

Package ‘CoSMoS’

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Type Package

Title Complete Stochastic Modelling Solution

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Description

Makes univariate, multivariate, or random fields simulations precise and simple. Just select the desired time series or random fields’ properties and it will do the rest. CoSMoS is based on the framework described in Papalexiou (2018, <[doi:10.1016/j.advwatres.2018.02.013](https://doi.org/10.1016/j.advwatres.2018.02.013)>), extended for random fields in Papalexiou and Serinaldi (2020, <[doi:10.1029/2019WR026331](https://doi.org/10.1029/2019WR026331)>), and further advanced in Papalexiou et al. (2021, <[doi:10.1029/2020WR029466](https://doi.org/10.1029/2020WR029466)>) to allow fine-scale space-time simulation of storms (or even cyclone-mimicking fields).

Depends R (>= 3.5.0), ggplot2, data.table

Imports utils, methods, stats, grDevices, nloptr, MBA, Matrix, mAr,
matrixcalc, mvtnorm, cowplot, directlabels, animation,
ggquiver, pracma, plot3D

Encoding UTF-8

LazyData true

RoxygenNote 7.1.1

Suggests testthat, knitr, rmarkdown

VignetteBuilder knitr

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URL <https://github.com/TycheLab/CoSMoS>

NeedsCompilation no

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Description

CoSMoS is an R package that makes time series generation with desired properties easy. Just choose the characteristics of the time series you want to generate, and it will do the rest.

Details

The generated time series preserve any probability distribution and any linear autocorrelation structure. Users can generate as many and as long time series from processes such as precipitation, wind, temperature, relative humidity etc. It is based on a framework that unified, extended, and improved a modelling strategy that generates time series by transforming "parent" Gaussian time series having specific characteristics (Papalexiou, 2018).

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References

- Papalexiou, S.M. (2018). Unified theory for stochastic modelling of hydroclimatic processes: Preserving marginal distributions, correlation structures, and intermittency. *Advances in Water Resources* 115, 234-252, doi: [10.1016/j.advwatres.2018.02.013](https://doi.org/10.1016/j.advwatres.2018.02.013)
- Papalexiou, S.M., Markonis, Y., Lombardo, F., AghaKouchak, A., Foufoula-Georgiou, E. (2018). Precise Temporal Disaggregation Preserving Marginals and Correlations (DiPMaC) for Stationary and Nonstationary Processes. *Water Resources Research*, 54(10), 7435-7458, doi: [10.1029/2018WR022726](https://doi.org/10.1029/2018WR022726)
- Papalexiou, S.M., Serinaldi, F. (2020). Random Fields Simplified: Preserving Marginal Distributions, Correlations, and Intermittency, With Applications From Rainfall to Humidity. *Water Resources Research*, 56(2), e2019WR026331, doi: [10.1029/2019WR026331](https://doi.org/10.1029/2019WR026331)
- Papalexiou, S.M., Serinaldi, F., Porcu, E. (2021). Advancing Space-Time Simulation of Random Fields: From Storms to Cyclones and Beyond. *Water Resources Research*, 57, e2020WR029466, doi: [10.1029/2020WR029466](https://doi.org/10.1029/2020WR029466)

acs

*AutoCorrelation Structure***Description**

Provides a parametric function that describes the values of the linear autocorrelation up to desired lags. For more details on the parametric autocorrelation structures see section 3.2 in Papalexiou (2018).

Usage

```
acs(id, ...)
```

Arguments

id	autocorrelation structure id
...	other arguments (t as lag and acs parameters)

References

Papalexiou, S.M. (2018). Unified theory for stochastic modelling of hydroclimatic processes: Preserving marginal distributions, correlation structures, and intermittency. *Advances in Water Resources*, 115, 234-252, doi: [10.1016/j.advwatres.2018.02.013](https://doi.org/10.1016/j.advwatres.2018.02.013)

Examples

```
library(CoSMoS)

## specify lag
t <- 0:10

## get the ACS
f <- acs('fgn', t = t, H = .75)
b <- acs('burrXII', t = t, scale = 1, shape1 = .6, shape2 = .4)
w <- acs('weibull', t = t, scale = 2, shape = 0.8)
p <- acs('paretoII', t = t, scale = 3, shape = 0.3)

## visualize the ACS
dta <- data.table(t, f, b, w, p)

m.dta <- melt(dta, id.vars = 't')

ggplot(m.dta,
  aes(x = t,
    y = value,
    group = variable,
    colour = variable)) +
  geom_point(size = 2.5) +
  geom_line(lwd = 1) +
```

```

scale_color_manual(values = c('steelblue4', 'red4', 'green4', 'darkorange'),
                    labels = c('FGN', 'Burr XII', 'Weibull', 'Pareto II'),
                    name = '') +
labs(x = bquote(lag ~ tau),
     y = 'Acf') +
scale_x_continuous(breaks = t) +
theme_classic()

```

actpnts

AutoCorrelation Transformed Points

Description

Transforms a Gaussian process in order to match a target marginal lowers its autocorrelation values. The actpnts evaluates the corresponding autocorrelations for the given target marginal for a set of Gaussian correlations, i.e., it returns (ρ_x, ρ_z) points where ρ_x and ρ_z represent, respectively, the autocorrelations of the target and Gaussian process.

Usage

```
actpnts(margdist, margarg, p0 = 0, distbounds = c(-Inf, Inf))
```

Arguments

margdist	target marginal distribution
margarg	list of marginal distribution arguments
p0	probability zero
distbounds	distribution bounds (default set to c(-Inf, Inf))

Examples

```

library(CoSMoS)

## here we target to a process that has the Pareto type II
## marginal distribution with scale parameter 1 and shape parameter 0.3
## (note that all parameters have to be named)
dist <- 'paretoII'
distarg <- list(scale = 1, shape = .3)

x <- actpnts(margdist = dist, margarg = distarg, p0 = 0)
x

## you can see the points by using
ggplot(x,
       aes(x = rhox,
           y = rhoz)) +
  geom_point(colour = 'royalblue4', size = 2.5) +

```



```
## visualize advection field
dta <- data.frame(lon = coord[,1], lat = coord[,2], u = af[,1], v = af[,2])
ggplot(dta, aes(x = lon, y = lat, u = u, v = v)) +
  geom_quiver() +
  theme_light()
```

advectionFhyperbolic *Hyperbolic advection field*

Description

Provides an advection field with hyperbolic trajectories.

Usage

```
advectionFhyperbolic(spacepoints, x0, y0, a, b)
```

Arguments

spacepoints	vector of coordinates (2 x d), where d is the number of locations/grid points
x0	x coordinate of the center of hyperbola
y0	y coordinate of the center of hyperbola
a	parameter controlling the x component of rotational velocity
b	parameter controlling the y component of rotational velocity

Note

- if $a > 0$, $b > 0$: toward bottom-left and top-right corner
- if $a < 0$, $b < 0$: toward top-left and bottom-right corner

References

Papalexiou, S.M., Serinaldi, F., Porcu, E. (2021). Advancing Space-Time Simulation of Random Fields: From Storms to Cyclones and Beyond. *Water Resources Research*, 57, e2020WR029466, doi: [10.1029/2020WR029466](https://doi.org/10.1029/2020WR029466)

Examples

```
library(ggquiver)
library(ggplot2)
## specify coordinates
m = 25
aux <- seq(0, m - 1, length = m)
coord <- expand.grid(aux, aux)
```

```
af <- advectionFhyperbolic(spacepoints = coord,
                           x0 = floor(m / 2),
                           y0 = floor(m / 2),
                           a = 3,
                           b = 2)

## visualize advection field
dta <- data.frame(lon = coord[,1], lat = coord[,2], u = af[,1], v = af[,2])
ggplot(dta, aes(x = lon, y = lat, u = u, v = v)) +
  geom_quiver() +
  theme_light()
```

advectionFradial	<i>Radial advection field</i>
------------------	-------------------------------

Description

Provides an advection field corresponding to radial motion from or towards a specified reference point.

Usage

```
advectionFradial(spacepoints, x0, y0, a, b)
```

Arguments

spacepoints	vector of coordinates (2 x d), where d is the number of locations/grid points
x0	x coordinate of the center of radial motion
y0	y coordinate of the center of radial motion
a	parameter controlling the x component of radial velocity
b	parameter controlling the y component of radial velocity

Note

- if $a > 0$, $b > 0$: divergence from (x_0, y_0) (source point effect)
- if $a < 0$, $b < 0$: convergence to (x_0, y_0) (sink effect)

References

Papalexiou, S.M., Serinaldi, F., Porcu, E. (2021). Advancing Space-Time Simulation of Random Fields: From Storms to Cyclones and Beyond. *Water Resources Research*, 57, e2020WR029466, doi: [10.1029/2020WR029466](https://doi.org/10.1029/2020WR029466)

Examples

```

library(ggquiver)
library(ggplot2)

## specify coordinates
m = 25
aux <- seq(0, m - 1, length = m)
coord <- expand.grid(aux, aux)

af <- advectionFradial(spacepoints = coord,
                      x0 = floor(m / 2),
                      y0 = floor(m / 2),
                      a = 3,
                      b = 2)

## visualize advection field
dta <- data.frame(lon = coord[,1], lat = coord[,2], u = af[,1], v = af[,2])
ggplot(dta, aes(x = lon, y = lat, u = u, v = v)) +
  geom_quiver() +
  theme_light()

```

advectionFrotation	<i>Rotational advection field</i>
--------------------	-----------------------------------

Description

Provides an advection field corresponding to rotation around a specified center.

