R package,
      which is available in a 'drat' repository.
      Install the ExactData R package from GitHub at <a href="https://pcalhoun1.github.io/drat/">https://pcalhoun1.github.io/drat/</a>>.
      The ExactData R package is approximately 85 MB.
License GPL-2
Depends R (>= 3.5.0)
Imports graphics, stats, utils, rootSolve
Suggests ExactData
Additional_repositories https://pcalhoun1.github.io/drat
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Description

This package performs unconditional exact tests using exact.test for independent samples or paired.exact.test function for paired samples. The unconditional exact tests for independent samples are referred to as Barnard's (1945, 1947) test and also extended to test two paired proportions. This package also includes the power.exact.test and power.paired.test functions to calculate the power of various tests and the exact.reject.region and paired.reject.region functions to determine the rejection region of a test.

Details

Unconditional exact tests are a more powerful alternative than conditional exact tests. This package can compute p-values, confidence intervals, and power calculations for various tests. Details of the tests are given in the exact.test documentation for independent samples and paired.exact.test documentation for paired samples.

Note

Thoughout the years I have received help while creating this package. Special thanks goes to Philo Calhoun, Tal Galili, Kamil Erguler, Roger Berger, Karl Hufthammer, and the R community.

Author(s)

Peter Calhoun [aut, cre]

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References

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Barnard, G.A. (1947) Significance tests for 2x2 tables. *Biometrika*, 34, 123–138

Boschloo, R. D. (1970), Raised Conditional Level of Significance for the 2x2-table when Testing the Equality of Two Probabilities. *Statistica Neerlandica*, **24**, 1–35

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Berger, R.L. and Sidik, K. (2003) Exact unconditional tests for 2 x 2 matched-pairs design. *Statistical Methods in Medical Research*, **12**, 91–108

Hsueh, H., Liu, J., and Chen, J.J. (2001) Unconditional exact tests for equivalence or noninferiority for paired binary endpoints. *Biometrics*, **57**, 478–483

exact.reject.region Rejection Region for 2x2 Tables with Independent Samples

Description

Determines the rejection region for comparing two independent proportions.

Usage

Arguments

n1	The sample size in first group
n2	The sample size in second group
alternative	Indicates the alternative hypothesis: must be either "two.sided", "less", or "greater"
alpha	Significance level
npNumbers	Number: The number of nuisance parameters considered
np.interval	Logical: Indicates if a confidence interval on the nuisance parameter should be computed
beta	Number: Confidence level for constructing the interval of nuisance parameters considered. Only used if np.interval=TRUE
method	Indicates the method for finding the more extreme tables: must be either "Z-pooled", "Z-unpooled", "Santner and Snell", "Boschloo", "CSM", "Fisher", "Pearson Chisq", or "Yates Chisq"
tsmethod	Indicates two-sided method: must be either "square" or "central"
delta	Number: null hypothesis of the difference in proportion
convexity	Logical: assumes convexity for interval approach. Only used if np.interval=TRUE
useStoredCSM	Logical: uses stored CSM ordering matrix. Only used if method="csm"

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Details

The rejection region is calculated for binomial models with independent samples. The design must know the fixed sample sizes in advance. Rejection region can be determined for any unconditional exact test in exact.test, Fisher's exact test, or chi-square test (Yates' or Pearson's; note: these are not exact tests). In very rare cases, using the nuisance parameter interval approach does not attain the convexity property, so it is possible using convexity=TRUE could yield an inaccurate power calculation with this method. This is extremely unlikely though, so default is to assume convexity and speed up computation time. For details regarding parameters, see exact.test.

Value

A matrix of the rejection region. The columns represent the number of successes in first group, rows represent the number of successess in second group, and cells represent whether the test is rejected (1) or failed to be rejected (0). This matrix represents all possible 2x2 tables.

Note

Pearson's and Yates' chi-square tests are not exact tests, so the function name may be a misnomer. These tests may have inflated type 1 error rates. These options were added to compute the rejection region efficiently when using asymptotic tests.

