

Package ‘ERP’

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Type Package

Title Significance Analysis of Event-Related Potentials Data

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Imports graphics,grDevices,stats,corpcor,irlba,fdrtool,splines,mnormt,pacman

Description Functions for signal detection and identification designed for Event-Related Potentials (ERP) data in a linear model framework. The functional F-test proposed in Causeur, Sheu, Perthame, Rufini (2018, submitted) for analysis of variance issues in ERP designs is implemented for signal detection (tests for mean difference among groups of curves in One-way ANOVA designs for example). Once an experimental effect is declared significant, identification of significant intervals is achieved by the multiple testing procedures reviewed and compared in Sheu, Perthame, Lee and Causeur (2016, <[DOI:10.1214/15-AOAS888](#)>). Some of the methods gathered in the package are the classical FDR- and FWER-controlling procedures, also available using function `p.adjust`. The package also implements the Guthrie-Buchwald procedure (Guthrie and Buchwald, 1991 <[DOI:10.1111/j.1469-8986.1991.tb00417.x](#)>), which accounts for the auto-correlation among t-tests to control erroneous detection of short intervals. The Adaptive Factor-Adjustment method is an extension of the method described in Causeur, Chu, Hsieh and Sheu (2012, <[DOI:10.3758/s13428-012-0230-0](#)>). It assumes a factor model for the correlation among tests and combines adaptively the estimation of the signal and the updating of the dependence modelling (see Sheu et al., 2016, <[DOI:10.1214/15-AOAS888](#)> for further details).

License GPL (>= 2)

URL <http://erpinr.org>

Suggests prettydoc, knitr, rmarkdown

VignetteBuilder knitr

NeedsCompilation no

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Contents

| | |
|--------------|-----------|
| ERP-package | 2 |
| emfa | 6 |
| erpavetest | 7 |
| erpfatest | 9 |
| erpFtest | 13 |
| erpplot | 15 |
| erptest | 17 |
| gbtest | 19 |
| ifa | 21 |
| impulsivity | 22 |
| isqrtfa | 23 |
| nbfactors | 24 |
| Index | 26 |

| | |
|-------------|---|
| ERP-package | <i>Significance Analysis of Event-Related Potentials Data: Significance Analysis of Event-Related Potentials Data</i> |
|-------------|---|

Description

Functions for signal detection and identification designed for Event-Related Potentials (ERP) data in a linear model framework. The functional F-test proposed in Causeur, Sheu, Perthame, Rufini (2018, submitted) for analysis of variance issues in ERP designs is implemented for signal detection (tests for mean difference among groups of curves in One-way ANOVA designs for example). Once an experimental effect is declared significant, identification of significant intervals is achieved by the multiple testing procedures reviewed and compared in Sheu, Perthame, Lee and Causeur (2016, <DOI:10.1214/15-AOAS888>). Some of the methods gathered in the package are the classical FDR- and FWER-controlling procedures, also available using function `p.adjust`. The package also implements the Guthrie-Buchwald procedure (Guthrie and Buchwald, 1991 <DOI:10.1111/j.1469-8986.1991.tb00417.x>), which accounts for the auto-correlation among t-tests to control erroneous detection of short intervals. The Adaptive Factor-Adjustment method is an extension of the method described in Causeur, Chu, Hsieh and Sheu (2012, <DOI:10.3758/s13428-012-0230-0>). It assumes a factor model for the correlation among tests and combines adaptively the estimation of the signal and the updating of the dependence modelling (see Sheu et al., 2016, <DOI:10.1214/15-AOAS888> for further details).: This package provides testing procedures designed for Event-Related Potentials (ERP) data in a linear model framework. The functional F-test proposed in Causeur, Sheu, Perthame, Rufini (2018) for analysis of variance issues in ERP designs is implemented for signal detection (tests for mean difference among groups of curves in One-way ANOVA designs for example). Once an experimental effect is declared significant, identification of significant intervals is achieved by the multiple testing procedures reviewed and compared in Sheu, Perthame, Lee and Causeur (2016, <DOI: 10.1214/15-AOAS888>). Some of the methods gathered in the package are the classical FDR- and FWER-controlling procedures, also available using function `p.adjust`. The package also implements the Guthrie-Buchwald procedure (Guthrie and Buchwald, 1991, <DOI: 10.1111/j.1469-8986.1991.tb00417.x>), which accounts for the auto-correlation among t-tests to control erroneous detection of short intervals. The Adaptive Factor-Adjustment

method is an extension of the method described in Causeur, Chu, Hsieh and Sheu (2012, <DOI: 10.3758/s13428-012-0230-0>). It assumes a factor model for the correlation among tests and combines adaptively the estimation of the signal and the updating of the dependence modelling (see Sheu et al., 2016, <DOI: 10.1214/15-AOAS888> for further details).

Details

The DESCRIPTION file:

```
Package:      ERP
Type:         Package
Title:        Significance Analysis of Event-Related Potentials Data
Version:      2.2
Date:         2019-12-10
Author:       David Causeur, Ching-Fan Sheu, Mei-Chen Chu, Flavia Rufini
Maintainer:   David Causeur <david.causeur@agrocampus-ouest.fr>
Depends:      R (>= 3.0.0)
Imports:      graphics,grDevices,stats,corpcor,irlba,fdrtool,splines,mnormt,pacman
Description:  Functions for signal detection and identification designed for Event-Related Potentials (ERP) data in a line
License:      GPL (>=2)
URL:          http://erpinr.org
Suggests:     prettydoc,knitr,rmarkdown
VignetteBuilder: knitr
```

Index of help topics:

| | |
|-------------|--|
| ERP-package | Significance Analysis of Event-Related Potentials Data: Significance Analysis of Event-Related Potentials Data |
| emfa | Expectation-Maximization (EM) estimation of a factor model. |
| erpFtest | Functional Analysis-of-Variance (Anova) testing of Event-Related Potentials (ERP) data |
| erpavetest | Significance testing of averaged ERPs. |
| erpfatest | Adaptive Factor-Adjustement for multiple testing of ERP data |
| erpplot | Plot of ERP curves or effect curves (difference curve for example) with confidence intervals. |
| erptest | FDR- and FWER-controlling Multiple testing of ERP data |
| gbtest | The Guthrie-Buchwald procedure for significance analysis of ERP data |
| ifa | Inverse of a matrix based on its factor decomposition. |
| impulsivity | Event-Related Potentials data from a study conducted by Shen et al. (2014) to investigate neural correlates of impulsive behavior. |
| isqrtfa | Inverse square-root of a matrix based on its |

nbfactors factor decomposition.
 Determination of the number of factors in high
 dimensional factor models.