Usage

```
advectionFrotation(spacepoints, x0, y0, a, b)
```

Arguments

spacepoints	vector of coordinates (2 x d), where d is the number of locations/grid points
x0	x coordinate of the center of rotation
y0	y coordinate of the center of rotation
a	parameter controlling the x component of rotational velocity
b	parameter controlling the y component of rotational velocity

Note

- if $a > 0$, $b > 0$: clockwise rotation around (x_0, y_0)
- if $a < 0$, $b < 0$: counter-clockwise rotation around (x_0, y_0)

References

Papalexiou, S.M., Serinaldi, F., Porcu, E. (2021). Advancing Space-Time Simulation of Random Fields: From Storms to Cyclones and Beyond. Water Resources Research, 57, e2020WR029466, doi: [10.1029/2020WR029466](https://doi.org/10.1029/2020WR029466)

Examples

```
library(ggquiver)
library(ggplot2)
## specify coordinates
m = 25
aux <- seq(0, m - 1, length = m)
coord <- expand.grid(aux, aux)

af <- advectionFrotation(spacepoints = coord,
                        x0 = floor(m / 2),
                        y0 = floor(m / 2),
                        a = 3,
                        b = 2)

## visualize advection field
dta <- data.frame(lon = coord[,1], lat = coord[,2], u = af[,1], v = af[,2])
ggplot(dta, aes(x = lon, y = lat, u = u, v = v)) +
  geom_quiver() +
  theme_light()
```

advectionFspiral	<i>Spiraling advection field</i>
------------------	----------------------------------

Description

Provides an advection field corresponding to a spiral motion to/from a specified reference point (sink).

Usage

```
advectionFspiral(spacepoints, x0, y0, a, b, rotation = 1)
```

Arguments

spacepoints	vector of coordinates (2 x d), where d is the number of locations/grid points
x0	x coordinate of reference point (sink)
y0	y coordinate of reference point (sink)
a	parameter controlling the x component of rotational velocity
b	parameter controlling the y component of rotational velocity
rotation	parameter controlling the rotational direction. The following combinations hold:

- if $a > 0$, $b > 0$, and $\text{direction} = 1$: spiraling CLOCKWISE TO (x_0, y_0)
- if $a < 0$, $b < 0$, and $\text{direction} = 1$: spiraling COUNTER-CLOCKWISE FROM (x_0, y_0)
- if $a > 0$, $b > 0$, and $\text{direction} = 2$: spiraling COUNTER-CLOCKWISE TO (x_0, y_0)
- if $a < 0$, $b < 0$, and $\text{direction} = 2$: spiraling CLOCKWISE FROM (x_0, y_0)

References

Papalexiou, S.M., Serinaldi, F., Porcu, E. (2021). Advancing Space-Time Simulation of Random Fields: From Storms to Cyclones and Beyond. Water Resources Research, 57, e2020WR029466, doi: [10.1029/2020WR029466](https://doi.org/10.1029/2020WR029466)

Examples

```
library(ggquiver)
library(ggplot2)
## specify coordinates
m = 25
aux <- seq(0, m - 1, length = m)
coord <- expand.grid(aux, aux)

af <- advectionFspiral(spacepoints = coord,
                      x0 = floor(m / 2),
                      y0 = floor(m / 2),
                      a = 3,
                      b = 2,
                      rotation = 1)

## visualize advection field
dta <- data.frame(lon = coord[,1], lat = coord[,2], u = af[,1], v = af[,2])
ggplot(dta, aes(x = lon, y = lat, u = u, v = v)) +
  geom_quiver() +
  theme_light()
```

advectionFspiralCE	<i>Spiraling advection field satisfying continuity equation</i>
--------------------	---

Description

Provides an advection field corresponding to a spiral motion to/from a specified reference point (sink) satisfying continuity equation (from [John Burkardt's website](#)).

Usage

```
advectionFspiralCE(spacepoints, a, C)
```

Arguments

spacepoints	vector of coordinates (2 x d), where d is the number of locations/grid points
a	parameter controlling the intensity of rotational velocity (a > 0 clockwise; a < 0 conter-clockwise)
C	parameter ranging in (0, 2*pi)

References

Papalexiou, S.M., Serinaldi, F., Porcu, E. (2021). Advancing Space-Time Simulation of Random Fields: From Storms to Cyclones and Beyond. Water Resources Research, 57, e2020WR029466, doi: [10.1029/2020WR029466](https://doi.org/10.1029/2020WR029466)

Examples

```
library(ggquiver)
library(ggplot2)
## specify coordinates
m = 25
aux <- seq(0, m - 1, length = m)
coord <- expand.grid(aux, aux)

af <- advectionFspiralCE(spacepoints = coord,
                        a = 5,
                        C = 1)

## visualize advection field
dta <- data.frame(lon = coord[,1], lat = coord[,2], u = af[,1], v = af[,2])
ggplot(dta, aes(x = lon, y = lat, u = u, v = v)) +
  geom_quiver() +
  theme_light()
```

advectionFuniform	<i>Uniform advection field</i>
-------------------	--------------------------------

Description

Provides an advection field with constant orthogonal (u and v) components at each grid point. This mimics rigid translation in a given direction according to the components u and v of the velocity vector.

Usage

```
advectionFuniform(spacepoints, u, v)
```

Arguments

spacepoints	vector of coordinates (2 x d), where d is the number of locations/grid points
u	velocity component along the x axis
v	velocity component along the y axis

References

Papalexiou, S.M., Serinaldi, F., Porcu, E. (2021). Advancing Space-Time Simulation of Random Fields: From Storms to Cyclones and Beyond. *Water Resources Research*, 57, e2020WR029466, doi: [10.1029/2020WR029466](https://doi.org/10.1029/2020WR029466)

Examples

```
library(ggquiver)
library(ggplot2)
## specify coordinates
m = 25
aux <- seq(0, m - 1, length = m)
coord <- expand.grid(aux, aux)

af <- advectionFuniform(spacepoints = coord,
                        u = 2,
                        v = 6)

## visualize advection field
dta <- data.frame(lon = coord[,1], lat = coord[,2], u = af[,1], v = af[,2])
ggplot(dta, aes(x = lon, y = lat, u = u, v = v)) +
  geom_quiver() +
  theme_light()
```

analyzeTS

The Functions analyzeTS, reportTS, and simulateTS

Description

Provide a complete set of tools to make time series analysis a piece of cake - analyzeTS automatically performs seasonal analysis, fits distributions and correlation structures, reportTS provides visualizations of the fitted distributions and correlation structures, and a table with the values of the fitted parameters and basic descriptive statistics, simulateTS automatically takes the results of analyzeTS and generates synthetic ones.

Usage

```
analyzeTS(
  TS,
  season = "month",
  dist = "ggamma",
  acsID = "weibull",
  norm = "N1",
  n.points = 30,
  lag.max = 30,
  constrain = FALSE,
  opts = NULL
```

```
)

reportTS(aTS, method = "dist")

simulateTS(aTS, from = NULL, to = NULL)
```

Arguments

TS	time series in format - date, value
season	name of the season (e.g. month, week)
dist	name of the distribution to be fitted
acsID	ID of the autocorrelation structure to be fitted
norm	norm used for distribution fitting - id ('N1', 'N2', 'N3', 'N4')
n.points	number of points to be subsetting from ecdf
lag.max	max lag for the empirical autocorrelation structure
constrain	logical - constrain shape2 parameters for finite tails
opts	minimization options
aTS	analyzed timeseries
method	report method - dist for distribution fits, acs for ACS fits and stat for basic statistical report
from	starting date/time of the simulation
to	end date/time of the simulation

Details

In practice, we usually want to simulate a natural process using some sampled time series. To generate a synthetic time series with similar characteristics to the observed values, we have to determine marginal distribution, autocorrelation structure and probability zero for each individual month. This can be done by fitting distributions and autocorrelation structures with `analyzeTS`. Result can be checked with `reportTS`. Synthetic time series with the same statistical properties can be produced with `simulateTS`.

Recommended distributions for variables:

- *precipitation*: ggamma (Generalized Gamma), burr### (Burr type)
- *streamflow*: ggamma (Generalized Gamma), burr### (Burr type)
- *relative humidity*: beta
- *temperature*: norm (Normal distribution)

Examples

```
library(CoSMoS)

## Load data included in the package
## (to find out more about the data use ?precip)
data('precip')
```

```

## Fit seasonal ACSs and distributions to the data
a <- analyzeTS(precip)

reportTS(a, 'dist') ## show seasonal distribution fit
reportTS(a, 'acs') ## show seasonal ACS fit
reportTS(a, 'stat') ## display basic descriptive statistics

#####
## 'duplicate' analyzed time series ##
sim <- simulateTS(a)

## plot the result
precip[, id := 'observed']
sim[, id := 'simulated']

dta <- rbind(precip, sim)

ggplot(dta) +
  geom_line(aes(x = date, y = value)) +
  facet_wrap(~id, ncol = 1) +
  theme_classic()

#####
## or simulate timeseries of different length ##
sim <- simulateTS(a,
  from = as.POSIXct('1978-12-01 00:00:00'),
  to = as.POSIXct('2008-12-01 00:00:00'))

## and plot the result
precip[, id := 'observed']
sim[, id := 'simulated']

dta <- rbind(precip, sim)

ggplot(dta) +
  geom_line(aes(x = date, y = value)) +
  facet_wrap(~id, ncol = 1) +
  theme_classic()

```

Description

Provides parametric functions that describe different types of planar deformation fields, including affine (rotation and stretching), and swirl-like deformation. For more details see Papalexiou et al.(2021) and references therein.

