

Package ‘CircNNTSRmult’

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Type Package

Title Multivariate Circular Data using MNNTS Models

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Description A collection of utilities for the statistical analysis of multivariate circular data using distributions based on Multivariate Nonnegative Trigonometric Sums (MNNTS). The package includes functions for calculation of densities and distributions, for the estimation of parameters, and more.

Depends R (>= 3.5.0), stats, psychTools, CircNNTSR

License GPL (>= 2)

LazyLoad yes

NeedsCompilation no

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Description

A collection of utilities for the statistical analysis of multivariate circular data using distributions based on Multivariate Nonnegative Trigonometric Sums (MNNTS). The package includes functions for calculation of densities and distributions, for the estimation of parameters, and more.

Details

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Version:	0.1.0
Date:	2023-09-09
License:	GLP (>=2)
Depends:	R (>= 3.5.0), stats, psychTools, CircNNTSR
LazyLoad:	yes
NeedsCompilation:	no

The MNNTS (multivariate NNTS) density on a d -dimensional ($d > 2$) hypertorus by Fernandez-Duran and Gregorio-Dominguez (2014) (see also Fernandez-Duran and Gregorio-Dominguez, 2016) for a vector of angles, $\underline{\Theta} = (\Theta_1, \Theta_2, \dots, \Theta_d)^\top$, is defined as

$$f_{\underline{\Theta}}(\underline{\theta}) = \frac{1}{(2\pi)^d} \underline{c}_{12\dots d}^H \underline{e} \underline{e}^H \underline{c}_{12\dots d}$$

$$= \frac{1}{(2\pi)^d} \sum_{k_1=0}^{M_1} \sum_{k_2=0}^{M_2} \dots \sum_{k_d=0}^{M_d} \sum_{m_1=0}^{M_1} \sum_{m_2=0}^{M_2} \dots \sum_{m_d=0}^{M_d} c_{k_1 k_2 \dots k_d} \bar{c}_{m_1 m_2 \dots m_d} e^{i \sum_{r=1}^d (k_r - m_r) \theta_r}$$

where $\underline{c}_{12\dots d}$ is a d -dimensional parameter vector of complex numbers of dimension $2 \prod_{r=1}^d (M_r + 1) - 1$ with subindexes given for all the combinations (Kronecker products) of the d vectors $\underline{M}_r = (0, 1, \dots, M_r)^\top$ for $r = 1, 2, \dots, d$ where M_r is the number of terms of the sum in the equation for the r -th component of the vector $\underline{\Theta}$. The vector $\underline{c}_{12\dots d}$ must satisfy $\underline{c}_{12\dots d}^H \underline{c}_{12\dots d} = \|\underline{c}_{12\dots d}\|^2 = \sum_{k_1=0}^{M_1} \sum_{k_2=0}^{M_2} \dots \sum_{k_d=0}^{M_d} \|c_{k_1 k_2 \dots k_d}\|^2 = 1$. For identifiability, $c_{00\dots 0}$ is a nonnegative real number. The vector $\underline{c}_{12\dots d}^H$ is the Hermitian (conjugate and transpose) of vector $\underline{c}_{12\dots d}$. The MNNTS family has many desirable properties, the marginal and conditional densities of any order of an MNNTS density are also MNNTS densities and, independence among the elements of the vector $\underline{\Theta}$ is translated into a Kronecker product decomposition in the parameter vector $\underline{c}_{12\dots d}$. For example, in the trivariate case $\underline{\Theta} = (\Theta_1, \Theta_2, \Theta_3)^\top$, if Θ_1 , Θ_2 and Θ_3 are joint independent then, $\underline{c}_{123} = \underline{c}_1 \otimes \underline{c}_2 \otimes \underline{c}_3$ where $\underline{c}_1$, $\underline{c}_2$ and $\underline{c}_3$ are the parameter vectors of the NNTS marginal densities of Θ_1 , Θ_2 and Θ_3 , respectively. Similarly, if Θ_1 is groupwise independent of $(\Theta_2, \Theta_3)^\top$ then, $\underline{c}_{123} = \underline{c}_1 \otimes \underline{c}_{23}$ where $\underline{c}_{23}$ is the parameter vector of the bivariate MNNTS density of $(\Theta_2, \Theta_3)^\top$. These results apply to higher dimensions.