Author(s)

Peter Calhoun

References

Barnard, G.A. (1947) Significance tests for 2x2 tables. Biometrika, 34, 123-138

Chan, I. (2003), Proving non-inferiority or equivalence of two treatments with dichotomous endpoints using exact methods, *Statistical Methods in Medical Research*, **12**, 37–58

See Also

```
power.exact.test
```

Examples

```
## Not run:
# Ensure that the ExactData R package is available before running the CSM test.
if (requireNamespace("ExactData", quietly = TRUE)) {
    exact.reject.region(n1=10, n2=20, alternative="two.sided", method="CSM")
}

## End(Not run)

exact.reject.region(n1=10, n2=20, alternative="less", method="Z-pooled", delta=0.10)
```

exact.test	Unconditional Exact Tests for 2x2 Tables with Independent Samples
	J 1

Description

Calculates Barnard's or Boschloo's unconditional exact test for binomial or multinomial models with independent samples

Usage

```
exact.test(data, alternative = c("two.sided", "less", "greater"), npNumbers = 100,
    np.interval = FALSE, beta = 0.001,
    method = c("z-pooled", "z-unpooled", "boschloo", "santner and snell", "csm"),
    model = c("Binomial", "Multinomial"), tsmethod = c("square", "central"),
    conf.int = FALSE, conf.level = 0.95,
    cond.row = TRUE, to.plot = TRUE, ref.pvalue = TRUE,
    delta = 0, reject.alpha = NULL, useStoredCSM = TRUE)
```

Arguments

data	A two dimensional contingency table in matrix form
alternative	Indicates the alternative hypothesis: must be either "two.sided", "less", or "greater"
npNumbers	Number: The number of nuisance parameters considered
np.interval	Logical: Indicates if a confidence interval on the nuisance parameter should be computed
beta	Number: Confidence level for constructing the interval of nuisance parameters considered. Only used if np.interval=TRUE
method	Indicates the method for finding the more extreme tables: must be either "Z-pooled", "Z-unpooled", "Santner and Snell", "Boschloo", or "CSM". CSM tests cannot be calculated for multinomial models
model	The model being used: must be either "Binomial" or "Multinomial"
tsmethod	Indicates two-sided method: must be either "square" or "central". Only used if model="Binomial"
conf.int	Logical: Indicates if a confidence interval on the difference in proportion should be computed. Only used if model="Binomial"
conf.level	Number: Confidence level of interval on difference in proportion. Only used if conf.int=TRUE
cond.row	Logical: Indicates if row margins are fixed in the binomial models. Only used if model="Binomial"
to.plot	Logical: Indicates if plot of p-value vs. nuisance parameter should be generated. Only used if model="Binomial"
ref.pvalue	Logical: Indicates if p-value should be refined by maximizing the p-value function after the nuisance parameter is selected. Only used if model="Binomial"

delta Number: null hypothesis of the difference in proportion. Only used if model="Binomial"

reject.alpha Number: significance level for exact test. Optional and primarily used to speed

up exact.reject.region function

useStoredCSM Logical: uses stored CSM ordering matrix. Only used if method="csm"

Details

Unconditional exact tests (i.e., Barnard's test) can be performed for binomial or multinomial models with independent samples. The binomial model assumes the row or column margins (but not both) are known in advance, while the multinomial model assumes only the total sample size is known beforehand. For the binomial model, the user needs to specify which margin is fixed (default is rows). Conditional tests (e.g., Fisher's exact test) have both row and column margins fixed, but this is a very uncommon design. For paired samples, see paired.exact.test.

For the binomial model, the null hypothesis is the difference of proportion is equal to 0. Under the null hypothesis, the probability of a 2x2 table is the product of two binomials. The p-value is calculated by maximizing a nuisance parameter and summing the as or more extreme tables. The method parameter specifies the method to determine the more extreme tables (see references for more details):

- Z-pooled (or Score) Uses the test statistic from a Z-test using a pooled proportion
- Z-unpooled Uses the test statistic from a Z-test without using the pooled proportion
- Santner and Snell Uses the difference in proportion
- Boschloo Uses the p-value from Fisher's exact test
- CSM Starts with the most extreme table and sequentially adds more extreme tables based on the smallest p-value (calculated by maximizing the probability of a 2x2 table). This is Barnard's original method

There is some disagreement on which method to use. Barnard's CSM (Convexity, Symmetry, and Minimization) test is often the most powerful test, but is much more computationally intensive. This test is recommended by Mato and Andres and the author of this R package when computationally feasible. Suissa and Shuster suggested using a Z-pooled statistic, which is uniformly more powerful than Fisher's test for balanced designs. Boschloo recommended using the p-value for Fisher's test as the test statistic. This method became known as Boschloo's test, and it is always uniformly more powerful than Fisher's test. Many researchers argue that Fisher's exact test should **never** be used to analyze 2x2 tables (except in the rare instance both margins are fixed).