Usage

```
anisotropyT(id, ...)
```

Arguments

<code>id</code>	anisotropy type id (affine, swirl, and wave)
<code>...</code>	additional arguments (vector of coordinates and parameters of the anisotropy transformations)

References

Papalexiou, S. M., Serinaldi, F., Porcu, E. (2021). Advancing Space-Time Simulation of Random Fields: From Storms to Cyclones and Beyond, Water Resources Research, doi: [10.1029/2020WR029466](https://doi.org/10.1029/2020WR029466)

Examples

```
library(CoSMoS)

## specify coordinates
m = 25
aux <- seq(0, m - 1, length = m)
coord <- expand.grid(aux, aux)

## get the anisotropy field
at1 <- anisotropyT('affine',
  spacepoints = coord,
  phi1 = 0.5,
  phi2 = 2,
  phi12 = 0,
  theta = -pi/3)
at2 <- anisotropyT('swirl',
  spacepoints = coord,
  x0 = floor(m / 2),
  y0 = floor(m / 2),
  b = 10,
  alpha = 1.5 * pi)
at3 <- anisotropyT('wave',
  spacepoints = coord,
  phi1 = 0.5,
  phi2 = 2,
  beta = 3,
  theta = 0)

## visualize anisotropy field
aux = data.frame(lon = at2[,1], lat = at2[,2], id1 = rep(1:m, each = m), id2 = rep(1:m, m))
ggplot(aux, aes(x = lon, y = lat)) +
  geom_path(aes(group = id1)) +
  geom_path(aes(group = id2)) +
  geom_point(col = 2) +
  theme_light()
```

anisotropyTaffine	<i>Affine anisotropy transformation</i>
-------------------	---

Description

Affine anisotropy transformation.

Usage

```
anisotropyTaffine(spacepoints, phi1, phi2, phi12, theta)
```

Arguments

spacepoints	vector of coordinates (2 x d), where d is the number of locations/grid points
phi1	stretching parameter along the x axis
phi2	stretching parameter along the y axis
phi12	shear effect
theta	rotation angle

References

Allard, D., Senoussi, R., Porcu, E. (2016). Anisotropy Models for Spatial Data. *Mathematical Geosciences*, 48(3), 305-328, doi: [10.1007/s110040159594x](https://doi.org/10.1007/s110040159594x)

Papalexiou, S.M., Serinaldi, F., Porcu, E. (2021). Advancing Space-Time Simulation of Random Fields: From Storms to Cyclones and Beyond. *Water Resources Research*, 57, e2020WR029466, doi: [10.1029/2020WR029466](https://doi.org/10.1029/2020WR029466)

Examples

```
## specify coordinates
m = 25
aux <- seq(0, m - 1, length = m)
coord <- expand.grid(aux, aux)

at <- anisotropyTaffine(spacepoints = coord,
                        phi1 = 0.5,
                        phi2 = 2,
                        phi12 = 0,
                        theta = -pi/3)

## visualize transformed coordinate system
aux = data.frame(lon = at[,1], lat = at[,2], id1 = rep(1:m, each = m), id2 = rep(1:m, m))
ggplot(aux, aes(x = lon, y = lat)) +
  geom_path(aes(group = id1)) +
  geom_path(aes(group = id2)) +
```

```
geom_point(col = 2) +
theme_light()
```

anisotropyTswirl	<i>Swirl anisotropy transformation</i>
------------------	--

Description

Swirl anisotropy transformation.

Usage

```
anisotropyTswirl(spacepoints, x0, y0, b, alpha)
```

Arguments

spacepoints	vector of coordinates (2 x d), where d is the number of locations/grid points
x0	x coordinate of the center of the swirl deformation
y0	y coordinate of the center of the swirl deformation
b	scaling parameter controlling the swirl deformation
alpha	rotation angle

References

Ligas, M., Banas, M., Szafarczyk, A. (2019). A method for local approximation of a planar deformation field. Reports on Geodesy and Geoinformatics, 108(1), 1-8, doi: [10.2478/rgg20190007](https://doi.org/10.2478/rgg20190007)

Papalexiou, S.M., Serinaldi, F., Porcu, E. (2021). Advancing Space-Time Simulation of Random Fields: From Storms to Cyclones and Beyond. Water Resources Research, 57, e2020WR029466, doi: [10.1029/2020WR029466](https://doi.org/10.1029/2020WR029466)

Examples

```
## specify coordinates
m = 25
aux <- seq(0, m - 1, length = m)
coord <- expand.grid(aux, aux)

at <- anisotropyTswirl(spacepoints = coord,
                      x0 = floor(m / 2),
                      y0 = floor(m / 2),
                      b = 10,
                      alpha = 1.5 * pi)

## visualize transformed coordinate system
aux = data.frame(lon = at[,1], lat = at[,2], id1 = rep(1:m, each = m), id2 = rep(1:m, m))
ggplot(aux, aes(x = lon, y = lat)) +
```

```
geom_path(aes(group = id1)) +
geom_path(aes(group = id2)) +
geom_point(col = 2) +
theme_light()
```

anisotropyTwave	<i>Wave anisotropy transformation</i>
-----------------	---------------------------------------

Description

Wave anisotropy transformation.

Usage

```
anisotropyTwave(spacepoints, phi1, phi2, beta, theta)
```

Arguments

spacepoints	vector of coordinates (2 x d), where d is the number of locations/grid points
phi1	stretching parameter along the x axis
phi2	stretching parameter along the y axis
beta	amplitude of sinusoidal wave
theta	rotation angle

References

Papalexiou, S.M., Serinaldi, F., Porcu, E. (2021). Advancing Space-Time Simulation of Random Fields: From Storms to Cyclones and Beyond. Water Resources Research, 57, e2020WR029466, doi: [10.1029/2020WR029466](https://doi.org/10.1029/2020WR029466)

Examples

```
## specify coordinates
m = 25
aux <- seq(0, m - 1, length = m)
coord <- expand.grid(aux, aux)

at <- anisotropyTwave(spacepoints = coord,
                      phi1 = 0.5,
                      phi2 = 2,
                      beta = 3,
                      theta = 0)

## visualize transformed coordinate system
aux = data.frame(lon = at[,1], lat = at[,2], id1 = rep(1:m, each = m), id2 = rep(1:m, m))
ggplot(aux, aes(x = lon, y = lat)) +
geom_path(aes(group = id1)) +
geom_path(aes(group = id2)) +
```

```
geom_point(col = 2) +
theme_light()
```

BurrIII

Burr Type III distribution

Description

Provides density, distribution function, quantile function, random value generation, and raw moments of order r for the Burr Type III distribution.

Usage

```
dburrIII(x, scale, shape1, shape2, log = FALSE)

pburrIII(q, scale, shape1, shape2, lower.tail = TRUE, log.p = FALSE)

qburrrIII(p, scale, shape1, shape2, lower.tail = TRUE, log.p = FALSE)

rburrIII(n, scale, shape1, shape2)

mburrIII(r, scale, shape1, shape2)
```

Arguments

<code>x, q</code>	vector of quantiles.
<code>scale, shape1, shape2</code>	scale and shape parameters; the shape arguments cannot be a vectors (must have length one).
<code>log, log.p</code>	logical; if TRUE, probabilities p are given as $\log(p)$.
<code>lower.tail</code>	logical; if TRUE (default), probabilities are $P[X \leq x]$ otherwise, $P[X > x]$.
<code>p</code>	vector of probabilities.
<code>n</code>	number of observations. If $\text{length}(n) > 1$, the length is taken to be the number required.
<code>r</code>	raw moment order

Examples

```
## plot the density

ggplot(data.frame(x = c(1, 15)),
  aes(x)) +
  stat_function(fun = dburrIII,
    args = list(scale = 5,
      shape1 = .25,
```

```

                                shape2 = .75),
                                colour = 'royalblue4') +
labs(x = '',
     y = 'Density') +
theme_classic()

```

BurrXII

*Burr Type XII distribution***Description**

Provides density, distribution function, quantile function, random value generation, and raw moments of order r for the Burr Type XII distribution.