Author(s)

Juan Jose Fernandez-Duran and Maria Mercedes Gregorio-Dominguez
 Maintainer: Maria Mercedes Gregorio Dominguez <mercedes@itam.mx>

References

- Fernandez-Duran, J. J. and Gregorio-Dominguez M. M. (2014) Modeling angles in proteins and circular genomes using multivariate angular distributions based on nonnegative trigonometric sums. *Statistical Applications in Genetics and Molecular Biology*, 13(1), 1-18.
- Fernandez-Duran, J. J. and Gregorio-Dominguez, M. M. (2016). CircNNTSR: an R package for the statistical analysis of circular, multivariate circular, and spherical data using nonnegative trigonometric sums. *Journal of Statistical Software*, 70, 1–19.
- Fernandez-Duran, J. J. and Gregorio-Dominguez, M. M. (2023). Multivariate Nonnegative Trigonometric Sums Distributions for High-Dimensional Multivariate Circular Data, *arXiv preprint arXiv:2301.03643v2*

EURUSDGBPBTCTimesminmax

Minimun and Maximun daily exchange rates

Description

Minimun and maximun daily bid and ask exchange rates from Euro-US dollar, GB pound-US dollar, Bitcoin-US dollar from March 22, 2019 to March 22, 2023

Usage

```
data("EURUSDGBPBTCTimesminmax")
```

Format

A data frame with 1048 observations on the following 14 variables.

id Observation number

day1 Date in format day/month/year

EURUSDAskMax Daily maximum of ask Euro-US dollar exchange rate

EURUSDAskMin Daily minimum of ask Euro-US dollar exchange rate

EURUSDBidMax Daily maximum of bid Euro-US dollar exchange rate

EURUSDBidMin Daily minimum of bid Euro-US dollar exchange rate

GBPUSDAskMax Daily maximum of ask GB pound-US dollar exchange rate

GBPUSDAskMin Daily minimum of ask GB pound-US dollar exchange rate

GBPUSDBidMax Daily maximum of bid GB pound-US dollar exchange rate

GBPUSDBidMin Daily minimum of bid GB pound-US dollar exchange rate

BTCUSDAskMax Daily maximum of ask Bitcoin-US dollar exchange rate

BTCUSDAskMin Daily minimum of ask Bitcoin-US dollar exchange rate

BTCUSDBidMax Daily maximum of bid Bitcoin-US dollar exchange rate

BTCUSDBidMin Daily minimum of bid Bitcoin-US dollar exchange rate

Source

Dukascopy publicly available tick-by-tick data

mnntestimationresultantvector
c Parameter Vector Estimate

Description

Computes the c parameter vector estimate based on the mean resultant vector of the vectors of observed trigonometric moments

Usage

```
mnntestimationresultantvector(data, M=0, R=1)
```

Arguments

data	Data frame with the observed vectors of angles. The number of columns must be equal to R
M	Vector of M parameters. A nonnegative integer number for each of the R components of the vector
R	Number of dimensions

Value

cestimates	A matrix with the index and values of the c parameters estimates of the MNNTS density
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Author(s)

Juan Jose Fernandez-Duran and Maria Mercedes Gregorio-Dominguez

References

Fernandez-Duran and J. J. and Gregorio-Dominguez and M. M (2023). Multivariate Nonnegative Trigonometric Sums Distributions for High-Dimensional Multivariate Circular Data, arXiv preprint arXiv:2301.03643v2

Examples

```
# A bivariate dataset

Mbiv<-c(2,3)
Rbiv<-length(Mbiv)
data(Nest)
data<-Nest*(pi/180)
estmeanresultant<-mnntestimationresultantvector(data, M=Mbiv, R=Rbiv)
```

```

estmeanresultant

# A trivariate dataset

Mtriv<-c(2,3,3)
Rtriv<-length(Mtriv)
data(WindDirectionsTrivariate)
data<-WindDirectionsTrivariate
estmeanresultant<-mnntestimationresultantvector(data,M=Mtriv,R=Rtriv)
estmeanresultant