This package is designed to help making decision about the position on the brain and the time interval after the onset where an effect is significant. The function `erpplot` can be used to display the ERP curves in an exploratory purpose or to plot effect curves (difference curve among experimental groups for example), with or without smoothing options and confidence intervals. All the other functions implement testing procedures of ERP data in a linear model framework (F-tests for the comparison of two nested models). The function `gbtest` implements the Guthrie-Buchwald procedure (see Guthrie and Buchwald, 1991). The function `erpavetest` first partitions the entire interval of ERP observations into a predetermined number of equally-spaced intervals before performing significance testing using the averaged ERPs. The function `erpctest` can be used for the classical FDR- and FWER-controlling multiple testing of ERP data: especially the Benjamini-Hochberg (see Benjamini and Hochberg, 1995) and Benjamini-Yekutieli (see Benjamini and Yekutieli, 2001) procedures, with the possible extension proposed by Storey and Tibshirani (2003) including a non-parametric estimation of the proportion of true nulls. Finally, `erpFtest` is designed for functional F-tests in ERP designs using the generalized likelihood-ratio test proposed by Causeur et al. (2018) and `erpfastest` for the identification of significant intervals with FDR control using the adaptive factor-adjustment (AFA) multiple testing procedure proposed by Sheu et al. (2016).

Author(s)

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- Causeur, D., Chu, M.-C., Hsieh, S. and Sheu, C.-F. (2012). A factor-adjusted multiple testing procedure for ERP data analysis. *Behavior Research Methods*, 44, 635-643.
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- Shen, I. H., Lee, D. S. and Chen, C. L. (2014). The role of trait impulsivity in response inhibition: event-related potentials in a stop-signal task. *International Journal of Psychophysiology* 91.
- Sheu, C.-F., Perthame, E., Lee, Y.-S., Causeur, D. (2016). Accounting for time dependence in large-scale multiple testing of event-related potential data. *Annals of Applied Statistics*. 10(1), 219-245.
- Wright, S. P. (1992). Adjusted P-values for simultaneous inference. *Biometrics*, 48, 1005-1013.

Examples

```
## Not run:

data(impulsivity)

# Paired t-tests for the comparison of the ERP curves in the two conditions,
# within experimental group High, at channel CPZ

erpdata.highCPZ = impulsivity[(impulsivity$Group=="High")&(impulsivity$Channel=="CPZ"),5:505]
# ERP curves for subjects in group 'High'
covariates.highCPZ = impulsivity[(impulsivity$Group=="High")&(impulsivity$Channel=="CPZ"),1:4]
covariates.highCPZ = droplevels(covariates.highCPZ)
# Experimental covariates for subjects in group High

design = model.matrix(~C(Subject,sum)+Condition,data=covariates.highCPZ)
# Design matrix to compare ERP curves in the two conditions
design0 = model.matrix(~C(Subject,sum),data=covariates.highCPZ)
# Design matrix for the null model (no condition effect)

tests = erpfatest(erpdata.highCPZ,design,design0,nbf=NULL,wantplot=TRUE,significance="none")
# with significance="none", just to choose a number of factors
Ftest = erpFtest(erpdata.highCPZ,design,design0,nbf=6)
Ftest$pval
tests = erpfatest(erpdata.highCPZ,design,design0,nbf=6)
# with nbf=6 (approximate conservative recommendation based on the variance inflation plot)

time_pt = seq(0,1000,2) # Sequence of time points (1 time point every 2ms in [0,1000])
nbs = 20 # Number of B-splines for the plot of the effect curve
effect=which(colnames(design)=="ConditionSuccess")
erpplot(erpdata.highCPZ,design=design,frames=time_pt,effect=effect,xlab="Time (ms)",
        ylab=expression(Effect~curve~(mu~V)),bty="l",ylim=c(-3,3),nbs=nbs,
        cex.axis=1.25,cex.lab=1.25,interval="simultaneous")
```

```

# with interval="simultaneous", both the pointwise and the simultaneous confidence bands
# are plotted
points(time_pt[tests$significant],rep(0,length(tests$significant)),pch=16,col="blue")
# Identifies significant time points by blue dots
title("Success-Failure effect curve with 95 percent C.I.",cex.main=1.25)
mtext(paste("12 subjects - Group High - ",nbs," B-splines",sep=""),cex=1.25)

## End(Not run)

```

emfa

Expectation-Maximization (EM) estimation of a factor model.

Description

This function implements the EM algorithm by Thayer and Rubin (1982) for the ML estimation of a factor model. It is an internal function used to estimate the factor model parameters in the factor-adjustment methods.

Usage

```
emfa(dta, nbf, min.err = 1e-06, verbose = FALSE, svd.method = c("fast.svd", "irlba"))
```

Arguments

| | |
|------------|--|
| dta | n x m matrix which rows are multivariate m-profiles for n individuals. n can be much smaller than m. |
| nbf | number of factors. It has to be a positive integer, smaller than the rank of dta. |
| min.err | stopping criterion for the iterative algorithm. Maximum difference between the estimated parameters in the last two iterations. |
| verbose | logical value. If verbose=TRUE, then some information is printed along the calculation. |
| svd.method | the EM algorithm starts from an SVD estimation of the factor model parameters. The default option to implement this SVD is fast.svd . An alternative option is an approximate but faster SVD by function irlba . |

Details

Data are centered but not scaled. If a factor model for a correlation matrix is to be estimated, then a scaled dataset is required as an input of the function.

Value

| | |
|-----------|---|
| B | m x nbf matrix of loadings |
| Psi | m-vector of specific variances |
| Factors | n x nbf matrix of factor scores |
| Objective | Final value of the stopping criterion, after convergence. |

Author(s)

David Causeur, IRMAR, UMR 6625 CNRS, Agrocampus Ouest, Rennes, France.

References

Friguet, C., Kloareg, M. and Causeur, D. (2009). A factor model approach to multiple testing under dependence. *Journal of the American Statistical Association*. 104 (488), 1406-1415.

Rubin, D. B., and Thayer, D. T. (1982), EM Algorithms for ML Factor Analysis, *Psychometrika*, 47 (1), 69-76.

See Also

[factanal](#)

Examples

```
data(impulsivity)

erpdt = as.matrix(impulsivity[,5:505]) # erpdt contains the whole set of ERP curves

fa = emfa(erpdt,nbf=1) # 1-factor modelling of the ERP curves
fa$Objective           # Final difference between the last two iterations
Semp = var(erpdt)      # Sample estimation of the variance of ERP curves
Sfa = diag(fa$Psi)+tcrossprod(fa$B) # Factorial estimation of the variance
max(abs(Semp-Sfa))     # Distance between the two estimates

fa = emfa(erpdt,nbf=20) # 20-factor modelling of the ERP curves in erpdt
fa$Objective           # Final difference between the last two iterations
Semp = var(erpdt)      # Sample estimation of the variance of ERP curves
Sfa = diag(fa$Psi)+tcrossprod(fa$B) # Factorial estimation of the variance
max(abs(Semp-Sfa))     # Distance between the two estimates
```

erpavetest

Significance testing of averaged ERPs.

Description

The function first calculates averaged ERP values within a predetermined number of equally-spaced intervals then tests for significance of the relationship between averaged ERPs and covariates in a linear model framework.