Once the more extreme tables are determined, the p-value is calculated by maximizing over the common success probability — a nuisance parameter. The p-value computation has many local maxima and can be computationally intensive. The code performs an exhaustive search by considering many values of the nuisance parameter from 0 to 1, represented by npNumbers. If ref.pvalue = TRUE, then the code will also use the optimise function near the nuisance parameter to refine the p-value. Increasing npNumbers and using ref.pvalue ensures the p-value is correctly calculated at the expense of slightly more computation time.

Another approach, proposed by Berger and Boos, is to calculate the Clopper-Pearson confidence interval of the nuisance parameter (represented by np.interval) and only maximize the p-value function for nuisance parameters within the confidence interval; this approach adds a small penalty to the p-value to control for the type 1 error rate (cannot be used with CSM).

The tests can also be implemented for non-inferiority hypotheses by changing the delta for binomial models. A confidence interval for the difference in proportion can be constructed by determining the smallest delta such that all greater deltas are significant (essentially the delta that crosses from non-significant to significant, but since the p-value is non-monotonic as a function of delta, this code takes the supremum). For details regarding calculation, please see Chan (2003). We note the "z-pooled" method uses a delta-projected Z-statistic (aka Score) and uses a constrained MLE of the success proportions, while "boschloo" method ignores the delta and uses the same ordering procedure.

For two-sided tests, the code will either sum the probabilities for both sides of the table if tsmethod = "square" (Default, same approach as fisher.test) or construct a one-sided test and double the p-value if tsmethod = "central". Generally, the "square" procedure is more powerful and conventional, although there are some advantages with using the "central" procedure. Mainly, Boschloo's test cannot order tables (i.e., use Fisher's p-value) for a two-sided alternative with non-zero delta. Thus, to calculate a two-sided confidence interval with Boschloo's test, one has to resort to using the "central" approach. For other tests, there is an equivalent statistic based on delta, and the two-sided p-value is determined by either the Agresti-Min interval (tsmethod = "square") or Chan-Zhang interval (tsmethod = "central").

The CSM test is computationally intensive due to iteratively maximizing the p-value calculation to order the tables. The CSM ordering matrix has been stored for all possible sample sizes less than or equal to 100 (i.e., max(n1,n2)<=100). In addition, any table with (n1+1)x(n2+1)<=15,000 with a ratio between 1:1 and 2:1 is stored. Thus, using the useStoredCSM = TRUE can greatly improve computation time. However, the stored ordering matrix was computed with npNumbers=100 and it is possible that the ordering matrix was not optimal for larger npNumbers. Increasing npNumbers and setting useStoredCSM = FALSE ensures the p-value is correctly calculated at the expense of significantly greater computation time. The stored ordering matrix is not used in the calculation of confidence intervals or non-inferiority tests, so CSM can still be very computationally intensive.

The above description applies to the binomial model. The multinomial model is similar except there are two nuisance parameters. The CSM test has not been developed for multinomial models. Improvements to the code have focused on the binomial model, so multinomial models takes substantially longer.

Value

p.value

A list with class "htest" containing the following components:

The p-value of the test

The observed test statistic to determine more extreme tables

An estimate of the difference in proportion

The difference in proportion under the null

Conf.int A confidence interval for the difference in proportion. Only present if conf.int

TRUE

A character string describing the alternative hypothesis

model A character string describing the model design ("Binomial" or "Multinomial")

method A character string describing the method to determine more extreme tables

tsmethod A character string describing the method to implement two-sided tests. Only

present if model = "binomial"

np The nuisance parameter that maximizes the p-value. For multinomial models,

both nuisance parameters are given

np.range The range of nuisance parameters considered. For multinomial models, both

nuisance parameter ranges are given

data.name A character string giving the names of the data

parameter The sample sizes

Warning

Multinomial models and CSM tests with confidence intervals may take a very long time, even for small sample sizes.