```

mnntscharacteristicfunction

Characteristic Function of an MNNTS Density

Description

Computes the characteristic function from the c parameters of an MNNTS density

Usage

```
mnntscharacteristicfunction(cestimatesarray=as.data.frame(matrix(c(0,1/(2*pi)),
nrow=1,ncol=2)),M=0,R=1)
```

Arguments

cestimatesarray	output from mnntsmanifoldnewtonestimation function
M	Vector of M parameters. A nonnegative integer number for each of the R components of the vector
R	Number of dimensions

Value

A data frame (matrix) with the support and values of the characteristic function of the MNNTS density

Author(s)

Juan Jose Fernandez-Duran and Maria Mercedes Gregorio-Dominguez

References

Fernandez-Duran and J. J. and Gregorio-Dominguez and M. M (2023). Multivariate Nonnegative Trigonometric Sums Distributions for High-Dimensional Multivariate Circular Data, arXiv preprint arXiv:2301.03643v2

Examples

```
# A characteristic function from a bivariate MNNTS density

set.seed(200)
Mbiv<-c(2,3)
Rbiv<-length(Mbiv)
data(Nest)
data<-Nest*(pi/180)
est<-mnntsmanifoldnewtonestimation(data,Mbiv,Rbiv,50)
est
charfunbiv23<-mnntscharacteristicfunction(cestimatesarray=est$cestimates,M=Mbiv,R=Rbiv)
charfunbiv23

# A characteristic function from a trivariate MNNTS density

set.seed(200)
Mtriv<-c(2,3,3)
Rtriv<-length(Mtriv)
data(WindDirectionsTrivariate)
data<-WindDirectionsTrivariate
est<-mnntsmanifoldnewtonestimation(data,Mtriv,Rtriv,50)
est
charfuntriv233<-mnntscharacteristicfunction(cestimatesarray=est$cestimates,M=Mtriv,R=Rtriv)
charfuntriv233
```

mnntsconditional	<i>Conditional MNNTS density</i>
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Description

Computes the c parameters of a conditional MNNTS density at a particular value of the conditioning random vector

Usage

```
mnntsconditional(cpars=as.data.frame(matrix(c(0,0,1/(2*pi)),nrow=1,ncol=3)),
M=c(0,0),R=2,cond=1,cond.values=0)
```

Arguments

cpars	Matrix of parameters of an MNNTS density with the first R columns containing the index of the c parameter and the $R+1$ containing the complex parameter
M	Vector of M parameters. A nonnegative integer number for each of the R components of the vector
R	Number of dimensions
cond	A subset of $1:R$ indicating the elements of the vector of variables to conditioning on
cond.values	A vector of fixed values of the conditional elements of the random vector at which to conditioning on

Value

param A matrix with the index and values of the c parameters for the MNNTS conditional density

Author(s)

Juan Jose Fernandez-Duran and Maria Mercedes Gregorio-Dominguez

References

Fernandez-Duran and J. J. and Gregorio-Dominguez and M. M (2023). Multivariate Nonnegative Trigonometric Sums Distributions for High-Dimensional Multivariate Circular Data, arXiv preprint arXiv:2301.03643v2

Examples

```
# A univariate conditional from a bivariate joint

set.seed(200)
Mbiv<-c(2,3)
Rbiv<-length(Mbiv)
data(Nest)
data<-Nest*(pi/180)
est<-mnntsmanifoldnewtonestimation(data,Mbiv,Rbiv,100)
est
cpars2cond1<-mnntsconditional(cpars=est$cestimates,M=Mbiv,R=Rbiv,cond=1,cond.values=c(pi/2))
cpars2cond1
mnntsplot(cpars2cond1$cpars.cond,M=Mbiv[2])

# A bivariate conditional from a trivariate joint

set.seed(200)
Mtriv<-c(2,3,3)
Rtriv<-length(Mtriv)
data(WindDirectionsTrivariate)
data<-WindDirectionsTrivariate
est<-mnntsmanifoldnewtonestimation(data,Mtriv,Rtriv,100)
est
cpars23cond1<-mnntsconditional(cpars=est$cestimates,M=Mtriv,R=Rtriv,cond=1,cond.values=pi/4)
cpars23cond1
mnntsplot(cpars23cond1,M=Mtriv[c(2,3)])
mnntsplotwithmarginals(cpars23cond1,M=Mtriv[c(2,3)])
```

mnntsgofdesignmatrix *Design Matrix of the MNNTS Goodness of Fit Test*

Description

Computes the design matrix of the auxiliary regression for the goodness of fit test of an MNNTS density based on the estimated characteristic function

