# Package 'BART'

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<b>Description</b> Bayesian Additive Regression Trees (BART) provide flexible nonparametric modeling of covariates for continuous, binary, categorical and time-to-event outcomes. For more information see Sparapani, Spanbauer and McCulloch <doi:10.18637 jss.v097.i01="">.</doi:10.18637>
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## **Description**

To avoid duplication, the main references that this package relies upon appear here only. For more information see Sparapani, Spanbauer and McCulloch <doi:10.18637/jss.v097.i01>.

## References

Sparapani R., Spanbauer C. and McCulloch R. (2021) Nonparametric Machine Learning and Efficient Computation with Bayesian Additive Regression Trees: The BART R Package. *JSS*, **97**, 1-66. <doi:10.18637/jss.v097.i01>.

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Albert J. and Chib S. (1993) Bayesian Analysis of Binary and Polychotomous Response Data. *JASA*, **88**, 669-679. <doi:10.1080/01621459.1993.10476321>.

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abart

AFT BART for time-to-event outcomes

# **Description**

```
BART is a Bayesian "sum-of-trees" model. For a numeric response y, we have y=f(x)+\epsilon, where \epsilon\sim N(0,\sigma^2).
```

f is the sum of many tree models. The goal is to have very flexible inference for the uknown function f.

In the spirit of "ensemble models", each tree is constrained by a prior to be a weak learner so that it contributes a small amount to the overall fit.

# Usage

```
abart(
      x.train, times, delta,
      x.test=matrix(0,0,0), K=100,
      type='abart', ntype=1,
      sparse=FALSE, theta=0, omega=1,
      a=0.5, b=1, augment=FALSE, rho=NULL,
      xinfo=matrix(0,0,0), usequants=FALSE,
      rm.const=TRUE,
      sigest=NA, sigdf=3, sigquant=0.90,
      k=2, power=2, base=0.95,
      lambda=NA, tau.num=c(NA, 3, 6)[ntype],
      offset=NULL, w=rep(1, length(times)),
      ntree=c(200L, 50L, 50L)[ntype], numcut=100L,
      ndpost=1000L, nskip=100L,
      keepevery=c(1L, 10L, 10L)[ntype],
      printevery=100L, transposed=FALSE,
      mc.cores = 1L, ## mc.abart only
      nice = 19L, ## mc.abart only
      seed = 99L
                    ## mc.abart only
)
mc.abart(
         x.train, times, delta,
         x.test=matrix(0,0,0), K=100,
         type='abart', ntype=1,
         sparse=FALSE, theta=0, omega=1,
         a=0.5, b=1, augment=FALSE, rho=NULL,
         xinfo=matrix(0,0,0), usequants=FALSE,
         rm.const=TRUE,
```

```
sigest=NA, sigdf=3, sigquant=0.90,
k=2, power=2, base=0.95,

lambda=NA, tau.num=c(NA, 3, 6)[ntype],
offset=NULL, w=rep(1, length(times)),

ntree=c(200L, 50L, 50L)[ntype], numcut=100L,
ndpost=1000L, nskip=100L,
keepevery=c(1L, 10L, 10L)[ntype],
printevery=100L, transposed=FALSE,
mc.cores = 2L, nice = 19L, seed = 99L
```

#### **Arguments**

x.train Explanatory variables for training (in sample) data.

May be a matrix or a data frame, with (as usual) rows corresponding to obser-

vations and columns to variables.

If a variable is a factor in a data frame, it is replaced with dummies. Note that q dummies are created if q>2 and one dummy created if q=2 where q is the number of levels of the factor. abart will generate draws of f(x) for each x

which is a row of x. train.

times The time of event or right-censoring.

If y. train is NULL, then times (and delta) must be provided.

delta The event indicator: 1 is an event while 0 is censored.

If y.train is NULL, then delta (and times) must be provided.

x.test Explanatory variables for test (out of sample) data. Should have same structure

as x. train. abart will generate draws of f(x) for each x which is a row of

x.test.

K If provided, then coarsen times per the quantiles 1/K, 2/K, ..., K/K.

type You can use this argument to specify the type of fit. 'abart' for AFT BART.

ntype The integer equivalent of type where 'abart' is 1.

sparse Whether to perform variable selection based on a sparse Dirichlet prior rather

than simply uniform; see Linero 2016.

theta Set *theta* parameter; zero means random.

omega Set *omega* parameter; zero means random.

a Sparse parameter for Beta(a,b) prior:  $0.5 \le a \le 1$  where lower values

inducing more sparsity.

b Sparse parameter for Beta(a, b) prior; typically, b = 1.

rho Sparse parameter: typically rho = p where p is the number of covariates under

consideration.

augment Whether data augmentation is to be performed in sparse variable selection.

xinfo You can provide the cutpoints to BART or let BART choose them for you. To

provide them, use the xinfo argument to specify a list (matrix) where the items (rows) are the covariates and the contents of the items (columns) are the cut-

points.

usequants If usequants=FALSE, then the cutpoints in xinfo are generated uniformly; oth-

erwise, if TRUE, uniform quantiles are used for the cutpoints.

rm. const Whether or not to remove constant variables.