Usage

```

dburrXII(x, scale, shape1, shape2, log = FALSE)

pburrXII(q, scale, shape1, shape2, lower.tail = TRUE, log.p = FALSE)

qburrrXII(p, scale, shape1, shape2, lower.tail = TRUE, log.p = FALSE)

rburrXII(n, scale, shape1, shape2)

mburrXII(r, scale, shape1, shape2)

```

Arguments

<code>x, q</code>	vector of quantiles.
<code>scale, shape1, shape2</code>	scale and shape parameters; the shape arguments cannot be a vector (must have length one).
<code>log, log.p</code>	logical; if TRUE, probabilities p are given as $\log(p)$.
<code>lower.tail</code>	logical; if TRUE (default), probabilities are $P[X \leq x]$ otherwise, $P[X > x]$.
<code>p</code>	vector of probabilities.
<code>n</code>	number of observations. If $\text{length}(n) > 1$, the length is taken to be the number required.
<code>r</code>	raw moment order

Examples

```

## plot the density

ggplot(data.frame(x = c(0, 10)),
       aes(x)) +
  stat_function(fun = dburrXII,

```

```

      args = list(scale = 5,
                  shape1 = .25,
                  shape2 = .75),
      colour = 'royalblue4') +
labs(x = '',
     y = 'Density') +
theme_classic()

```

checkRF

*Numerical and visual check of generated random fields***Description**

Compares generated random fields sample statistics with the theoretically expected values (similar to [checkTS](#)). It also returns graphical output for visual check.

Usage

```
checkRF(RF, lags = 30, nfields = 49, method = "stat")
```

Arguments

RF	output of generateRF
lags	number of lags of empirical STCF to be considered in the graphical output (default set to 30)
nfields	number of fields to be used in the numerical and graphical output (default set to 49). As the plots are arranged in a matrix with nrows as close as possible to ncol, we suggest using values such as 3x3, 3x4, 7x8, etc.
method	report method - 'stat' for basic statistical report, 'statplot' for graphical check of lagged SCS, target STCS, and marginal distribution, 'field' for plotting a matrix of the first nfields, and 'movie' to save the first nfields as a GIF file named "movieRF.gif" in the current working directory

Examples

```

## The example below refers to the fitting and simulation of 10 random fields
## of size 10x10 with AR(1) temporal correlation. As the fitting algorithm has
## O((mxm)^3) complexity for a mxm field, this setting allows for quick fitting
## and simulation (short CPU time). However, for a more effective visualization
## and reliable performance assessment, we suggest to generate a larger number
## of fields (e.g. 100 or more) of size about 30X30. This setting needs more
## CPU time but enables more effective comparison of theoretical and
## empirical statistics. Sizes larger than about 50x50 can be impractical
## on standard machines.

```

```

fit <- fitVAR(
  spacepoints = 10,

```

```

p = 1,
margdist = 'burrXII',
margarg = list(scale = 3, shape1 = .9, shape2 = .2),
p0 = 0.8,
stcsid = "clayton",
stcsarg = list(scfid = "weibull", tcfid = "weibull",
               copulaarg = 2,
               scfarg = list(scale = 20, shape = 0.7),
               tcfarg = list(scale = 1.1, shape = 0.8))
)

sim <- generateRF(n = 12,
                 STmodel = fit)
checkRF(RF = sim,
        lags = 10,
        nfields = 12)

```

checkTS

*Check generated timeseries***Description**

Compares generated time series sample statistics with the theoretically expected values.

Usage

```
checkTS(TS, distbounds = c(-Inf, Inf))
```

Arguments

TS	generated timeseries
distbounds	distribution bounds (default set to c(-Inf, Inf))

Examples

```

library(CoSMoS)

## check your generated timeseries
x <- generateTS(margdist = 'burrXII',
               margarg = list(scale = 1,
                             shape1 = .75,
                             shape2 = .25),
               acsvalue = acs(id = 'weibull',
                             t = 0:30,
                             scale = 10,
                             shape = .75),
               n = 1000, p = 30, p0 = .5, TSn = 5)

```

checkTS(x)

disch

Daily streamflow data data

Description

Station details

- Name: Nassawango Creek near Snow Hill, Worcester County, Maryland, Hydrologic Unit 02080111
- Network Id: , USGS 01485500
- Latitude/Longitude: 38°13'44.1", 75°28'17.2"
- Elevation: 11.49 ft above North American Vertical Datum of 1988.
- Measurement unit: cubic feet per second

Usage

disch

Format

A data.table with 23315 rows and 2 variables:

date POSIXct format date/time

value daily avarage values

Details

more details can be found [here](#).

Source

The United States Geological Survey (USGS) National Water Information System (NWIS)

fitactf

Fit the AutoCorrelation Transformation Function

Description

Fits the ACTF (Autocorrelation Transformation Function) to the estimated points (ρ_x, ρ_z) using nls.

Usage

```
fitactf(actpnts, discrete = FALSE)
```

Arguments

actpnts	estimated ACT points
discrete	logical - is the marginal distribution discrete?

Examples

```
library(CoSMoS)

## choose the marginal distribution as Pareto type II
## with corresponding parameters
dist <- 'paretoII'
distarg <- list(scale = 1, shape = .3)

## estimate rho 'x' and 'z' points using ACTI
p <- actpnts(margdist = dist, margarg = distarg, p0 = 0)

## fit ACTF
fit <- fitactf(p)

## plot the result
plot(fit)
```

fitDist

Distribution fitting

Description

Uses Nelder-Mead simplex algorithm to minimize fitting norms.

Usage

```
fitDist(
  data,
  dist,
  n.points,
  norm,
  constrain,
  opts = list(algorithm = "NLOPT_LN_NELDERMEAD", xtol_rel = 1e-08, maxeval = 10000)
)
```

Arguments

data	value to be fitted
dist	name of the distribution to be fitted
n.points	number of points to be subsetted from ecdf
norm	norm used for distribution fitting - id ('N1', 'N2', 'N3', 'N4')
constrain	logical - constrain shape2 parametes for finite tails
opts	minimization options

Examples

```
x <- fitDist(rnorm(1000), 'norm', 30, 'N1', FALSE)
x
```

fitVAR	<i>VAR model parameters to simulate correlated parent Gaussian random vectors and fields</i>
--------	--

Description

Compute VAR model parameters to simulate parent Gaussian random vectors with specified spatiotemporal correlation structure using the method described by Biller and Nelson (2003).

Usage

```
fitVAR(
  spacepoints,
  p,
  margdist,
  margarg,
  p0,
  distbounds = c(-Inf, Inf),
  stcsid,
  stcsarg,
```

```

    scalefactor = 1,
    anisotropyid = "affine",
    anisotropyarg = list(phi1 = 1, phi2 = 1, phi12 = 0, theta = 0),
    advectionid = "uniform",
    advectionarg = list(u = 0, v = 0)
)

```

Arguments

spacepoints	it can be a numeric integer, which is interpreted as the side length m of the square field ($m \times m$), or a matrix ($d \times 2$) of coordinates (e.g. longitude and latitude) of d spatial locations (e.g. d gauge stations)
p	order of VAR(p) model
margdist	target marginal distribution of the field
margarg	list of marginal distribution arguments. Please consult the documentation of the selected marginal distribution indicated in the argument <code>margdist</code> for the list of required parameters
p0	probability zero
distbounds	distribution bounds (default set to <code>c(-Inf, Inf)</code>)
stcsid	spatiotemporal correlation structure ID
stcsarg	list of spatiotemporal correlation structure arguments. Please consult the documentation of the selected spatiotemporal correlation structure indicated in the argument <code>stcsid</code> for the list of required parameters
scalefactor	factor specifying the distance between the centers of two pixels (default set to 1)
anisotropyid	spatial anisotropy ID (affine by default, swirl or wave)
anisotropyarg	list of arguments characterizing the spatial anisotropy according to the syntax of the function anisotropyT . Isotropic fields by default
advectionid	advection field ID (uniform by default, rotation, spiral, spiralCE, radial, or hyperbolic)
advectionarg	list of arguments characterizing the advection field according to the syntax of the function advectionF . No advection by default

Details

The fitting algorithm has $O(m*m)^3$ complexity for a $(m*m)$ field or equivalently $O(d^3)$ complexity for a d -dimensional vector. Very large values of $(m*m)$ (or d) and high order AR correlation structures can be unpractical on standard machines.

Here, we give indicative CPU times for some settings, referring to a Windows 10 Pro x64 laptop with Intel(R) Core(TM) i7-6700HQ CPU @ 2.60GHz, 4-core, 8 logical processors, and 32GB RAM.

: CPU time:

$d = 100$ or $m = 10$, $p = 1$: $\sim 0.4s$

$d = 900$ or $m = 30$, $p = 1$: $\sim 6.0s$

$d = 900$ or $m = 30$, $p = 5$: $\sim 47.0s$

$d = 2500$ or $m = 50$, $p = 1$: $\sim 100.0s$

Note

While all the advection types can be applied to isotropic random fields, anisotropic random fields require more care. We suggest combining affine anisotropy with uniform advection, and `swirl` anisotropy with rotation or spiral advection with the same rotation center.