Usage

```
mnntsgofdesignmatrix(data, charfunarray, R=1)
```

Arguments

data	Matrix of angles in radians (with R columns)
charfunarray	A data frame (matrix) with the support and values of the characteristic function of the MNNTS density obtained by using the function <code>mnntscharacteristicfunction</code> with vector of parameters M of dimension R
R	Number of dimensions

Value

A matrix that is the design matrix to run the auxiliary regression for the goodness of fit test

Author(s)

Juan Jose Fernandez-Duran and Maria Mercedes Gregorio-Dominguez

References

Fernandez-Duran and J. J. and Gregorio-Dominguez and M. M (2023). Multivariate Nonnegative Trigonometric Sums Distributions for High-Dimensional Multivariate Circular Data, arXiv preprint arXiv:2301.03643v2

Fan, Y. (1997). Goodness-of-fit tests for a multivariate distribution by the empirical characteristic function. *Journal of Multivariate Analysis*, 62, 36-63.

Examples

```
# A characteristic function from a bivariate MNNTS density

set.seed(200)
Mbiv<-c(2,3)
Rbiv<-length(Mbiv)
data(Nest)
data<-Nest*(pi/180)
est<-mnntsmanifoldnewtonestimation(data,Mbiv,Rbiv,70)
est
charfunbiv23<-mnntscharacteristicfunction(ce$estimatesarray=est$ce$estimates,M=Mbiv,R=Rbiv)
charfunbiv23
designmatrix23<-mnntsgofdesignmatrix(data,charfunbiv23,R=2)
designmatrix23

# A characteristic function from a trivariate MNNTS density

set.seed(200)
Mtriv<-c(2,3,3)
Rtriv<-length(Mtriv)
data(WindDirectionsTrivariate)
data<-WindDirectionsTrivariate
```

```

est<-mnntsmanifoldnewtonestimation(data,Mtriv,Rtriv,40)
est
charfuntriv233<-mnntscharacteristicfunction(cestimatesarray=est$cestimates,M=Mtriv,R=Rtriv)
charfuntriv233
designmatrix233<-mnntsgofdesignmatrix(data,charfuntriv233,R=3)
designmatrix233

```

mnntsgofstatistics *Statistics of the MNNTS Goodness of Fit Test*

Description

Computes the statistics of the goodness of fit test of an MNNTS density based on the estimated characteristic function

Usage

```
mnntsgofstatistics(data,charfunarray,R=1)
```

Arguments

data	Matrix of angles in radians (with R columns)
charfunarray	A data frame (matrix) with the support and values of the characteristic function of the MNNTS density obtained by using the function mnntscharacteristicfunction with vector of parameters M of dimension R
R	Number of dimensions

Value

gofstat	The value of the goodness of fit statistic
gofstatnormal	The value of the normal approximation of the goodness of fit statistic

Author(s)

Juan Jose Fernandez-Duran and Maria Mercedes Gregorio-Dominguez

References

Fernandez-Duran and J. J. and Gregorio-Dominguez and M. M (2023). Multivariate Nonnegative Trigonometric Sums Distributions for High-Dimensional Multivariate Circular Data, arXiv preprint arXiv:2301.03643v2

Fan, Y. (1997). Goodness-of-fit tests for a multivariate distribution by the empirical characteristic function. *Journal of Multivariate Analysis*, 62, 36-63.

Examples

```
# A characteristic function from a bivariate MNNTS density

set.seed(200)
Mbiv<-c(2,3)
Rbiv<-length(Mbiv)
data(Nest)
data<-Nest*(pi/180)
est<-mnntsmanifoldnewtonestimation(data,Mbiv,Rbiv,70)
est
charfunbiv23<-mnntscharacteristicfunction(cestimatesarray=est$cestimates,M=Mbiv,R=Rbiv)
charfunbiv23
gofstats23<-mnntsgofstatistics(data,charfunbiv23,R=2)
gofstats23

# A characteristic function from a trivariate MNNTS density

set.seed(200)
Mtriv<-c(2,3,3)
Rtriv<-length(Mtriv)
data(WindDirectionsTrivariate)
data<-WindDirectionsTrivariate
est<-mnntsmanifoldnewtonestimation(data,Mtriv,Rtriv,50)
est
charfuntriv233<-mnntscharacteristicfunction(cestimatesarray=est$cestimates,M=Mtriv,R=Rtriv)
charfuntriv233
gofstats233<-mnntsgofstatistics(data,charfuntriv233,R=3)
gofstats233
```