Usage

```
erpavetest(dta, design, design0 = NULL, nintervals = 10,
method = c("none", "BH", "holm", "hochberg", "hommel", "bonferroni", "BY", "fdr"), alpha = 0.05)
```

Arguments

| | |
|------------|---|
| dta | Data frame containing the ERP curves: each column corresponds to a time frame and each row to a curve. |
| design | Design matrix of the nonnull model for the relationship between the ERP and the experimental variables. Typically the output of the function <code>model.matrix</code> |
| design0 | Design matrix of the null model. Typically a submodel of the nonnull model, obtained by removing columns from <code>design</code> . Default is <code>NULL</code> , corresponding to the model with no covariates. |
| nintervals | Number of intervals in the partition of the whole interval of observation. Default is 10. |
| method | FDR- or FWER- controlling multiple testing procedures as available in the function <code>p.adjust</code> . Default is "none", for no multiplicity correction. |
| alpha | The FDR or FWER control level. Default is 0.05 |

Value

| | |
|---------------|--|
| pval | p-values of the tests. |
| correctedpval | Corrected p-values, for the multiplicity of tests. Depends on the multiple testing method (see function <code>p.adjust</code>). |
| significant | Indices of the time points for which the test is positive. |
| segments | Factor giving the membership of timepoints to each interval in the partition. |
| breaks | Breakpoints of the partition. |
| test | Pointwise F-statistics if $p > 1$, where p is the difference between the numbers of parameters in the nonnull and null models. Otherwise, if $p = 1$, the function returns pointwise t-statistics (signed square-roots of F-statistics). |
| df1 | Residual degrees of freedom for the nonnull model. |
| df0 | Residual degrees of freedom for the null model. |
| signal | Estimated signal: a $p \times T$ matrix, where T the number of frames. |
| r2 | R-squared values for each of the T linear models. |

Author(s)

David Causeur, IRMAR, UMR 6625 CNRS, Agrocampus Ouest, Rennes, France.

See Also

[erpptest](#), [erpfatest](#), [gbtest](#), [p.adjust](#)

Examples

```
data(impulsivity)

# Paired t-tests for the comparison of the ERP curves in the two conditions,
# within experimental group High, at channel CPZ
```



```

erpdt.high = impulsivity[impulsivity$Group=="High",5:505]
# ERP curves for subjects in group 'High'
covariates.high = impulsivity[impulsivity$Group=="High",1:4]
# Experimental covariates for subjects in group 'High'

design = model.matrix(~C(Subject,sum)+Condition,data=covariates.high)
# Design matrix to compare ERP curves in the two conditions
design0 = model.matrix(~C(Subject,sum),data=covariates.high)
# Design matrix for the null model (no condition effect)

tests = erpavetest(erpdt.high,design,design0)

time_pt = seq(0,1000,2) # sequence of time points (1 time point every 2ms in [0,1000])
nbs = 20 # Number of B-splines for the plot of the effect curve
effect=which(colnames(design)=="ConditionSuccess")
erpplot(erpdt.high,design=design,frames=time_pt,effect=effect,xlab="Time (ms)",
        ylab=expression(Effect~curve~(mu~V)),bty="l",ylim=c(-3,3),nbs=nbs,
        cex.axis=1.25,cex.lab=1.25,interval="simultaneous")
# with interval="simultaneous", both the pointwise and the simultaneous confidence bands
# are plotted
abline(v=time_pt[tests$breaks],lty=2,col="darkgray")
# Add a grid to show breakpoints
points(time_pt[tests$significant],rep(0,length(tests$significant)),pch=16,col="blue")
# Identifies significant time points by blue dots
title("Success-Failure effect curve with 95 percent C.I.",cex.main=1.25)
mtext(paste("12 subjects - Group 'High' - ",nbs," B-splines",sep=""),cex=1.25)

```

erpfatest

Adaptive Factor-Adjustment for multiple testing of ERP data

Description

Adaptive factor-adjusted FDR- and FWER-controlling multiple testing procedures for ERP data. The procedure is described in detail in Sheu, Perthame, Lee, and Causeur (2016).

Usage

```

erpfatest(dta, design, design0 = NULL,
method = c("BH", "holm", "hochberg", "hommel", "bonferroni", "BY", "fdr", "none"), nbf = NULL,
nsamples = 200, significance = c("Satterthwaite", "none"),
nbxmax = min(c(nsamples, nrow(design))) - ncol(design) - 1, alpha = 0.05, pi0 = 1,
wantplot = ifelse(is.null(nbf), TRUE, FALSE), s0 = NULL, min.err = 0.01, maxiter = 5,
verbose = FALSE, svd.method = c("fast.svd", "irlba"))

```

Arguments

dta Data frame containing the ERP measurements: each column corresponds to a time frame and each row to a curve.

| | |
|--------------|--|
| design | Design matrix of the nonnull model for the relationship between the ERP and the experimental variables. Typically the output of the function <code>model.matrix</code> |
| design0 | Design matrix of the null model. Typically a submodel of the nonnull model, obtained by removing columns from <code>design</code> . Default is <code>NULL</code> , corresponding to the model with no covariates. |
| method | FDR- or FWER- controlling multiple testing procedures as available in the function <code>p.adjust</code> . Default is "BH", for the Benjamini-Hochberg procedure (see Benjamini and Hochberg, 1995). |
| nbf | Number of factors in the residual covariance model. Default is <code>NULL</code> : the number of factors is determined by minimization of the variance inflation criterion as suggested in Friguet et al. (2009). |
| nsamples | Number of Monte-Carlo samples for the estimation of the null distribution. Default is <code>nsamples=200</code> , recommended when the Satterthwaite approximation is used. |
| significance | If "Satterthwaite", then the Monte-Carlo p-value is calculated with a Satterthwaite approximation of the null distribution. The other possible value is "none", for no calculation of the p-value. |
| nbfmax | Only required if <code>nbf=NULL</code> . The largest possible number of factors. |
| alpha | The FDR or FWER control level. Default is 0.05 |
| pi0 | An estimate of the proportion of true null hypotheses, which can be plugged into an FDR controlling multiple testing procedure to improve its efficiency. Default is 1, corresponding to the classical FDR controlling procedures. If <code>NULL</code> , the proportion is estimated using the function <code>pval.estimate.eta0</code> of package <code>fdrtol</code> , with the method proposed by Storey and Tibshirani (2003). |
| wantplot | If <code>TRUE</code> , a diagnostic plot is produced to help choosing the number of factors. Only active if <code>nbf=NULL</code> . |
| s0 | Prior knowledge of the time frames for which no signal is expected. For example, <code>s0=c(1:50, 226:251)</code> specifies that the first 50 time frames and time frames between 226 and 251 are known not to contain ERP signal. <code>s0</code> can also be specified by giving the lower and upper fraction of the entire time interval in which the signal is to be searched for. For example: <code>s0=c(0.2, 0.9)</code> means that ERP signals are not expected for for the first 20 percent and last 10 percent of the time frames measured. Default is <code>NULL</code> and it initiates a data-driven determination of <code>s0</code> . |
| min.err | Control parameter for convergence of the iterative algorithm. Default is 1e-03. |
| maxiter | Maximum number of iterations in algorithms. Default is 5. |
| verbose | If <code>TRUE</code> , details are printed along the iterations of the algorithm. Default is <code>FALSE</code> . |
| svd.method | the EM algorithm starts from an SVD estimation of the factor model parameters. The default option to implement this SVD is <code>fast.svd</code> . An alternative option is an approximate but faster SVD by function <code>irlba</code> . |

Details

The method is described in Sheu et al. (2016). It combines a decorrelation step based on a regression factor model as in Leek and Storey (2008), Friguet et al. (2009) or Sun et al. (2012) with an adaptive estimation of the ERP signal. The multiple testing corrections of the p-values are described in the help documentation of the function `p.adjust`.