Note

CSM test and multinomial models are much more computationally intensive. I have also spent a greater amount of time improving the computation speed and adding functionality to the binomial model. Increasing the number of nuisance parameters considered and refining the p-value will increase the computation time, but more likely to ensure accurate calculations. Performing confidence intervals also greatly increases computation time.

This code was influenced by the FORTRAN program located at https://www4.stat.ncsu.edu/ ~boos/exact/

Author(s)

Peter Calhoun

References

Agresti, A. and Min, Y. (2001) On small-sample confidence intervals for parameters in discrete distributions. *Biometrics*, **57**, 963–971

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Mehrotra, D., Chan, I., Berger, R. (2003), A Cautionary Note on Exact Unconditional Inference for a Difference Between Two Independent Binomial Proportions. *Biometrics*, **59**, 441–450

Ruxton, G. D. and Neuhauser M (2010), Good practice in testing for an association in contingency tables. *Behavioral Ecology and Sociobiology*, **64**, 1505–1513

Suissa, S. and Shuster, J. J. (1985), Exact Unconditional Sample Sizes for the 2x2 Binomial Trial, *Journal of the Royal Statistical Society, Ser. A*, **148**, 317–327

See Also

fisher.test and exact2x2

Examples

paired.exact.test

Unconditional Exact Tests for 2x2 Tables with Paired Samples

Description

Calculates unconditional exact test for paired samples

Usage

```
paired.exact.test(data, alternative = c("two.sided", "less", "greater"), npNumbers = 100,
    np.interval = FALSE, beta = 0.001,
    method = c("uam", "ucm", "uamcc", "csm"),
    tsmethod = c("square", "central"),
    conf.int = FALSE, conf.level = 0.95, to.plot = TRUE,
    ref.pvalue = TRUE, delta = 0,
    reject.alpha = NULL, useStoredCSM = TRUE)
```

Arguments

data	A two dimensional contingency table in matrix form
alternative	Indicates the alternative hypothesis: must be either "two.sided", "less", or "greater"
npNumbers	Number: The number of nuisance parameters considered
np.interval	Logical: Indicates if a confidence interval on the nuisance parameter should be computed
beta	Number: Confidence level for constructing the interval of nuisance parameters considered. Only used if np.interval=TRUE
method	Indicates the method for finding the more extreme tables: must be either "UAM", "UCM", "UAMCC", or "CSM"
tsmethod	A character string describing the method to implement two-sided tests.
conf.int	Logical: Indicates if a confidence interval on the difference in proportion should be computed
conf.level	Number: Confidence level of interval on difference in proportion. Only used if conf.int=TRUE
to.plot	Logical: Indicates if plot of p-value vs. nuisance parameter should be generated
ref.pvalue	Logical: Indicates if p-value should be refined by maximizing the p-value function after the nuisance parameter is selected
delta	Number: null hypothesis of the difference in proportion
reject.alpha	Number: significance level for exact test. Optional and primarily used to speed up paired.reject.region function
useStoredCSM	Logical: uses stored CSM ordering matrix. Only used if method="csm"

Details

This function performs unconditional exact tests to compare two paired proportions. The null hypothesis is the difference of two paired proportions is equal to 0. Under the null hypothesis, the probability of a 2x2 table is a trinomial distribution. The p-value is calculated by maximizing a nuisance parameter and summing the as or more extreme tables. The method parameter specifies the method to determine the more extreme tables (see references for more details):

- UAM (Unconditional Asymptotic McNemar) Uses McNemar's Z-statistic
- UCM (Unconditional Conditional McNemar) Uses McNemar's conditional p-value
- UAMCC (Unconditional Asyptotic McNemar with Continuity Correction) Uses McNemar's Z-statistic with Continuity Correction
- CSM Starts with the most extreme table and sequentially adds more extreme tables based on the smallest p-value (calculated by maximizing the probability of a 2x2 table). This is extending Barnard's original method to test two paired proportions

There is little research comparing two paired proportions. The author of this R package recommends using the CSM (Convexity, Symmetry, and Minimization) test as this test is often the most powerful, but is much more computationally intensive.

