

# Package ‘CommonMean.Copula’

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**Type** Package

**Title** Common Mean Vector under Copula Models

**Version** 1.0.4

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**Description** Estimate bivariate common mean vector under copula models with known correlation. In the current version, available copulas are the Clayton, Gumbel, Frank, Farlie-Gumbel-Morgenstern (FGM), and normal copulas. See Shih et al. (2019) <doi:10.1080/02331888.2019.1581782> and Shih et al. (2021) <under review> for details under the FGM and general copulas, respectively.

**Depends** pracma, mvtnorm

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**Encoding** UTF-8

**RoxygenNote** 7.1.2

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**NeedsCompilation** no

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CommonMean.Copula-package

*Common Mean Vector under Copula Models*

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## Description

Estimate bivariate common mean vector under copula models with known correlation. A maximum likelihood estimation procedure is employed. In the current version, available copulas are the Clayton, Gumbel, Frank, Farlie-Gumbel-Morgenstern (FGM), and normal copulas. See Shih et al. (2019) and Shih et al. (2021) for details under the FGM and general copulas, respectively.

## Details

The method implemented in this package can be used for bivariate meta-analyses. See Shih et al. (2019) and Shih et al. (2021) for the example of bivariate entrance exam data analysis.

## Author(s)

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## References

Shih J-H, Konno Y, Chang Y-T, Emura T (2019) Estimation of a common mean vector in bivariate meta-analysis under the FGM copula, *Statistics* 53(3): 673-95.

Shih J-H, Konno Y, Emura T (2021-) Copula-based estimation methods for a common mean vector for bivariate meta-analyses, under review.

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CommonMean.Copula

*Estimate bivariate common mean vector under copula models*

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## Description

Estimate the common mean vector under copula models with known correlation. A maximum likelihood estimation procedure is employed. See Shih et al. (2019) and Shih et al. (2021) for details under the Farlie-Gumbel-Morgenstern (FGM) and general copulas, respectively.

## Usage

```
CommonMean.Copula(Y1, Y2, Sigma1, Sigma2, rho, copula = "Clayton")
```

**Arguments**

Y1	Outcome 1
Y2	Outcome 2
Sigma1	Standard deviation of outcome 1.
Sigma2	Standard deviation of outcome 2.
rho	Correlation coefficient between outcomes.
copula	The copula to be used with possible options "Clayton", "Gumbel", "Frank", "FGM", and "normal".

**Details**

We apply "optim" routine to maximize the log-likelihood function. In addition, boundary corrected correlations will be used (Shih et al., 2019).

**Value**

Outcome 1	Outcome 1.
Outcome 2	Outcome 2.
Correlation	Correlation coefficient between outcomes.
Sample size	Sample size.
Copula	Selected copula.
Copula parameter	Copula parameter.
Corrected correlation	Boundary corrected correlations.
CommonMean 1	Estimation results of outcome 1.
CommonMean 2	Estimation results of outcome 2.
V	Covariance matrix of the common mean vector estimate.
Log-likelihood values	Fitted log-likelihood values.

**Note**

When rho is 1 or -1, there are some computational issues since the copula parameter may correspond to infinite or negative infinite under some copulas. For the Clayton copula, if  $\rho > 0.95$ , it will be approximated by 0.95. For the Frank copula, if  $\rho > 0.95$  or  $\rho < -0.95$ , it will be approximated by 0.95 or -0.95, respectively.

**References**

- Shih J-H, Konno Y, Chang Y-T, Emura T (2019) Estimation of a common mean vector in bivariate meta-analysis under the FGM copula, *Statistics* 53(3): 673-95.
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**Examples**

```
library(CommonMean.Copula)
Y1 = c(35,25,30,50,60) # outcome 1
Y2 = c(30,30,50,65,40) # outcome 2
Sigma1 = c(1.3,1.4,1.5,2.0,1.8) # SE of outcome 1
Sigma2 = c(1.7,1.9,2.5,2.2,1.8) # SE of outcome 2
rho = c(0.4,0.7,0.6,0.7,0.6) # correlation between two outcomes
CommonMean.Copula(Y1,Y2,Sigma1,Sigma2,rho) # input
```

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