Value

| | |
|----------------------------|--|
| <code>pval</code> | p-values of the Adaptive Factor-Adjusted tests. |
| <code>correctedpval</code> | Corrected p-values, for the multiplicity of tests. Depends on the multiple testing method (see function <code>p.adjust</code>). |
| <code>significant</code> | Indices of the time points for which the test is positive. |
| <code>pi0</code> | Value for π_0 : if the input argument <code>pi0</code> is NULL, the output is the estimated proportion of true null hypotheses using the method by Storey and Tibshirani (2003). |
| <code>test</code> | Pointwise factor-adjusted F-statistics if $p > 1$, where p is the difference between the numbers of parameters in the nonnull and null models. Otherwise, if $p = 1$, the function returns pointwise factor adjusted t-statistics (signed square-roots of F-statistics). |
| <code>df1</code> | Residual degrees of freedom for the nonnull model. |
| <code>df0</code> | Residual degrees of freedom for the null model. |
| <code>nbf</code> | Number of factors for the residual covariance model. |
| <code>signal</code> | Estimated signal: a $p \times T$ matrix, where p is the difference between the numbers of parameters in the nonnull and null models and T the number of frames. |
| <code>r2</code> | R-squared values for each of the T linear models. |

Author(s)

David Causeur, IRMAR, UMR 6625 CNRS, Agrocampus Ouest, Rennes, France.

References

- Causeur, D., Chu, M.-C., Hsieh, S., Sheu, C.-F. 2012. A factor-adjusted multiple testing procedure for ERP data analysis. *Behavior Research Methods*, 44, 635-643.
- Friguet, C., Kloareg, M., Causeur, D. 2009. A factor model approach to multiple testing under dependence. *Journal of the American Statistical Association*, 104, 1406-1415.
- Leek, J.T., Storey, J.D. 2008. A general framework for multiple testing dependence. *Proceedings of the National Academy of Sciences of the United States of America*, 105, 18718-18723.
- Sheu, C.-F., Perthame, E., Lee Y.-S. and Causeur, D. 2016. Accounting for time dependence in large-scale multiple testing of event-related potential data. *Annals of Applied Statistics*. 10(1), 219-245.
- Storey, J. D., Tibshirani, R. 2003. Statistical significance for genome-wide experiments. *Proceedings of the National Academy of Sciences of the United States of America*, 100, 9440-9445.
- Sun, Y., Zhang, N.R., Owen, A.B. 2012. Multiple hypothesis testing adjusted for latent variables, with an application to the AGEMAP gene expression data. *The Annals of Applied Statistics*, 6, no. 4, 1664-1688.

See Also

[erpavetest](#), [erptest](#), [gbtest](#), [p.adjust](#), [pval.estimate.eta0](#)

Examples

```
## Not run:

data(impulsivity)

# Paired t-tests for the comparison of the ERP curves in the two conditions,
# within experimental group High, at channel CPZ

erpdt.highCPZ = impulsivity[(impulsivity$Group=="High")&(impulsivity$Channel=="CPZ"),5:505]
# ERP curves for subjects in group 'High', at channel CPZ
covariates.highCPZ = impulsivity[(impulsivity$Group=="High")&(impulsivity$Channel=="CPZ"),1:4]
covariates.highCPZ = droplevels(covariates.highCPZ)
# Experimental covariates for subjects in group 'High', at channel CPZ

design = model.matrix(~C(Subject,sum)+Condition,data=covariates.highCPZ)
# Design matrix to compare ERP curves in the two conditions
design0 = model.matrix(~C(Subject,sum),data=covariates.highCPZ)
# Design matrix for the null model (no condition effect)

tests = erpfatest(erpdt.highCPZ,design,design0,nbf=NULL,wantplot=TRUE,significance="none")
# with nbf=NULL and significance="none", just to choose a number of factors
Ftest = erpFtest(erpdt.highCPZ,design,design0,nbf=6)
# with nbf=6 (approximate conservative recommendation based on the variance inflation plot)
# Signal detection: test for an eventual condition effect.
Ftest$pval

tests = erpfatest(erpdt.highCPZ,design,design0,nbf=6)
# Signal identification: which are the significant intervals?

time_pt = seq(0,1000,2) # sequence of time points (1 time point every 2ms in [0,1000])
nbs = 20 # Number of B-splines for the plot of the effect curve
effect=which(colnames(design)=="ConditionSuccess")
erpplot(erpdt.highCPZ,design=design,frames=time_pt,effect=effect,xlab="Time (ms)",
        ylab=expression(Effect~curve~(mu~V)),bty="l",ylim=c(-3,3),nbs=nbs,
        cex.axis=1.25,cex.lab=1.25,interval="simultaneous")
# with interval="simultaneous", both the pointwise and the simultaneous confidence bands
# are plotted
points(time_pt[tests$significant],rep(0,length(tests$significant)),pch=16,col="blue")
# Identifies significant time points by blue dots
title("Success-Failure effect curve with 95 percent C.I.",cex.main=1.25)
mtext(paste("12 subjects - Group 'High' - ",nbs," B-splines",sep=""),cex=1.25)

## End(Not run)
```

| | |
|----------|---|
| erpFtest | <i>Functional Analysis-of-Variance (Anova) testing of Event-Related Potentials (ERP) data</i> |
|----------|---|

Description

Factor-based generalized Likelihood-Ratio Test for functional ANOVA in ERP designs. The procedure is described in details in Causeur, Sheu, Perthame and Rufini (2018).

Usage

```
erpFtest(dta, design, design0=NULL, nbf=NULL, pvalue=c("Satterthwaite", "MC", "none"),
  nsamples=200, min.err=0.01, verbose=FALSE,
  nbfmax=min(c(nsamples, nrow(design)))-ncol(design)-1,
  wantplot=ifelse(is.null(nbf), TRUE, FALSE), svd.method=c("fast.svd", "irlba"))
```