mnntsmarginalgeneral *Mixing Probabilities of the Elements of the Mixture*

Description

Computes the mixing probabilities (eigenvalues) and parameter c vectors (eigenvectors) of the elements of the mixture defining a general MNNTS marginal of any dimension from an MNNTS density

Usage

```
mnntsmarginalgeneral(cpars=as.data.frame(matrix(c(0,0,1/(2*pi)),nrow=1,ncol=3)),
M=c(0,0),R=2,marginal=1)
```

Arguments

cpars	Matrix of parameters of an MNNTS density with the first R columns containing the index of the c parameter and the $R+1$ containing the complex parameter
M	Vector of M parameters. A nonnegative integer number for each of the R components of the vector

R	Number of dimensions
marginal	A subset of 1:R indicating the elements of the random vector in the marginal

Value

index	Matrix of the index of the marginal MNNTS density
eigenvectors	Matrix of the c parameter vectors of each element of the mixture. Each column is a parameter vector
eigenvalues	The vector of mixing probabilities

Author(s)

Juan Jose Fernandez-Duran and Maria Mercedes Gregorio-Dominguez

References

Fernandez-Duran and J. J. and Gregorio-Dominguez and M. M (2023). Multivariate Nonnegative Trigonometric Sums Distributions for High-Dimensional Multivariate Circular Data, arXiv preprint arXiv:2301.03643v2

Examples

```
# A univariate marginal from a bivariate joint

set.seed(200)
Mbiv<-c(2,3)
Rbiv<-length(Mbiv)
data(Nest)
data<-Nest*(pi/180)
est<-mnntsmifoldnewtonestimation(data,Mbiv,Rbiv,100)
est
cparsmarginal1<-mnntsmarginalgeneral(cpars=est$cestimates,M=Mbiv,R=Rbiv,marginal=1)
cparsmarginal1

# A bivariate marginal from a trivariate joint

set.seed(200)
Mtriv<-c(2,3,3)
Rtriv<-length(Mtriv)
data(WindDirectionsTrivariate)
data<-WindDirectionsTrivariate
est<-mnntsmifoldnewtonestimation(data,Mtriv,Rtriv,100)
est
cparsmarginal12<-mnntsmarginalgeneral(cpars=est$cestimates,M=Mtriv,R=Rtriv,marginal=c(1,2))
cparsmarginal12
```

mnntsmarginalgeneraldimension

Marginal Density Function at a Vector of Fixed Values

Description

Computes the value of the marginal density function at a set of vector of angles

Usage

```
mnntsmarginalgeneraldimension(cpars=as.data.frame(matrix(c(0,0,1/(2*pi)),nrow=1,
ncol=3)),M=c(0,0),R=2,marginal=1,theta=matrix(0,nrow=1,ncol=1))
```

Arguments

cpars	Matrix of parameters of an MNNTS density with the first R columns containing the index of the c parameter and the R+1 containing the complex parameter
M	Vector of M parameters. A nonnegative integer number for each of the R components of the vector
R	Number of dimensions
marginal	A subset of 1:R indicating the elements of the vector of variables in the marginal
theta	A vector of fixed values of the marginal elements of the random vector at which to obtain the value of the marginal density

Value

A scalar with the value of the marginal density at the specified value of the marginal vector.