References

- Biller, B., Nelson, B.L. (2003). Modeling and generating multivariate time-series input processes using a vector autoregressive technique. *ACM Trans. Model. Comput. Simul.* 13(3), 211-237, doi: [10.1145/937332.937333](https://doi.org/10.1145/937332.937333)
- Papalexiou, S.M. (2018). Unified theory for stochastic modelling of hydroclimatic processes: Preserving marginal distributions, correlation structures, and intermittency. *Advances in Water Resources*, 115, 234-252, doi: [10.1016/j.advwatres.2018.02.013](https://doi.org/10.1016/j.advwatres.2018.02.013)
- Papalexiou, S.M., Serinaldi, F. (2020). Random Fields Simplified: Preserving Marginal Distributions, Correlations, and Intermittency, With Applications From Rainfall to Humidity. *Water Resources Research*, 56(2), e2019WR026331, doi: [10.1029/2019WR026331](https://doi.org/10.1029/2019WR026331)
- Papalexiou, S.M., Serinaldi, F., Porcu, E. (2021). Advancing Space-Time Simulation of Random Fields: From Storms to Cyclones and Beyond. *Water Resources Research*, 57, e2020WR029466, doi: [10.1029/2020WR029466](https://doi.org/10.1029/2020WR029466)

Examples

```
## for multivariate simulation
coord <- cbind(runif(4)*30, runif(4)*30)

fit <- fitVAR(
  spacepoints = coord,
  p = 1,
  margdist = 'burrXII',
  margarg = list(scale = 3,
                 shape1 = .9,
                 shape2 = .2),
  p0 = 0.8,
  stcsid = "clayton",
  stcsarg = list(scfid = "weibull",
                 tcfid = "weibull",
                 copulaarg = 2,
                 scfarg = list(scale = 20,
                              shape = 0.7),
                 tcfarg = list(scale = 1.1,
                              shape = 0.8))
)

dim(fit$alpha)
dim(fit$res.cov)

fit$m
fit$margarg
fit$margdist
```

```
## for random fields simulation
fit <- fitVAR(
  spacepoints = 10,
  p = 1,
  margdist = 'burrXII',
  margarg = list(scale = 3, shape1 = .9, shape2 = .2),
  p0 = 0.8,
  stcsid = "clayton",
  stcsarg = list(scfid = "weibull", tcfid = "weibull",
    copulaarg = 2,
    scfarg = list(scale = 20, shape = 0.7),
    tcfarg = list(scale = 1.1, shape = 0.8))
)

dim(fit$alpha)
dim(fit$res.cov)

fit$m
fit$margarg
fit$margdist
```

generateMTS

Simulation of multiple time series with given marginals and spatiotemporal properties

Description

Generates multiple time series with given marginals and spatiotemporal properties, just provide (1) the output of [fitVAR](#) function, and (2) the number of time steps to simulate.

Usage

```
generateMTS(n, STmodel)
```

Arguments

n	number of fields (time steps) to simulate
STmodel	list of arguments resulting from fitVAR function

Details

Referring to the documentation of [fitVAR](#) for details on computational complexity of the fitting algorithm, here we report indicative simulation CPU times for some settings, assuming that the model parameters are already evaluated. CPU times refer to a Windows 10 Pro x64 laptop with Intel(R) Core(TM) i7-6700HQ CPU @ 2.60GHz, 4-core, 8 logical processors, and 32GB RAM.

CPU time:

d = 900, p = 1, n = 1000: ~17s

d = 900, p = 1, n = 10000: ~75s

$d = 900, p = 5, n = 100$: ~280s
 $d = 900, p = 5, n = 1000$: ~302s
 $d = 2500, p = 1, n = 1000$: ~160s
 $d = 2500, p = 1, n = 10000$: ~570s
 where d denotes the number of spatial locations

Examples

```

## Simulation of a 4-dimensional vector with VAR(1) correlation structure
coord <- cbind(runif(4)*30, runif(4)*30)

fit <- fitVAR(
  spacepoints = coord,
  p = 1,
  margdist = 'burrXII',
  margarg = list(scale = 3,
                 shape1 = .9,
                 shape2 = .2),
  p0 = 0.8,
  stcsid = "clayton",
  stcsarg = list(scfid = "weibull",
                 tcfid = "weibull",
                 copulaarg = 2,
                 scfarg = list(scale = 20,
                              shape = 0.7),
                 tcfarg = list(scale = 1.1,
                              shape = 0.8))
)

sim <- generateMTS(n = 100,
                  STmodel = fit)

```

generateMTSFast	<i>Faster simulation of multiple time series with approximately separable spatiotemporal correlation structure</i>
-----------------	--

Description

For more details see section 6 in Serinaldi and Kilsby (2018), and section 2.4 in Papalexiou and Serinaldi (2020).

Usage

```

generateMTSFast(
  n,
  spacepoints,
  margdist,
  margarg,

```

```

    p0,
    distbounds = c(-Inf, Inf),
    stcsid,
    stcsarg,
    scalefactor = 1,
    anisotropyid = "affine",
    anisotropyarg = list(phi1 = 1, phi2 = 1, phi12 = 0, theta = 0)
)

```

Arguments

n	number of fields (time steps) to simulate
spacepoints	matrix (d x 2) of coordinates (e.g. longitude and latitude) of d spatial locations (e.g. d gauge stations)
margdist	target marginal distribution
margarg	list of marginal distribution arguments. Please consult the documentation of the selected marginal distribution indicated in the argument <code>margdist</code> for the list of required parameters
p0	probability zero
distbounds	distribution bounds (default set to <code>c(-Inf, Inf)</code>)
stcsid	spatiotemporal correlation structure ID
stcsarg	list of spatiotemporal correlation structure arguments. Please consult the documentation of the selected spatiotemporal correlation structure indicated in the argument <code>stcsid</code> for the list of required parameters
scalefactor	factor specifying the distance between the centers of two pixels (default set to 1)
anisotropyid	spatial anisotropy ID (affine by default, swirl or wave)
anisotropyarg	list of arguments characterizing the spatial anisotropy according to the syntax of the function anisotropyT . Isotropic fields by default

Details

[generateMTSFast](#) provides a faster approach to multivariate simulation compared to [generateMTS](#) by exploiting circulant embedding fast Fourier transformation. However, this approach is feasible only for approximately separable target spatiotemporal correlation functions. [generateMTSFast](#) comprises fitting and simulation in a single function. Here, we give indicative CPU times for some settings, referring to a Windows 10 Pro x64 laptop with Intel(R) Core(TM) i7-6700HQ CPU @ 2.60GHz, 4-core, 8 logical processors, and 32GB RAM.

CPU time:

d = 2500, n = 1000: ~58s

d = 2500, n = 10000: ~160s

d = 10000, n = 1000: ~2955s (~50min)

References

Serinaldi, F., Kilsby, C.G. (2018). Unsurprising Surprises: The Frequency of Record-breaking and Overthreshold Hydrological Extremes Under Spatial and Temporal Dependence. *Water Resources Research*, 54(9), 6460-6487, doi: [10.1029/2018WR023055](https://doi.org/10.1029/2018WR023055)

Papalexiou, S.M., Serinaldi, F. (2020). Random Fields Simplified: Preserving Marginal Distributions, Correlations, and Intermittency, With Applications From Rainfall to Humidity. *Water Resources Research*, 56(2), e2019WR026331, doi: [10.1029/2019WR026331](https://doi.org/10.1029/2019WR026331)

Examples

```
coord <- cbind(runif(4)*30, runif(4)*30)

sim <- generateMTSFast(
  n = 50,
  spacepoints = coord,
  p0 = 0.7,
  margdist = 'paretoII',
  margarg = list(scale = 1,
                 shape = .3),
  stcsarg = list(scfid = "weibull",
                 tcfid = "weibull",
                 scfarg = list(scale = 20,
                              shape = 0.7),
                 tcfarg = list(scale = 1.1,
                              shape = 0.8))
)
```

generateRF	<i>Simulation of random field with given marginals and spatiotemporal properties</i>
------------	--

Description

Generates random field with given marginals and spatiotemporal properties, just provide (1) the output of [fitVAR](#) function, and (2) the number of time steps to simulate.

Usage

```
generateRF(n, STmodel)
```

Arguments

n	number of fields (time steps) to simulate
STmodel	list of arguments resulting from fitVAR function

Details

Referring to the documentation of `fitVAR` for details on computational complexity of the fitting algorithm, here we report indicative simulation CPU times for some settings, assuming that the model parameters are already evaluated. CPU times refer to a Windows 10 Pro x64 laptop with Intel(R) Core(TM) i7-6700HQ CPU @ 2.60GHz, 4-core, 8 logical processors, and 32GB RAM.

CPU time:

$m = 30, p = 1, n = 1000$: ~17s

$m = 30, p = 1, n = 10000$: ~75s

$m = 30, p = 5, n = 100$: ~280s

$m = 30, p = 5, n = 1000$: ~302s

$m = 50, p = 1, n = 1000$: ~160s

$m = 50, p = 1, n = 10000$: ~570s where m denotes the side length of a square field ($m \times m$)

Examples

```
## The example below refers to the simulation of few random fields of
## size 10x10 with AR(1) temporal correlation for the sake of illustration.
## For a more effective visualization and reliable performance assessment,
## we suggest to generate a larger number of fields (e.g. 100 or more)
## of size about 30X30.
## See section 'Details' for additional information on running times
## with different settings.
```

```
fit <- fitVAR(
  spacepoints = 10,
  p = 1,
  margdist = 'burrrXII',
  margarg = list(scale = 3, shape1 = .9, shape2 = .2),
  p0 = 0.8,
  stcsid = "clayton",
  stcsarg = list(scfid = "weibull", tcfid = "weibull",
    copulaarg = 2,
    scfarg = list(scale = 20, shape = 0.7),
    tcfarg = list(scale = 1.1, shape = 0.8))
)
```

```
sim <- generateRF(n = 12,
  STmodel = fit)
checkRF(sim,
  lags = 10,
  nfields = 12)
```

Description

For more details see section 6 in Serinaldi and Kilsby (2018), and section 2.4 in Papalexiou and Serinaldi (2020).