Arguments

| | |
|------------|--|
| dta | Data frame containing the ERP measurements: each column corresponds to a time frame and each row to a curve. |
| design | Design matrix of the nonnull model for the relationship between the ERP and the experimental variables. Typically the output of the function <code>model.matrix</code> |
| design0 | Design matrix of the null model. Typically a submodel of the nonnull model, obtained by removing columns from <code>design</code> . Default is <code>NULL</code> , corresponding to the model with no covariates. |
| nbf | Number of factors in the residual covariance model. Default is <code>NULL</code> : the number of factors is determined by minimization of the variance inflation criterion as suggested in Friguet et al. (2009). |
| pvalue | If "Satterthwaite", then the Monte-Carlo p-value is calculated with a Satterthwaite approximation of the null distribution. The other possible value is "none", for no calculation of the p-value or "MC" for the Monte-Carlo p-value. |
| nsamples | Number of Monte-Carlo samples for the estimation of the null distribution. Default is <code>nsamples=200</code> , recommended when the Satterthwaite approximation is used. |
| min.err | Control parameter for convergence of the iterative algorithm. Default is <code>1e-02</code> . |
| verbose | If <code>TRUE</code> , details are printed along the iterations of the algorithm. Default is <code>FALSE</code> . |
| nbfmax | Only required if <code>nbf=NULL</code> . The largest possible number of factors. |
| wantplot | If <code>TRUE</code> , a diagnostic plot is produced to help choosing the number of factors. Only active if <code>nbf=NULL</code> . |
| svd.method | the EM algorithm starts from an SVD estimation of the factor model parameters. The default option to implement this SVD is <code>fast.svd</code> . An alternative option is an approximate but faster SVD by function <code>irlba</code> . |

Details

The method is described in Causeur et al. (2018). It can be viewed as a Hotelling's T-squared multivariate ANOVA test based on a factor decomposition of the time-dependence across point-wise F-tests. For 1-way functional ANOVA, it can be compared to function `anova.onefactor` in package `fda.usc`.

Value

| | |
|------------------------|--|
| <code>Fgls</code> | The generalized LRT statistics comparing the nonnull model with design matrix <code>design</code> and the null model with design matrix <code>design0</code> . |
| <code>Fols</code> | The LRT statistics ignoring time-dependence across pointwise F-tests. |
| <code>pval</code> | p-value of the generalized LRT statistics. |
| <code>pval.Fols</code> | p-value of the LRT statistics ignoring time-dependence across pointwise F-tests. |

Author(s)

David Causeur, IRMAR, UMR 6625 CNRS, Agrocampus Ouest, Rennes, France. Flavia Rufini, Agrocampus Ouest, Rennes, France.

References

Causeur, D., Sheu, C.-F., Perthame, E. and Rufini, F. (2018). A functional generalized F-test for signal detection with applications to event-related potentials significance analysis. Submitted.

Examples

```
data(impulsivity)

# Comparison of ERP curves in the two conditions, within experimental group 'High', at channel CPZ

erpdata.highCPZ = impulsivity[(impulsivity$Group=="High")&(impulsivity$Channel=="CPZ"),5:505]
# ERP curves for subjects in group 'High'
covariates.highCPZ = impulsivity[(impulsivity$Group=="High")&(impulsivity$Channel=="CPZ"),1:4]
covariates.highCPZ = droplevels(covariates.highCPZ)
# Experimental covariates for subjects in group 'High'

design = model.matrix(~C(Subject,sum)+Condition,data=covariates.highCPZ)
# Design matrix to compare ERP curves in the two conditions
design0 = model.matrix(~C(Subject,sum),data=covariates.highCPZ)
# Design matrix for the null model (no condition effect)

Ftest = erpFtest(erpdata.highCPZ,design,design0,nbf=NULL,wantplot=TRUE,pvalue="none")
# with pvalue="none", just to choose a number of factors
Ftest = erpFtest(erpdata.highCPZ,design,design0,nbf=6)
Ftest$pval      # p-value of the Generalized LRT statistic
Ftest$pval.Fols # p-value of the LRT statistic when time-dependence is ignored

time_pt = seq(0,1000,2) # sequence of time points (1 time point every 2ms in [0,1000])
nbs = 20                # Number of B-splines for the plot of the effect curve
effect=which(colnames(design)=="ConditionSuccess")
```

```

erpplot(erpdata.highCPZ,design=design,frames=time_pt,effect=effect,xlab="Time (ms)",
        ylab=expression(Effect~curve~(mu~V)),bty="l",ylim=c(-3,3),nbs=nbs,
        cex.axis=1.25,cex.lab=1.25,interval="simultaneous")
# with interval="simultaneous", both the pointwise and the simultaneous confidence bands
# are plotted
title("Success-Failure effect curve with 95 percent C.I.",cex.main=1.25)
mtext(paste("12 subjects - Group 'High' - ",nbs," B-splines",sep=""),cex=1.25)

```

| | |
|---------|--|
| erpplot | <i>Plot of ERP curves or effect curves (difference curve for example) with confidence intervals.</i> |
|---------|--|

Description

The function is designed to plot either raw ERP curves or estimated effect curves. In the case an effect curve is displayed, then spline smoothing can be used to obtain more regular curves. Pointwise or simultaneous confidence intervals can be added to the plot.

Usage

```

erpplot(dta,design=NULL,effect=1,interval=c("none","pointwise","simultaneous"),
        alpha=0.05,frames=NULL,ylim=NULL,nbs=NULL, ...)

```

Arguments

| | |
|----------|---|
| dta | Data frame containing the ERP curves: each column corresponds to a time frame and each row to a curve. |
| design | Design matrix of the nonnull model for the relationship between the ERP and the experimental variables. Typically the output of the function model.matrix. Only needed if an effect curve is to be plotted. |
| effect | Integer value giving the column number of the design matrix corresponding to the effect curve to be plotted |
| interval | Type of confidence interval to be added to the plot of an effect curve. Default is "none" for no confidence interval. Other possibilities are "pointwise" for a pointwise confidence interval or "simultaneous" for both a pointwise and a simultaneous confidence interval. |
| alpha | The confidence level for the confidence interval is 1-alpha. |
| frames | Sequence of time frames. Default is NULL, in which case frames is just the sequence of integers between one and the total number of frames. |
| ylim | Limits for the y-axis. Default is NULL (set into the function). |
| nbs | Number of B-spline basis for an eventual spline smoothing of the effect curve. Default is NULL for no smoothing. |
| ... | Graphical parameters (see par) and any further arguments of plot, typically plot.default, may also be supplied as arguments to this function. Hence, the high-level graphics control arguments described under par and the arguments to title may be supplied to this function. |

Value

The function generates a plot, but does not return any other numerical outputs.

Author(s)

David Causeur, IRMAR, UMR 6625 CNRS, Agrocampus Ouest, Rennes, France.