Author(s)

Juan Jose Fernandez-Duran and Maria Mercedes Gregorio-Dominguez

References

Fernandez-Duran and J. J. and Gregorio-Dominguez and M. M (2023). Multivariate Nonnegative Trigonometric Sums Distributions f

Examples

```
# A univariate marginal from a bivariate joint

set.seed(200)
Mbiv<-c(2,3)
Rbiv<-length(Mbiv)
data(Nest)
data<-Nest
est<-mnntsmanifoldnewtonestimation(data,Mbiv,Rbiv,100)
```

```

est
marginal1value<-mnntsmarginalgenealdimension(cpars=est$cestimates,
M=Mbiv,R=Rbiv,marginal=1,theta=matrix(c(pi/2),nrow=1,ncol=1))
marginal1value

# A bivariate marginal from a trivariate joint

set.seed(200)
Mtriv<-c(2,3,3)
Rtriv<-length(Mtriv)
data(WindDirectionsTrivariate)
data<-WindDirectionsTrivariate
est<-mnntsmanifoldnewtonestimation(data,Mtriv,Rtriv,100)
est
marginal12value<-mnntsmarginalgenealdimension(cpars=est$cestimates,
M=Mtriv,R=Rtriv,marginal=c(1,2),theta=matrix(c(pi/4,pi/2),nrow=1,ncol=2))
marginal12value

```

mnntsparametersunderindependenceunivariate

Marginal Density Function at a Vector of Fixed Values

Description

Computes the vector of c parameters of an MNNTS density from the vectors of c parameters of its independent marginals

Usage

```
mnntsparametersunderindependenceunivariate(data,R,Mvector,cparlist)
```

Arguments

data	Matrix of angles in radians (with R columns)
R	Number of dimensions
Mvector	Vector of M parameters. A nonnegative integer number for each of the R components of the vector
cparlist	A list in which each element is a matrix containing the information of the vector of c parameters for each independent marginal component

Value

cestimates	Matrix of $\text{prod}(M+1)*(R+1)$. The first R columns are the parameter number, and the last column is the c parameter's estimators
loglik	Log-likelihood value
AIC	Value of Akaike's Information Criterion
BIC	Value of Bayesian Information Criterion

Author(s)

Juan Jose Fernandez-Duran and Maria Mercedes Gregorio-Dominguez

References

Fernandez-Duran and J. J. and Gregorio-Dominguez and M. M (2023). Multivariate Nonnegative Trigonometric Sums Distributions for High-Dimensional Multivariate Circular Data, arXiv preprint arXiv:2301.03643v2

Examples

```
# Bivariate MNNTS density from independent marginals

set.seed(200)
Mbiv<-c(2,3)
Rbiv<-length(Mbiv)
data(Nest)
data<-Nest*(pi/180)
est1<-nntsmanifoldnewtonestimation(data[,1],Mbiv[1])
est1
est2<-nntsmanifoldnewtonestimation(data[,2],Mbiv[2])
est2
est12independent<-mnntsparametersunderindependenceunivariate(data,R=Rbiv,
Mvector=Mbiv,cparlist=list(est1,est2))
est12independent

# Trivariate MNNTS density from independent marginals

set.seed(200)
Mtriv<-c(2,3,3)
Rtriv<-length(Mtriv)
data(WindDirectionsTrivariate)
data<-WindDirectionsTrivariate
est1<-nntsmanifoldnewtonestimation(data[,1],Mtriv[1],70)
est1
est2<-nntsmanifoldnewtonestimation(data[,2],Mtriv[2],70)
est2
est3<-nntsmanifoldnewtonestimation(data[,3],Mtriv[3],70)
est3
est123independent<-mnntsparametersunderindependenceunivariate(data,R=Rtriv,
Mvector=Mtriv,cparlist=list(est1,est2,est3))
est123independent
```

Nest

Nest orientations and creek directions

Description

Orientation of nests of 50 noisy scrub birds (theta) along the bank of a creek bed, together with the corresponding directions (phi) of creek flow at the nearest point to the nest.

Usage

```
data(Nest)
```

Format

Orientation of 50 nests (vectors)

Source

Data supplied by Dr. Graham Smith

References

N.I. Fisher (1993) Statistical analysis of circular data. Cambridge University Press.

WindDirectionsTrivariate

Wind directions

Description

Wind directions registered at the monitoring stations of San Agustin located in the north, Pedregal in the southwest, and Hangares in the southeast of the Mexico Central Valley's at 14:00 on days between January 1, 1993 and February 29, 2000. There are a total of 1,682 observations

Usage

```
data(WindDirectionsTrivariate)
```

Format

Three columns of angles in radians

Source

Mexico Central Valleys pollution monitoring network. RAMA SIMAT (Red Automatica de Monitoreo Ambiental)

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