Usage

```
generateRFFast(
  n,
  spacepoints,
  margdist,
  margarg,
  p0,
  distbounds = c(-Inf, Inf),
  stcsid,
  stcsarg,
  scalefactor = 1,
  anisotropyid = "affine",
  anisotropyarg = list(phi1 = 1, phi2 = 1, phi12 = 0, theta = 0)
)
```

Arguments

n	number of fields (time steps) to simulate
spacepoints	side length m of the square field (m x m)
margdist	target marginal distribution of the field
margarg	list of marginal distribution arguments. Please consult the documentation of the selected marginal distribution indicated in the argument margdist for the list of required parameters
p0	probability zero
distbounds	distribution bounds (default set to c(-Inf, Inf))
stcsid	spatiotemporal correlation structure ID
stcsarg	list of spatiotemporal correlation structure arguments. Please consult the documentation of the selected spatiotemporal correlation structure indicated in the argument stcsid for the list of required parameters
scalefactor	factor specifying the distance between the centers of two pixels (default set to 1)
anisotropyid	spatial anisotropy ID (affine by default, swirl or wave)
anisotropyarg	list of arguments characterizing the spatial anisotropy according to the syntax of the function anisotropyT . Isotropic fields by default

Details

[generateRFFast](#) provides a faster approach to RF simulation compared to [generateRF](#) by exploiting circulant embedding fast Fourier transformation. However, this approach is feasible only for approximately separable target spatiotemporal correlation functions. [generateRFFast](#) comprises fitting and simulation in a single function. Here, we give indicative CPU times for some settings,

referring to a Windows 10 Pro x64 laptop with Intel(R) Core(TM) i7-6700HQ CPU @ 2.60GHz, 4-core, 8 logical processors, and 32GB RAM.

CPU time:

m = 50, n = 1000: ~58s

m = 50, n = 10000: ~160s

m = 100, n = 1000: ~2955s (~50min)

References

Serinaldi, F., Kilsby, C.G. (2018). Unsurprising Surprises: The Frequency of Record-breaking and Overthreshold Hydrological Extremes Under Spatial and Temporal Dependence. *Water Resources Research*, 54(9), 6460-6487, doi: [10.1029/2018WR023055](https://doi.org/10.1029/2018WR023055)

Papalexiou, S.M., Serinaldi, F. (2020). Random Fields Simplified: Preserving Marginal Distributions, Correlations, and Intermittency, With Applications From Rainfall to Humidity. *Water Resources Research*, 56(2), e2019WR026331, doi: [10.1029/2019WR026331](https://doi.org/10.1029/2019WR026331)

Examples

```
sim <- generateRFFast(
  n = 50,
  spacepoints = 3,
  p0 = 0.7,
  margdist = 'paretoII',
  margarg = list(scale = 1,
                 shape = .3),
  stcsarg = list(scfid = "weibull",
                 tcfid = "weibull",
                 scfarg = list(scale = 20,
                              shape = 0.7),
                 tcfarg = list(scale = 1.1,
                              shape = 0.8))
)

checkRF(sim,
  lags = 10,
  nfields = 49)
```

generateTS

Generate timeseries

Description

Generates timeseries with given properties, just provide (1) the target marginal distribution and its parameters, (2) the target autocorrelation structure or individual autocorrelation values up to a desired lag, and (3) the probability zero if you wish to simulate an intermittent process.

Usage

```
generateTS(
  n,
  margdist,
  margarg,
  p = NULL,
  p0 = 0,
  TSn = 1,
  distbounds = c(-Inf, Inf),
  acsvalue = NULL
)
```

Arguments

n	number of values
margdist	target marginal distribution
margarg	list of marginal distribution arguments
p	integer - model order (if NULL - limits maximum model order according to auto-correlation structure values)
p0	probability zero
TSn	number of timeseries to be generated
distbounds	distribution bounds (default set to c(-Inf, Inf))
acsvalue	target auto-correlation structure (from lag 0)

Details

A step-by-step guide:

- First define the target marginal (margdist), that is, the probability distribution of the generated data. For example set margdist = 'ggamma' if you wish to generate data following the Generalized Gamma distribution, margdist = 'burrXII' for Burr type XII distribution etc. For a full list of the distributions we support see the help [vignette](#). In general, the package supports all build-in distribution functions of R and of other packages.
- Define the parameters' values (margarg) of the distribution you selected. For example the Generalized Gamma has one scale and two shape parameters so set the desired value, e.g., margarg = list(scale = 2, shape1 = 0.9, shape2 = 0.8). Note distributions might have different number of parameters and different type of parameters (location, scale, shape). See the help [vignette](#) for details on the parameters of each distribution we support.
- If you wish your time series to be intermittent (e.g., precipitation), then define the probability zero. For example, set p0 = 0.9, if you wish your generated data to have 90% of zero values (dry days).
- Define your linear autocorrelations.
 - You can supply specific lag autocorrelations starting from lag 0 and up to a desired lag, e.g., acs = c(1, 0.9, 0.8, 0.7); this will generate a process with lag1, 2 and 3 autocorrelations equal with 0.9, 0.8 and 0.7.

- Alternatively, you can use a parametric autocorrelation structure (see section 3.2 in Papalexiou (2018)). We support the following autocorrelation structures (acs) weibull, paretoII, fgn and burrXII. See also [acs](#) examples.
- Define the order to the autoregressive model p. For example if you aim to preserve the first 10 lag autocorrelations then just set p = 10. Otherwise set it p = NULL and the model will decide the value of p in order to preserve the whole autocorrelation structure.
- Lastly just define the time series length, e.g., n = 1000 and number of time series you wish to generate, e.g., TSn = 10.

Play around with the following given examples which will make the whole process a piece of cake.

References

Papalexiou, S.M. (2018). Unified theory for stochastic modelling of hydroclimatic processes: Preserving marginal distributions, correlation structures, and intermittency. *Advances in Water Resources*, 115, 234-252, doi: [10.1016/j.advwatres.2018.02.013](https://doi.org/10.1016/j.advwatres.2018.02.013)

Examples

```
library(CoSMoS)

## Case1:
## You wish to generate 3 time series of size 1000 each
## that follow the Generalized Gamma distribution with parameters
## scale = 1, shape1 = 0.8, shape2 = 0.8
## and autocorrelation structure the ParetoII
## with parameters scale = 1 and shape = .75
x <- generateTS(margdist = 'ggamma',
               margarg = list(scale = 1,
                             shape1 = .8,
                             shape2 = .8),
               acsvalue = acs(id = 'paretoII',
                             t = 0:30,
                             scale = 1,
                             shape = .75),
               n = 1000,
               p = 30,
               TSn = 3)

## see the results
plot(x)

## Case2:
## You wish to generate time series the same distribution
## and autocorrelations as is Case1 but intermittent
## with probability zero equal to 90%
y <- generateTS(margdist = 'ggamma',
               margarg = list(scale = 1,
                             shape1 = .8,
```

```

                                shape2 = .8),
acsvvalue = acs(id = 'paretoII',
                t = 0:30,
                scale = 1,
                shape = .75),

p0 = .9,
n = 1000,
p = 30,
TSn = 3)

## see the results
plot(y)

## Case3:
## You wish to generate a time series of size 1000
## that follows the Beta distribution
## (e.g., relative humidity ranging from 0 to 1)
## with parameters shape1 = 0.8, shape2 = 0.8, is defined from 0 to 1
## and autocorrelation structure the ParetoII
## with parameters scale = 1 and shape = .75
z <- generateTS(margdist = 'beta',
                margarg = list(shape1 = .6,
                              shape2 = .8),
                distbounds = c(0, 1),
                acsvvalue = acs(id = 'paretoII',
                                t = 0:30,
                                scale = 1,
                                shape = .75),
                n = 1000,
                p = 20)

## see the results
plot(z)

## Case4:
## Same in previous case but now you provide specific
## autocorrelation values for the first three lags,
## ie., lag 1 to 3 equal to 0.9, 0.8 and 0.7

z <- generateTS(margdist = 'beta',
                margarg = list(shape1 = .6,
                              shape2 = .8),
                distbounds = c(0, 1),
                acsvvalue = c(1, .9, .8, .7),
                n = 1000,
                p = TRUE)

## see the results
plot(z)

```

GEV	<i>Generalized extreme value distribution</i>
-----	---

Description

Provides density, distribution function, quantile function, and random value generation, for the generalized extreme value distribution.