See Also

[matplot](#)

Examples

```
data(impulsivity)

# Comparison of ERP curves in the two conditions, within experimental group 'High', at channel CPZ

erpdt.highCPZ = impulsivity[(impulsivity$Group=="High")&(impulsivity$Channel=="CPZ"),5:505]
# ERP curves for subjects in group 'High'
covariates.highCPZ = impulsivity[(impulsivity$Group=="High")&(impulsivity$Channel=="CPZ"),1:4]
covariates.highCPZ = droplevels(covariates.highCPZ)
# Experimental covariates for subjects in group 'High'

colors = ifelse(covariates.highCPZ$Condition=="Success","darkgray","orange")
# Gives a color code for each condition
time_pt = seq(0,1000,2) # sequence of time points (1 time point every 2ms in [0,1000])
erpplot(erpdt.highCPZ,frames=time_pt,xlab="Time (ms)",lty=1,col=colors,
        ylab=expression(ERPs~(mu~V)),bty="l",
        cex.axis=1.25,cex.lab=1.25)
# Displays the ERP curves in group 'High', at channel CPZ
legend("topright",bty="n",lty=1,col=c("darkgray","orange"),legend=c("Success","Failure"))
title("ERP curves",cex.main=1.25)
mtext(paste("12 subjects - Group 'High'",sep=""),cex=1.25)

design = model.matrix(~C(Subject,sum)+Condition,data=covariates.highCPZ)
# Design matrix to compare ERP curves in the two conditions
design0 = model.matrix(~C(Subject,sum),data=covariates.highCPZ)
# Design matrix for the null model (no condition effect)

nbs = 20 # Number of B-splines for the plot of the effect curve
effect=which(colnames(design)=="ConditionSuccess")
erpplot(erpdt.highCPZ,design=design,frames=time_pt,effect=effect,xlab="Time (ms)",
        ylab=expression(Effect~curve~(mu~V)),bty="l",ylim=c(-3,3),nbs=nbs,
        cex.axis=1.25,cex.lab=1.25,interval="simultaneous")
# with interval="simultaneous", both the pointwise and the simultaneous confidence bands
# are plotted
title("Success-Failure effect curve with 95 percent C.I.",cex.main=1.25)
mtext(paste("12 subjects - Group 'High' - ",nbs," B-splines",sep=""),cex=1.25)
```


erptest

*FDR- and FWER-controlling Multiple testing of ERP data***Description**

Classical FDR- and FWER-controlling multiple testing procedures for ERP data in a linear model framework.

Usage

```
erptest(dta, design, design0=NULL,
        method=c("BH", "holm", "hochberg", "hommel", "bonferroni", "BY", "fdr", "none"), alpha=0.05,
        pi0 = 1, nbs = NULL)
```

Arguments

| | |
|---------|--|
| dta | Data frame containing the ERP curves: each column corresponds to a time frame and each row to a curve. |
| design | Design matrix of the nonnull model for the relationship between the ERP and the experimental variables. Typically the output of the function <code>model.matrix</code> |
| design0 | Design matrix of the null model. Typically a submodel of the nonnull model, obtained by removing columns from <code>design</code> . Default is <code>NULL</code> , corresponding to the model with no covariates. |
| method | FDR- or FWER- controlling multiple testing procedures as available in the function <code>p.adjust</code> . Default is "BH", for the Benjamini-Hochberg procedure (see Benjamini and Hochberg, 1995). |
| alpha | The FDR or FWER control level. Default is 0.05 |
| pi0 | An estimate of the proportion of true null hypotheses, which can be plugged into an FDR controlling multiple testing procedure to improve its efficiency. Default is 1, corresponding to the classical FDR controlling procedures. If <code>NULL</code> , the proportion is estimated using the function <code>pval.estimate.eta0</code> of package <code>fdrtool</code> , with the method proposed by Storey and Tibshirani (2003). |
| nbs | Number of B-spline basis for an eventual spline smoothing of the effect curve. Default is <code>NULL</code> for no smoothing. |

Value

| | |
|---------------|---|
| pval | p-values of the tests. |
| correctedpval | Corrected p-values, for the multiplicity of tests. Depends on the multiple testing method (see function <code>p.adjust</code>). |
| significant | Indices of the time points for which the test is positive. |
| pi0 | Value for <code>pi0</code> : if the input argument <code>pi0</code> is <code>NULL</code> , the output is the estimated proportion of true null hypotheses using the method by Storey and Tibshirani (2003). |

| | |
|-----------|--|
| test | Pointwise F-statistics if $p > 1$, where p is the difference between the numbers of parameters in the nonnull and null models. Otherwise, if $p = 1$, the function returns pointwise t-statistics (signed square-roots of F-statistics). |
| df1 | Residual degrees of freedom for the nonnull model. |
| df0 | Residual degrees of freedom for the null model. |
| signal | Estimated signal: a $p \times T$ matrix, where p is the difference between the numbers of parameters in the nonnull and null models and T the number of time points. |
| sd | T-vector of estimated residual standard deviations where T is the number of time points. |
| r2 | R-squared values for each of the T linear models. |
| sdsignal | Standard deviations of the estimated signal: a $p \times T$ matrix, where p is the difference between the numbers of parameters in the nonnull and null models and T the number of time points. |
| residuals | $n \times T$ matrix of residuals of the fit of the nonnull model. |
| coef | Estimated regression coefficients: a $q \times T$ matrix, where q is the number of parameters in the nonnull model and T the number of time points. |

Author(s)

David Causeur, IRMAR, UMR 6625 CNRS, Agrocampus Ouest, Rennes, France.

See Also

[erpavetest](#), [erpfatest](#), [gbtest](#), [p.adjust](#)

Examples

```
data(impulsivity)

# Paired t-tests for the comparison of the ERP curves in the two conditions,
# within experimental group High, at channel CPZ

erpdata.highCPZ = impulsivity[(impulsivity$Group=="High") & (impulsivity$Channel=="CPZ"), 5:505]
# ERP curves for subjects in group 'High'
covariates.highCPZ = impulsivity[(impulsivity$Group=="High") & (impulsivity$Channel=="CPZ"), 1:4]
covariates.highCPZ = droplevels(covariates.highCPZ)
# Experimental covariates for subjects in group 'High'

design = model.matrix(~C(Subject, sum) + Condition, data=covariates.highCPZ)
# Design matrix to compare ERP curves in the two conditions
design0 = model.matrix(~C(Subject, sum), data=covariates.highCPZ)
# Design matrix for the null model (no condition effect)

tests = erptest(erpdata.highCPZ, design, design0)

time_pt = seq(0, 1000, 2) # sequence of time points (1 time point every 2ms in [0, 1000])
nbs = 20 # Number of B-splines for the plot of the effect curve
effect = which(colnames(design) == "ConditionSuccess")
erpplot(erpdata.highCPZ, design=design, frames=time_pt, effect=effect, xlab="Time (ms)",
```

```

      ylab=expression(Effect~curve~(mu~V)),bty="l",ylim=c(-3,3),nbs=nbs,
      cex.axis=1.25,cex.lab=1.25,interval="simultaneous")
    # with interval="simultaneous", both the pointwise and the simultaneous confidence bands
    # are plotted
    points(time_pt[tests$significant],rep(0,length(tests$significant)),pch=16,col="blue")
    # Identifies significant time points by blue dots
    title("Success-Failure effect curve with 95 percent C.I.",cex.main=1.25)
    mtext(paste("12 subjects - Group 'High' - ",nbs," B-splines",sep=""),cex=1.25)

```

| | |
|--------|---|
| gbtest | <i>The Guthrie-Buchwald procedure for significance analysis of ERP data</i> |
|--------|---|

Description

Monte-Carlo implementation of the Guthrie-Buchwald procedure (see Guthrie and Buchwald, 1991) which accounts for the auto-correlation among test statistics to control erroneous detections of short intervals.