Once the more extreme tables are determined, the p-value is calculated by maximizing over the common discordant probability – a nuisance parameter. The p-value computation has many local

maxima and can be computationally intensive. The code performs an exhaustive search by considering many values of the nuisance parameter from 0 to 0.5, represented by npNumbers. If ref.pvalue = TRUE, then the code will also use the optimise function near the nuisance parameter to refine the p-value. Increasing npNumbers and using ref. pvalue ensures the p-value is correctly calculated at the expense of slightly more computation time.

Another approach, proposed by Berger and Sidik, is to calculate the Clopper-Pearson confidence interval of the nuisance parameter (represented by np.interval) and only maximize the p-value function for nuisance parameters within the confidence interval; this approach adds a small penalty to the p-value to control for the type 1 error rate (cannot be used with CSM). If the CSM test is too computationally intensive, the author of this R package generally recommends using the UAM test with confidence interval approach.

The tests can also be implemented for non-inferiority hypotheses by changing the delta. A confidence interval for the difference in proportion can be constructed by determining the smallest delta such that all greater deltas are significant (essentially the delta that crosses from non-significant to significant, but since the p-value is non-monotonic as a function of delta, this code takes the supremum). We note the "UAM" method uses a delta-projected Z-statistic, while "UCM" method ignores the delta and uses the same ordering procedure.

For two-sided tests, the code will either sum the probabilities for both sides of the table if tsmethod = "square" (Default) or construct a one-sided test and double the p-value if tsmethod = "central". The two methods give the same results when delta is zero. For a non-zero delta, the "square" procedure is generally more powerful and conventional, although there are some advantages with using the "central" procedure. Mainly, UCM test cannot order tables (i.e., use McNemar's conditional p-value) for a two-sided alternative with non-zero delta. Thus, to calculate a two-sided confidence interval with UCM test, one has to resort to using the "central" approach. For other tests, there is an equivalent statistic based on delta, and the two-sided p-value is determined by either the Agresti-Min interval (tsmethod = "square") or Chan-Zhang interval (tsmethod = "central").

The CSM test is computationally intensive due to iteratively maximizing the p-value calculation to order the tables. The CSM ordering matrix has been stored for total sample sizes less than or equal to 200. Thus, using the useStoredCSM = TRUE can greatly improve computation time. However, the stored ordering matrix was computed with npNumbers=100 and it is possible that the ordering matrix was not optimal for larger npNumbers. Increasing npNumbers and setting useStoredCSM = FALSE ensures the p-value is correctly calculated at the expense of significantly greater computation time. The stored ordering matrix is not used in the calculation of confidence intervals or noninferiority tests, so CSM can still be very computationally intensive.

Value

A list with class "htest" containing the following components:

p.value	The p-value of the test
statistic	The observed test statistic to determine more extreme tables
estimate	An estimate of the difference in proportion
null.value	The difference in proportion under the null
conf.int	A confidence interval for the difference in proportion. Only present if ${\tt conf.int}$ = TRUE
alternative	A character string describing the alternative hypothesis

method	A character string describing the method to determine more extreme tables
tsmethod	A character string describing the method to implement two-sided tests
np	The nuisance parameter that maximizes the p-value
np.range	The range of nuisance parameters considered
data.name	A character string giving the names of the data
parameter	The sample sizes

Warning

CSM tests with confidence intervals may take a very long time, even for small sample sizes.

Note

CSM test is much more computationally intensive. Increasing the number of nuisance parameters considered and refining the p-value will increase the computation time, but more likely to ensure accurate calculations. Performing confidence intervals also greatly increases computation time.

Author(s)

Peter Calhoun

References

Berger, R.L. and Sidik, K. (2003) Exact unconditional tests for 2 x 2 matched-pairs design. *Statistical Methods in Medical Research*, **12**, 91–108

Hsueh, H., Liu, J., and Chen, J.J. (2001) Unconditional exact tests for equivalence or noninferiority for paired binary endpoints. *Biometrics*, **57**, 478–483

See Also

```
mcnemar.test and exact2x2
```

Examples

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paired.reject.region Rejection Region for 2x2 Tables with Paired Samples

Description

Determines the rejection region for comparing two paired proportions.