Usage

```
dgev(x, loc, scale, shape, log = FALSE)

pgev(q, loc, scale, shape, lower.tail = TRUE, log.p = FALSE)

qgev(p, loc, scale, shape, lower.tail = TRUE, log.p = FALSE)

rgev(n, loc, scale, shape)

mgev(r, loc, scale, shape)
```

Arguments

x, q	vector of quantiles.
loc, scale, shape	location, scale and shape parameters.
log, log.p	logical; if TRUE, probabilities p are given as log(p).
lower.tail	logical; if TRUE (default), probabilities are $P[X \leq x]$ otherwise, $P[X > x]$.
p	vector of probabilities.
n	number of observations. If length(n) > 1, the length is taken to be the number required.
r	raw moment order

Examples

```
## plot the density

ggplot(data.frame(x = c(0, 20)),
  aes(x)) +
  stat_function(fun = dgev,
    args = list(loc = 1,
      scale = .5,
      shape = .15),
    colour = 'royalblue4') +
  labs(x = '',
    y = 'Density') +
  theme_classic()
```

Description

Provides density, distribution function, quantile function, random value generation, and raw moments of order r for the generalized gamma distribution.

Usage

```
dggamma(x, scale, shape1, shape2, log = FALSE)

pggamma(q, scale, shape1, shape2, lower.tail = TRUE, log.p = FALSE)

qggamma(p, scale, shape1, shape2, lower.tail = TRUE, log.p = FALSE)

rggamma(n, scale, shape1, shape2)

mggamma(r, scale, shape1, shape2)
```

Arguments

<code>x, q</code>	vector of quantiles.
<code>scale, shape1, shape2</code>	scale and shape parameters; the shape arguments cannot be a vectors (must have length one).
<code>log, log.p</code>	logical; if TRUE, probabilities p are given as $\log(p)$.
<code>lower.tail</code>	logical; if TRUE (default), probabilities are $P[X \leq x]$ otherwise, $P[X > x]$.
<code>p</code>	vector of probabilities.
<code>n</code>	number of observations. If $\text{length}(n) > 1$, the length is taken to be the number required.
<code>r</code>	raw moment order

Examples

```
## plot the density

ggplot(data.frame(x = c(0, 20)),
  aes(x)) +
  stat_function(fun = dggamma,
    args = list(scale = 5,
      shape1 = .25,
      shape2 = .75),
    colour = 'royalblue4') +
  labs(x = '',
    y = 'Density') +
  theme_classic()
```

moments	<i>Numerical estimation of moments</i>
---------	--

Description

Uses numerical integration to calculate the theoretical raw or central moments of the specified distribution.

Usage

```
moments(
  dist,
  distarg,
  p0 = 0,
  raw = T,
  central = T,
  coef = T,
  distbounds = c(-Inf, Inf),
  order = 1:4
)
```

Arguments

dist	distribution
distarg	list of distribution arguments
p0	probability zero
raw	logical - calculate raw moments?
central	logical - calculate central moments?
coef	logical - calculate coefficients (coefficient of variation, skewness and kurtosis)?
distbounds	distribution bounds (default set to c(-Inf, Inf))
order	vector of integers - raw moment orders

Examples

```
library(CoSMoS)

## Normal Distribution
moments('norm', list(mean = 2, sd = 1))

## Pareto type II
scale <- 1
shape <- .2

moments(dist = 'paretoII',
        distarg = list(shape = shape,
                        scale = scale))
```

ParetoII	<i>Pareto type II distribution</i>
----------	------------------------------------

Description

Provides density, distribution function, quantile function, random value generation and raw moments of order r for the Pareto type II distribution.

Usage

```

dparetoII(x, scale, shape, log = FALSE)

pparetoII(q, scale, shape, lower.tail = TRUE, log.p = FALSE)

qparetoII(p, scale, shape, lower.tail = TRUE, log.p = FALSE)

rparetoII(n, scale, shape)

mparetoII(r, scale, shape)

```

Arguments

<code>x, q</code>	vector of quantiles.
<code>scale, shape</code>	scale and shape parameters; the shape argument cannot be a vector (must have length one).
<code>log, log.p</code>	logical; if TRUE, probabilities p are given as $\log(p)$.
<code>lower.tail</code>	logical; if TRUE (default), probabilities are $P[X \leq x]$ otherwise, $P[X > x]$.
<code>p</code>	vector of probabilities.
<code>n</code>	number of observations. If $\text{length}(n) > 1$, the length is taken to be the number required.
<code>r</code>	raw moment order

Examples

```

## plot the density

ggplot(data.frame(x = c(0, 20)),
  aes(x)) +
  stat_function(fun = dparetoII,
    args = list(scale = 1,
      shape = .3),
    colour = 'royalblue4') +
  labs(x = '',
    y = 'Density') +
  theme_classic()

```

plot.acti

*AutoCorrelation Transformation Function visualisation***Description**

Visualizes the autocorrelation tranformation integral (there are two possible methods for plotting - base graphics and ggplot2 package).

Usage

```
## S3 method for class 'acti'
plot(x, ...)
```

Arguments

```
x          fitactf result object
...        other arguments
```

Examples

```
library(CoSMoS)

## choose the marginal distribution as Pareto type II with corresponding parameters
dist <- 'paretoII'
distrib <- list(scale = 1, shape = .3)

## estimate rho 'x' and 'z' points using ACTI
p <- actpnts(margdist = dist, margarg = distrib, p0 = 0)

## fit ACTF
fit <- fitactf(p)

## plot the results
plot(fit)
plot(fit, main = 'Pareto type II distribution \nautocorrelation tranformation')
```

plot.checkTS

*Plot method for check results***Description**

Plot method for check results.

Usage

```
## S3 method for class 'checkTS'
plot(x, ...)
```

Arguments

x	check result
...	other args

Examples

```
library(CoSMoS)

## check your generated timeseries
x <- generateTS(margdist = 'burrXII',
               margarg = list(scale = 1,
                             shape1 = .75,
                             shape2 = .15),
               acsvalue = acs(id = 'weibull',
                             t = 0:30,
                             scale = 10,
                             shape = .75),
               n = 1000, p = 30, p0 = .25, TSn = 100)

chck <- checkTS(x)

plot(chck)
```

plot.cosmosts

*Plot generated Timeseries***Description**

Visualizes Timeseries generated by the package CoSMoS.

Usage

```
## S3 method for class 'cosmosts'
plot(x, ...)
```

Arguments

x	fitactf result object
...	other arguments

Examples

```
library(CoSMoS)

## generate TS
ts <- generateTS(margdist = 'ggamma',
               margarg = list(scale = 1,
```

```

                                shape1 = .8,
                                shape2 = .8),
  acsvalue = acs(id = 'paretoII',
                 t = 0:30,
                 scale = 1,
                 shape = .75),

  n = 1000,
  p = 30,
  TSn = 2)

## plot the TS
plot(ts)

```

precip	<i>Hourly station precipitation data</i>
--------	--

Description

Station details

- Name: Philadelphia International Airport
- Network ID: COOP:366889
- Latitude/Longitude: 39.87327°, -75.22678°
- Elevation: 3m

Usage

```
precip
```

Format

A data.table with 79633 rows and 2 variables:

date POSIXct format date/time

value precipitation totals

Details

more details can be found [here](#).

Source

The National Oceanic and Atmospheric Administration (NOAA)

quickTSPlot

Quick visualization of basic timeseries properties

Description

Return timeseries diagram, empirical density function, and empirical autocorrelation function.

Usage

```
quickTSPlot(TS, ci = 0.95)
```

Arguments

TS	timeseries to plot
ci	confidence interval around the zero autocorrelation value (default set to 0.95, i.e. 95% CI)

Examples

```
no <- 1000
ggamma_sim <- rggamma(n = no, scale = 1, shape1 = 1, shape2 = .5)
quickTSPlot(ggamma_sim)
```

regenerateTS

Bulk Timeseries generation

Description

Resamples given timeseries.

Usage

```
regenerateTS(ts, TSn = 1)
```

Arguments

ts	generated timeseries using ARp
TSn	number of timeseries to be (re)generated

Details

You have used the [generateTS](#) function and you wish to generate more time series. Instead of re-running [generateTS](#) you can use [regenerateTS](#), which generates timeseries using the parameters previously calculated by the [generateTS](#) function, and thus it is faster.

Examples

```
library(CoSMoS)

## define marginal distribution and arguments with target
## autocorrelation structure
x <- generateTS(margdist = 'burrXII',
               margarg = list(scale = 1,
                             shape1 = .75,
                             shape2 = .25),
               acsvalue = acs(id = 'weibull',
                             t = 0:30,
                             scale = 10,
                             shape = .75),
               n = 1000, p = 30, p0 = .5, TSn = 3)

## generate new values with same parameters
r <- regenerateTS(x)

plot(r)
```

sample.moments	<i>Estimation of sample moments</i>
----------------	-------------------------------------

Description

Estimation of sample moments.

Usage

```
sample.moments(x, na.rm = FALSE, raw = T, central = T, coef = T, order = 1:4)
```

Arguments

x	a numeric vector of values
na.rm	a logical value indicating whether NA values should be stripped before the computation proceeds
raw	logical - calculate raw moments?
central	logical - calculate central moments?
coef	logical - calculate coefficients (coefficient of variation, skewness and kurtosis)?
order	vector of integers - raw moment orders

Examples

```
library(CoSMoS)

x <- rnorm(1000)
sample.moments(x)

y <- rparetoII(1000, 10, .1)
sample.moments(y)
```

stcfclayton

Clayton SpatioTemporal Correlation Structure

Description

Provides spatiotemporal correlation structure function based on Clayton copula. For more details on the parametric spatiotemporal correlation structures see section 2.3 and 2.4 in Papalexiou and Serinaldi (2020).