Usage

```
gbtest(dta, design, design0 = NULL, graphthresh = 0.05, nsamples = 1000)
```

Arguments

| | |
|-------------|---|
| dta | Data frame containing the ERP curves: each column corresponds to a time frame and each row to a curve. |
| design | Design matrix of the nonnull model for the relationship between the ERP and the experimental variables. Typically the output of the function <code>model.matrix</code> |
| design0 | Design matrix of the null model. Typically a submodel of the nonnull model, obtained by removing columns from <code>design</code> . Default is <code>NULL</code> , corresponding to the model with no covariates. |
| graphthresh | Graphical threshold (see Guthrie and Buchwald, 1991). Default is 0.05. As the FDR control level, the smaller is the graphical threshold, the more conservative is the procedure. |
| nsamples | Number of samples in the Monte-Carlo method to estimate the residual covariance. Default is 1000. |

Details

The Guthrie-Buchwald method starts from a preliminary estimation of r , the lag-1 autocorrelation, among test statistics. Then, the null distribution of the lengths of the intervals $I_{\alpha} = t : p_{\text{value},t} \leq \alpha$, where α is the so-called graphical threshold parameter of the method, is obtained using simulations of p -values p_t associated to auto-regressive t -test process of order 1 with mean 0 and auto-correlation r . Such an interval I_{α} is declared significant if its length exceeds the $(1-\alpha)$ -quantile of the null distribution. Note that the former method is designed to control erroneous detections of short significant intervals but not to control any type-I error rate.

Value

| | |
|-------------------|---|
| nbsignifintervals | Number of significant intervals. |
| intervals | List of length nbsignifintervals which components give the indices of each significant intervals. |
| significant | Indices of the time points for which the test is positive. |
| signal | Estimated signal: a $p \times T$ matrix, where p is the difference between the numbers of parameters in the nonnull and null models and T the number of frames. |
| rho | Estimated lag-1 auto-correlation. |
| r2 | R-squared values for each of the T linear models. |

Author(s)

David Causeur - david.causeur@agrocampus-ouest.fr and Mei-Chen Chu (National Cheng-Kung University, Tainan, Taiwan)

References

Guthrie, D. and Buchwald, J.S. (1991). Significance testing of difference potentials. *Psychophysiology*, 28, 240-244.

Sheu, C.-F., Perthame, E., Lee Y.-S. and Causeur, D. (2016). Accounting for time dependence in large-scale multiple testing of event-related potentials data. *Annals of Applied Statistics*. 10(1), 219-245.

See Also

[erpavetest](#), [erpfatest](#), [erptest](#)

Examples

```
data(impulsivity)

# Paired t-tests for the comparison of the ERP curves in the two conditions,
# within experimental group High, at channel CPZ

erpdt.highCPZ = impulsivity[(impulsivity$Group=="High")&(impulsivity$Channel=="CPZ"),5:505]
# ERP curves for subjects in group 'High'
covariates.highCPZ = impulsivity[(impulsivity$Group=="High")&(impulsivity$Channel=="CPZ"),1:4]
covariates.highCPZ = droplevels(covariates.highCPZ)
# Experimental covariates for subjects in group 'High'

design = model.matrix(~C(Subject,sum)+Condition,data=covariates.highCPZ)
# Design matrix to compare ERP curves in the two conditions
design0 = model.matrix(~C(Subject,sum),data=covariates.highCPZ)
# Design matrix for the null model (no condition effect)

tests = gbtest(erpdt.highCPZ,design,design0)

time_pt = seq(0,1000,2) # sequence of time points (1 time point every 2ms in [0,1000])
```

```

nbs = 20                                # Number of B-splines for the plot of the effect curve
effect=which(colnames(design)=="ConditionSuccess")
erpplot(erpdt.highCPZ,design=design,frames=time_pt,effect=effect,xlab="Time (ms)",
        ylab=expression(Effect~curve~(mu~V)),bty="l",ylim=c(-3,3),nbs=nbs,
        cex.axis=1.25,cex.lab=1.25,interval="simultaneous")
# with interval="simultaneous", both the pointwise and the simultaneous confidence bands
# are plotted
points(time_pt[tests$significant],rep(0,length(tests$significant)),pch=16,col="blue")
# Identifies significant time points by blue dots
title("Success-Failure effect curve with 95 percent C.I.",cex.main=1.25)
mtext(paste("12 subjects - Group 'High' - ",nbs," B-splines",sep=""),cex=1.25)

```

ifa

*Inverse of a matrix based on its factor decomposition.***Description**

This function is not supposed to be called directly by users. It is needed in function `emfa` implementing an EM algorithm for a factor model.

Usage

```
ifa(Psi, B)
```

Arguments

| | |
|-----|--|
| Psi | m-vector of specific variances, where m is the number of rows and columns of the matrix. |
| B | m x q matrix of loadings, where q is the number of factors |

Details

If Sigma has the q-factor decomposition $\text{Sigma} = \text{diag}(\text{Psi}) + \text{BB}'$, then Sigma^{-1} has the corresponding q-factor decomposition $\text{Sigma}^{-1} = \text{diag}(\text{phi})(\text{I} - \text{theta theta}')\text{diag}(\text{phi})$, where theta is a mxq matrix and phi the vector of inverse specific standard deviations.

Value

| | |
|-------|--|
| iS | m x m inverse of $\text{diag}(\text{Psi}) + \text{BB}'$. |
| iSB | m x q matrix $(\text{diag}(\text{Psi}) + \text{BB}')^{-1}\text{B}$. |
| Phi | m-vector of inverse specific standard deviations. |
| Theta | mxq matrix of loadings for the inverse factor model (see the details Section). |

Author(s)

David Causeur, IRMAR, UMR 6625 CNRS, Agrocampus Ouest, Rennes, France.

References

Woodbury, M.A. (1949) The Stability of Out-Input Matrices. Chicago, Ill., 5 pp

See Also

[emfa](#), [isqrtfa](#)

Examples

```
data(impulsivity)
erpdt = as.matrix(impulsivity[,5:505]) # erpdt contains the whole set of ERP curves
fa = emfa(erpdt,nbf=20) # 20-factor modelling of the ERP curves in erpdt
Sfa = diag(fa$Psi)+tcrossprod(fa$B) # Factorial estimation of the variance
iSfa = ifa(fa$Psi,fa$B)$iS # Matrix inversion
max(abs(crossprod(Sfa,iSfa)-diag(ncol(erpdt)))) # Checks that Sfa x iSfa = diag(ncol(erpdt))
```

| | |
|-------------|---|
| impulsivity | <i>Event-Related Potentials data from a study conducted by Shen et al. (2014) to investigate neural correlates of impulsive behavior.</i> |
|-------------|---|

Description

In the study, adult males who scored at the top 25% and bottom 25% on a scale measuring trait impulsivity were recruited to participate in an ERP experiment. There were twelve subjects in each impulsivity trait group (high or low). Specifically, the influence of trait impulsivity in response inhibition was examined in a two-choice discrimination task using the stop-signal paradigm (Logan et al, 1984). Participants were asked to withhold their responses when a 'stop' signal appeared after the 'go' stimulus. ERP amplitudes from 32 scalp locations (channels) were recorded from 200 ms before signal onset till 1000 ms after with one reading per 2 ms. Two of the 32 channels were excluded in the analysis by the authors. The response inhibition is a within-subject factor with two levels (successful or failed).