Usage

```
paired.reject.region(N, alternative = c("two.sided", "less", "greater"),
    alpha = 0.05, npNumbers = 100, np.interval = FALSE, beta = 0.001,
    method = c("uam", "ucm", "uamcc", "csm", "cm", "am", "amcc"),
    tsmethod = c("square", "central"),
    delta = 0, convexity = TRUE, useStoredCSM = TRUE)
```

Arguments

N	The total sample size
alternative	Indicates the alternative hypothesis: must be either "two.sided", "less", or "greater"
alpha	Significance level
npNumbers	Number: The number of nuisance parameters considered
np.interval	Logical: Indicates if a confidence interval on the nuisance parameter should be computed
beta	Number: Confidence level for constructing the interval of nuisance parameters considered. Only used if np.interval=TRUE
method	Indicates the method for finding the more extreme tables: must be either "UAM", "UCM", "UAMCC", "CSM", "CM", "AM", or "AMCC"
tsmethod	A character string describing the method to implement two-sided tests
delta	Number: null hypothesis of the difference in proportion
convexity	Logical: assumes convexity for interval approach. Only used if np.interval=TRUE
useStoredCSM	Logical: uses stored CSM ordering matrix. Only used if method="csm"

Details

The rejection region is calculated for paired samples. Rejection region can be determined for any unconditional exact test in paired.exact.test, the Conditional McNemar's (CM) exact test, the Asymptotic McNemar's (AM) test, or Asymptotic McNemar's test with Continuity Correction (AMCC) (note: asymptotic tests are not exact tests). In very rare cases, using the nuisance parameter interval approach does not attain the convexity property, so it is possible using convexity=TRUE could yield an inaccurate power calculation with this method. This is extremely unlikely though, so default is to assume convexity and speed up computation time. For details regarding parameters, see paired.exact.test.

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Value

A matrix of the rejection region. The rows and columns represent the discordant pairs. Specifically, the columns represent x12, the number of successes in first group and number of failures in second group, and rows represent x21, the number of failures in first group and number of successes in second group. The number of concordant pairs is simply the total sample size minus number of discordant pairs. The cells represent whether the test is rejected (1) or failed to be rejected (0). Values with an NA are not possible. This matrix represents all possible 2x2 tables.

Note

McNemar's asymptotic tests are not exact test and may have inflated type 1 error rates. These options were added to compute the rejection region efficiently when using asymptotic tests.

Author(s)

Peter Calhoun

See Also

```
power.paired.test
```

Examples

```
## Not run:
# Ensure that the ExactData R package is available before running the CSM test.
if (requireNamespace("ExactData", quietly = TRUE)) {
  paired.reject.region(N=15, alternative="two.sided", method="CSM")
}

## End(Not run)
paired.reject.region(N=15, alternative="less", method="UAM", delta=0.10)
```

power.exact.test

Power Calculations for 2x2 Tables with Independent Samples

Description

Calculates the power of the design for known sample sizes and true probabilities.

Usage

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The probability of success given in first group

Arguments p1

p2	The probability of success given in second group
n1	The sample size in first group
n2	The sample size in second group
alternative	Indicates the alternative hypothesis: must be either "two.sided", "less", or "greater"
alpha	Significance level
npNumbers	Number: The number of nuisance parameters considered
np.interval	Logical: Indicates if a confidence interval on the nuisance parameter should be computed
beta	Number: Confidence level for constructing the interval of nuisance parameters considered. Only used if np.interval=TRUE
method	Indicates the method for finding more extreme tables: must be either "Z-pooled", "Z-unpooled", "Santner and Snell", "Boschloo", "CSM", "Fisher", "Pearson Chisq", or "Yates Chisq"

tsmethod Indicates two-sided method: must be either "square" or "central"

simulation Logical: Indicates if the power calculation is exact or estimated by simulation

nsim Number of simulations run. Only used if simulation=TRUE
delta Number: null hypothesis of the difference in proportion

convexity Logical: assumes convexity for interval approach. Only used if np.interval=TRUE

useStoredCSM Logical: uses stored CSM ordering matrix. Only used if method="csm"

Details

The power calculations are for binomial models with independent samples. The design must know the fixed sample sizes in advance. There are (n1+1) x (n2+1) possible tables that could be produced. There are two ways to calculate the power: simulate the tables under two independent binomial distributions or determine the rejection region for all possible tables and calculate the exact power. The calculations can be done using any exact.test computation, Fisher's exact test, or chi-square tests (Yates' or Pearson's; note: these are not exact tests). The power calculations utilize the convexity property, which greatly speeds up computation time (see exact.reject.region documentation).