Usage

```
stcfclayton(t, s, scfid, tcfid, copulaarg, scfarg, tcfarg)
```

Arguments

t	time lag
s	spatial lag (distance)
scfid	ID of the spatial (marginal) correlation structure (e.g. weibull)
tcfid	ID of the temporal (marginal) correlation structure (e.g. weibull)
copulaarg	parameter of the Clayton copula linking the marginal correlation structures
scfarg	parameters of spatial (marginal) correlation structure
tcfarg	parameters of temporal (marginal) correlation structure

References

Papalexiou, S.M., Serinaldi, F. (2020). Random Fields Simplified: Preserving Marginal Distributions, Correlations, and Intermittency, With Applications From Rainfall to Humidity. *Water Resources Research*, 56(2), e2019WR026331, doi: [10.1029/2019WR026331](https://doi.org/10.1029/2019WR026331)

Papalexiou, S.M., Serinaldi, F., Porcu, E. (2021). Advancing Space-Time Simulation of Random Fields: From Storms to Cyclones and Beyond. *Water Resources Research*, 57, e2020WR029466, doi: [10.1029/2020WR029466](https://doi.org/10.1029/2020WR029466)

Examples

```

library(plot3D)

## specify grid of spatial and temporal lags
d <- 31
st <- expand.grid(0:(d - 1),
                 0:(d - 1))

## get the STCS
wc <- stcfclayton(t = st[, 1],
                 s = st[, 2],
                 scfid = 'weibull',
                 tcfid = 'weibull',
                 copulaarg = 2,
                 scfarg = list(scale = 20,
                               shape = 0.7),
                 tcfarg = list(scale = 1.1,
                               shape = 0.8))

## visualize the STCS
wc.m <- matrix(wc,
              nrow = d)

persp3D(z = wc.m, x = 1: nrow(wc.m), y = 1:ncol(wc.m),
        expand = 1, main = "", scale = TRUE, facets = TRUE,
        xlab="Time lag", ylab = "Distance", zlab = "STCF",
        colkey = list(side = 4, length = 0.5), phi = 20, theta = 120,
        resfac = 5, col= gg2.col(100))

```

stcfgneiting14

Gneiting-14 SpatioTemporal Correlation Structure

Description

Provides spatiotemporal correlation structure function proposed by Gneiting (2002; Eq.14 at p. 593).

Usage

```
stcfgneiting14(t, s, a, c, alpha, beta, gamma, tau)
```

Arguments

t	time lag
s	spatial lag (distance)
a	nonnegative scaling parameter of time
c	nonnegative scaling parameter of space

alpha	smoothness parameter of time. Valid range: (0, 1]
beta	space-time interaction parameter. Valid range: [0, 1]
gamma	smoothness parameter of space. Valid range: (0, 1]
tau	space-time interaction parameter. Valid range: ≥ 1 (for 2-dimensional fields)

References

Gneiting, T. (2002). Nonseparable, Stationary Covariance Functions for Space-Time Data, Journal of the American Statistical Association, 97:458, 590-600, doi: [10.1198/016214502760047113](https://doi.org/10.1198/016214502760047113)

Examples

```
library(plot3D)

## specify grid of spatial and temporal lags
d <- 31
st <- expand.grid(0:(d - 1),
                 0:(d - 1))

## get the STCS
g14 <- stcfgneiting14(t = st[, 1],
                     s = st[, 2],
                     a = 1/50,
                     c = 1/10,
                     alpha = 1,
                     beta = 1,
                     gamma = 0.5,
                     tau = 1)

## visualize the STCS

g14.m <- matrix(g14,
               nrow = d)

persp3D(z = g14.m, x = 1: nrow(g14.m), y = 1:ncol(g14.m),
        expand = 1, main = "", scale = TRUE, facets = TRUE,
        xlab="Time lag", ylab = "Distance", zlab = "STCF",
        colkey = list(side = 4, length = 0.5), phi = 20, theta = 120,
        resfac = 5, col= gg2.col(100))
```

stcfgneiting16

Gneiting-16 SpatioTemporal Correlation Structure

Description

Provides spatiotemporal correlation structure function proposed by Gneiting (2002; Eq.16 at p. 594).

Usage

```
stcfgneiting16(t, s, a, c, alpha, beta, nu, tau)
```

Arguments

t	time lag
s	spatial lag (distance)
a	nonnegative scaling parameter of time
c	nonnegative scaling parameter of space
alpha	smoothness parameter of time. Valid range: (0, 1]
beta	space-time interaction parameter. Valid range: [0, 1]
nu	smoothness parameter of space. Valid range: > 0
tau	space-time interaction parameter. Valid range: ≥ 1 (for 2-dimensional fields)

References

Gneiting, T. (2002). Nonseparable, Stationary Covariance Functions for Space-Time Data, Journal of the American Statistical Association, 97:458, 590-600, doi: [10.1198/016214502760047113](https://doi.org/10.1198/016214502760047113)

Examples

```
library(plot3D)

## specify grid of spatial and temporal lags
d <- 31
st <- expand.grid(0:(d - 1),
                 0:(d - 1))

## get the STCS
g16 <- stcfgneiting16(t = st[, 1],
                     s = st[, 2],
                     a = 1/50,
                     c = 1/10,
                     alpha = 1,
                     beta = 1,
                     nu = 0.5, tau = 1)

## visualize the STCS

g16.m <- matrix(g16,
               nrow = d)

persp3D(z = g16.m, x = 1:nrow(g16.m), y = 1:ncol(g16.m),
        expand = 1, main = "", scale = TRUE, facets = TRUE,
        xlab="Time lag", ylab = "Distance", zlab = "STCF",
        colkey = list(side = 4, length = 0.5), phi = 20, theta = 120,
        resfac = 5, col= gg2.col(100))
```

stcs

*SpatioTemporal Correlation Structure***Description**

Provides a parametric function that describes the values of the linear spatiotemporal autocorrelation up to desired lags. For more details on the parametric spatiotemporal correlation structures see section 2.3 and 2.4 in Papalexiou and Serinaldi (2020).

Usage

```
stcs(id, ...)
```

Arguments

<code>id</code>	spatiotemporal correlation structure ID
<code>...</code>	additional arguments (t as time lag, s as spatial lag (distance), and stcs parameters)

References

Papalexiou, S.M., Serinaldi, F. (2020). Random Fields Simplified: Preserving Marginal Distributions, Correlations, and Intermittency, With Applications From Rainfall to Humidity. *Water Resources Research*, 56(2), e2019WR026331, doi: [10.1029/2019WR026331](https://doi.org/10.1029/2019WR026331)

Papalexiou, S.M., Serinaldi, F., Porcu, E. (2021). Advancing Space-Time Simulation of Random Fields: From Storms to Cyclones and Beyond. *Water Resources Research*, 57, e2020WR029466, doi: [10.1029/2020WR029466](https://doi.org/10.1029/2020WR029466)

Examples

```
library(plot3D)

## specify grid of spatial and temporal lags
d <- 31
st <- expand.grid(0:(d-1),
                 0:(d-1))

## get the STCS
wc <- stcs("clayton",
          t = st[, 1],
          s = st[, 2],
          scfid = 'weibull',
          tcfid = 'weibull',
          copulaarg = 2,
          scfarg = list(scale = 20,
                        shape = 0.7),
          tcfarg = list(scale = 1.1,
                        shape = 0.8))
```

```

g14 <- stcs("gneiting14",
            t = st[, 1],
            s = st[, 2],
            a = 1/50,
            c = 1/10,
            alpha = 1,
            beta = 1,
            gamma = 0.5,
            tau = 1)

g16 <- stcs("gneiting16",
            t = st[, 1],
            s = st[, 2],
            a = 1/50,
            c = 1/10,
            alpha = 1,
            beta = 1,
            nu = 0.5,
            tau = 1)

## note: for nu = 0.5 stcfgneiting16 is equivalent to
## stcfgneiting14 with gamma = 0.5

## visualize the STCS

wc.m <- matrix(wc,
               nrow = d)

persp3D(z = wc.m, x = 1: nrow(wc.m), y = 1:ncol(wc.m),
        expand = 1, main = "", scale = TRUE, facets = TRUE,
        xlab="Time lag", ylab = "Distance", zlab = "STCF",
        colkey = list(side = 4, length = 0.5), phi = 20, theta = 120,
        resfac = 5, col= gg2.col(100))

g14.m <- matrix(g14,
               nrow = d)

persp3D(z = g14.m, x = 1: nrow(wc.m), y = 1:ncol(wc.m),
        expand = 1, main = "", scale = TRUE, facets = TRUE,
        xlab="Time lag", ylab = "Distance", zlab = "STCF",
        colkey = list(side = 4, length = 0.5), phi = 20, theta = 120,
        resfac = 5, col= gg2.col(100))

```

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