Usage

```
data("impulsivity")
```

Format

A data frame with 144 observations on the following 505 variables. The first four variables are categorical: Channel with levels CPZ CZ FCZ giving the electrode position, Subject with levels S1 S2 ... to identify the subjects, Group with levels High Low for the membership to an impulsivity group and Condition with levels Failure Success for the response inhibition condition. The remaining 501 variables are the ERP values at time 0 (onset), 2ms, 4ms, ..., 1000ms.

Source

Shen, I., Lee, D., and Chen, C. (2014), The role of trait impulsivity in response inhibition: event-related potentials in a stop-signal task. *International Journal of Psychophysiology*, 91(2).

References

- Causeur, D., Sheu, C.-F., Perthame, E. and Rufini, F. (2018). A functional generalized F-test for signal detection with applications to event-related potentials significance analysis. Submitted.
- Logan, G. D., Cowan, W., and Davis, K. (1984), On the ability to inhibit simple and choice reaction time responses: a model and a method. *Journal of Experimental Psychology: Human Perception and Performance*, 10(2), 276-291.

Examples

```
data(impulsivity)

head(impulsivity[,1:10]) # each row of impulsivity contains an ERP curve (from column 5 to 505)
# Column 1: electrode position (channel)
# Column 2: subject id
# Column 3: impulsivity group (High/Low)
# Column 4: response inhibition condition (Success/Failure)

time_pt = seq(0, 1000, 2) # sequence of time points (1 time point every 2ms in [0,1000])
erpdata = impulsivity[,5:505] # erpdata contains the ERP curves
T = length(time_pt) # number of time points

covariates = impulsivity[,1:4] # contains the experimental covariates of interest

# Impulsivity ERP design

with(data=covariates, table(Channel, Condition, Group))
# 48 ERP curves for each of the 3 channels
# Within each channel, 12 ERP curves in each Condition x Group
# Within each channel, 12 subjects in group High, 12 in group Low
```

isqrtfa

Inverse square-root of a matrix based on its factor decomposition.

Description

This function is not supposed to be called directly by users. It is needed in functions `erpfatest` and `erpFtest` implementing factor-adjusted testing methods.

Usage

```
isqrtfa(Psi, B)
```

Arguments

- | | |
|-----|--|
| Psi | m-vector of specific variances, where m is the number of rows and columns of the matrix. |
| B | mxq matrix of loadings, where q is the number of factors |

Details

If Sigma has the q-factor decomposition $\text{Sigma} = \text{diag}(\Psi) + \text{BB}'$, then the function returns a matrix Omega such that $\text{Sigma}^{-1} = \text{Omega} \text{Omega}'$. Equivalently, $\text{Omega}' \text{Sigma} \text{Omega} = \text{I}$.

Value

The mxm matrix Omega (see the details Section).

Author(s)

David Causeur, IRMAR, UMR 6625 CNRS, Agrocampus Ouest, Rennes, France.

References

Woodbury, M.A. (1949) The Stability of Out-Input Matrices. Chicago, Ill., 5 pp

See Also

[emfa](#), [ifa](#)

Examples

```
data(impulsivity)
erpdt = as.matrix(impulsivity[,5:505]) # erpdt contains the whole set of ERP curves
fa = emfa(erpdt,nbf=20) # 20-factor modelling of the ERP curves in erpdt
Sfa = diag(fa$Psi)+tcrossprod(fa$B) # Factorial estimation of the variance
iSfa = ifa(fa$Psi,fa$B)$iS # Matrix inversion
isqrtSfa = isqrtfa(fa$Psi,fa$B) # Inverse square-root of Sfa
max(abs(tcrossprod(isqrtSfa)-iSfa)) # Checks that isqrtSfa x t(isqrtSfa) = iSfa
```

nbfactors

Determination of the number of factors in high dimensional factor models.

Description

This function is not supposed to be called directly by users. It implements the variance inflation method proposed by Friguet et al. (2009) to choose the number of factors in high dimensional factor models.

Usage

```
nbfactors(dta,maxnbfactors=15,diagnostic.plot=FALSE,min.err=0.001,verbose=FALSE,
svd.method=c("fast.svd","irlba"))
```


Arguments

| | |
|------------------------------|--|
| <code>dta</code> | n x m scaled matrix which rows are multivariate m-profiles for n individuals. n can be much smaller than m. Columns are all centered with standard deviations 1. |
| <code>maxnbfactors</code> | Maximum number of factors. It has to be a positive integer, smaller than the rank of dta. |
| <code>diagnostic.plot</code> | Logical value. If TRUE, a plot displaying the variance inflation curve is produced, with recommendations for the optimal number of factors. |
| <code>min.err</code> | stopping criterion for the iterative algorithm. Maximum difference between the estimated parameters in the last two iterations. |
| <code>verbose</code> | logical value. If verbose=TRUE, then some information is printed along the calculation. |
| <code>svd.method</code> | the EM algorithm starts from an SVD estimation of the factor model parameters. The default option to implement this SVD is fast.svd . An alternative option is an approximate but faster SVD by function irlba . |

Details

It is highly recommended to run the function first with `diagnostic.plot=TRUE` and to choose the number of factors based on the plot that will be produced. Two recommendations are provided: a conservative one obtained using a kind of elbow criterion, and a liberal one that minimizes the variance inflation curve.

Value

| | |
|------------------|---|
| <code>sdt</code> | Variance inflation values for a number of factors going from 0 to <code>maxnbfactors</code> . |
| <code>nbf</code> | Recommendation for an optimal number of factors (the more liberal, see the details Section for more information). |

Author(s)

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References

Friguet, C., Kloareg, M. and Causeur, D. (2009). A factor model approach to multiple testing under dependence. *Journal of the American Statistical Association*. 104 (488), 1406-1415.

See Also

[emfa](#)

Examples

```
data(impulsivity)
erpdt = as.matrix(impulsivity[,5:505]) # erpdta contains the whole set of ERP curves
nbf = nbfactors(scale(erpdt),maxnbfactors=10,diagnostic.plot=TRUE)
```

Index

* datasets

impulsivity, [22](#)

emfa, [6](#), [22](#), [24](#), [25](#)

ERP (ERP-package), [2](#)

ERP-package, [2](#)

erpavetest, [7](#), [12](#), [18](#), [20](#)

erpfatest, [8](#), [9](#), [18](#), [20](#)

erpFtest, [13](#)

erpplot, [15](#)

erptest, [8](#), [12](#), [17](#), [20](#)

factanal, [7](#)

fast.svd, [6](#), [10](#), [13](#), [25](#)

gbtest, [8](#), [12](#), [18](#), [19](#)

ifa, [21](#), [24](#)

impulsivity, [22](#)

irlba, [6](#), [10](#), [13](#), [25](#)

isqrtfa, [22](#), [23](#)

matplot, [16](#)

nbfactors, [24](#)

p.adjust, [8](#), [11](#), [12](#), [18](#)

pval.estimate.eta0, [12](#)