Value

A list with class "power.htest" containing the following components:

n1, n2 The respective sample sizes
 p1, p2 The respective success probabilities
 alpha Significance level

power Power of the test

alternative A character string describing the alternative hypothesis

delta Null hypothesis of the difference in proportion

method A character string describing the method to determine more extreme tables

power.paired.test

Note

Pearson's and Yates' chi-square tests are not exact tests, so the function name may be a misnomer. These tests may have inflated type 1 error rates. These options were added to compute the power efficiently when using asymptotic tests.

Author(s)

Peter Calhoun

References

Berger, R. (1994) Power comparison of exact unconditional tests for comparing two binomial proportions. *Institute of Statistics Mimeo Series No.* 2266

Berger, R. (1996) More powerful tests from confidence interval p values. *American Statistician*, **50**, 314-318

Boschloo, R. D. (1970), Raised Conditional Level of Significance for the 2x2-table when Testing the Equality of Two Probabilities. *Statistica Neerlandica*, **24**, 1-35

See Also

```
exact.reject.region and statmod
```

Examples

power.paired.test

Power Calculations for 2x2 Tables with Paired Samples

Description

Calculates the power of the design for known sample size and true probabilities.

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Usage

```
power.paired.test(p12, p21, N, alternative = c("two.sided", "less", "greater"),
    alpha = 0.05, npNumbers = 100, np.interval = FALSE, beta = 0.001,
    method = c("uam", "ucm", "uamcc", "csm", "cm", "am", "amcc"),
    tsmethod = c("square", "central"),
    simulation = FALSE, nsim = 100,
    delta = 0, convexity = TRUE, useStoredCSM = TRUE)
```

Arguments

p12	The probability of success in first group and failure in second group. This is the probability of the discordant pair x12
p21	The probability of failure in first group and success in second group. This is the probability of the discordant pair x21
N	The total sample size
alternative	Indicates the alternative hypothesis: must be either "two.sided", "less", or "greater"
alpha	Significance level
npNumbers	Number: The number of nuisance parameters considered
np.interval	Logical: Indicates if a confidence interval on the nuisance parameter should be computed
beta	Number: Confidence level for constructing the interval of nuisance parameters considered. Only used if np.interval=TRUE
method	Indicates the method for finding the more extreme tables: must be either "UAM", "UCM", "UAMCC", "CSM", "CM", "AM", or "AMCC"
tsmethod	A character string describing the method to implement two-sided tests
simulation	Logical: Indicates if the power calculation is exact or estimated by simulation
nsim	Number of simulations run. Only used if simulation=TRUE
delta	Number: null hypothesis of the difference in proportion
convexity	Logical: assumes convexity for interval approach. Only used if np.interval=TRUE
useStoredCSM	Logical: uses stored CSM ordering matrix. Only used if method="csm"

Details

The power calculations are for paired samples. All possible tables can be represented by an (N+1) x (N+1) matrix. There are two ways to calculate the power: simulate the tables under a trinomial distribution or determine the rejection region for all possible tables and calculate the exact power. The power calculations can be determined for any unconditional exact test in paired.exact.test, the Conditional McNemar's (CM) exact test, the Asymptotic McNemar's (AM) test, or Asymptotic McNemar's test with Continuity Correction (AMCC) (note: asymptotic tests are not exact tests). The power calculations utilize the convexity property, which greatly speeds up computation time (see paired.reject.region documentation).

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Value

A list with class "power.htest" containing the following components:

N The total sample size

p12, p21 The respective discordant probabilities

alpha Significance level power Power of the test

alternative A character string describing the alternative hypothesis

delta Null hypothesis of the difference in proportion

method A character string describing the method to determine more extreme tables

Note

McNemar's asymptotic tests are not exact test and may have inflated type 1 error rates. These options were added to compute the power efficiently when using asymptotic tests.

Author(s)

Peter Calhoun

References

Berger, R.L. and Sidik, K. (2003) Exact unconditional tests for 2 x 2 matched-pairs design. *Statistical Methods in Medical Research*, **12**, 91–108

See Also

```
paired.reject.region
```

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