sigest The prior for the error variance  $(sigma^2)$  is inverted chi-squared (the standard

conditionally conjugate prior). The prior is specified by choosing the degrees of freedom, a rough estimate of the corresponding standard deviation and a quantile to put this rough estimate at. If sigest=NA then the rough estimate will be the usual least squares estimator. Otherwise the supplied value will be used. Not

used if y is binary.

sigdf Degrees of freedom for error variance prior. Not used if y is binary.

sigquant The quantile of the prior that the rough estimate (see sigest) is placed at. The

closer the quantile is to 1, the more aggresive the fit will be as you are putting more prior weight on error standard deviations (sigma) less than the rough es-

timate. Not used if y is binary.

k For numeric y, k is the number of prior standard deviations E(Y|x) = f(x) is away from  $\pm 1.05$ . For binary y, k is the number of prior standard deviations

away from +/-0.5. For binary y, k is the number of prior standard deviations f(x) is away from +/-3. The bigger k is, the more conservative the fitting will

be.

power Power parameter for tree prior.

base Base parameter for tree prior.

1 The scale of the prior for the variance. Not used if y is binary.

tau.num The numerator in the tau definition, i.e., tau=tau.num/(k\*sqrt(ntree)).

offset Continous BART operates on y.train centered by offset which defaults to

mean(y.train). With binary BART, the centering is P(Y=1|x)=F(f(x)+offset) where offset defaults to F^{-1}(mean(y.train)). You can use the

offset parameter to over-ride these defaults.

W Vector of weights which multiply the standard deviation. Not used if y is binary.

ntree The number of trees in the sum.

number of possible values of c (see usequants). If a single number if

given, this is used for all variables. Otherwise a vector with length equal to ncol(x.train) is required, where the  $i^{th}$  element gives the number of c used for the  $i^{th}$  variable in x.train. If usequants is false, numcut equally spaced cutoffs are used covering the range of values in the corresponding column of

 ${\tt x.train.}$  If usequants is true, then min(numcut, thenumber of unique values in the corresponding contains the correspondin

1) values are used.

ndpost The number of posterior draws returned.

nskip Number of MCMC iterations to be treated as burn in.

printevery As the MCMC runs, a message is printed every printevery draws.

keepevery Every keepevery draw is kept to be returned to the user.

transposed When running abart in parallel, it is more memory-efficient to transpose x.train

and x.test, if any, prior to calling mc.abart.

seed Setting the seed required for reproducible MCMC.

mc.cores Number of cores to employ in parallel.

nice Set the job niceness. The default niceness is 19: niceness goes from 0 (highest)

to 19 (lowest).

#### **Details**

BART is a Bayesian MCMC method. At each MCMC interation, we produce a draw from the joint posterior  $(f, \sigma)|(x, y)$  in the numeric y case and just f in the binary y case.

Thus, unlike a lot of other modelling methods in R, we do not produce a single model object from which fits and summaries may be extracted. The output consists of values  $f^*(x)$  (and  $\sigma^*$  in the numeric case) where \* denotes a particular draw. The x is either a row from the training data, x.train or the test data, x.test.

#### Value

abart returns an object of type abart which is essentially a list. In the numeric y case, the list has components:

yhat.train A matrix with ndpost rows and nrow(x.train) columns. Each row corresponds

to a draw  $f^*$  from the posterior of f and each column corresponds to a row of x.train. The (i, j) value is  $f^*(x)$  for the  $i^{th}$  kept draw of f and the  $j^{th}$  row of

x.train.

Burn-in is dropped.

yhat.test Same as yhat.train but now the x's are the rows of the test data.

yhat.train.mean

train data fits = mean of yhat.train columns.

yhat.test.mean test data fits = mean of yhat.test columns.

sigma post burn in draws of sigma, length = ndpost.

first.sigma burn-in draws of sigma.

varcount a matrix with ndpost rows and nrow(x.train) columns. Each row is for a draw.

For each variable (corresponding to the columns), the total count of the number of times that variable is used in a tree decision rule (over all trees) is given.

sigest The rough error standard deviation  $(\sigma)$  used in the prior.

#### See Also

wbart

# **Examples**

N = 1000

P = 5 #number of covariates

M = 8

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```
set.seed(12)
x.train=matrix(runif(N*P, -2, 2), N, P)
mu = x.train[, 1]^3
y=rnorm(N, mu)
offset=mean(y)
T=exp(y)
C=rexp(N, 0.05)
delta=(T<C)*1
table(delta)/N
times=(T*delta+C*(1-delta))
##test BART with token run to ensure installation works
set.seed(99)
post1 = abart(x.train, times, delta, nskip=5, ndpost=10)
## Not run:
post1 = mc.abart(x.train, times, delta,
                mc.cores=M, seed=99)
post2 = mc.abart(x.train, times, delta, offset=offset,
                 mc.cores=M, seed=99)
Z=8
plot(mu, post1$yhat.train.mean, asp=1,
     xlim=c(-Z, Z), ylim=c(-Z, Z))
abline(a=0, b=1)
plot(mu, post2$yhat.train.mean, asp=1,
     xlim=c(-Z, Z), ylim=c(-Z, Z))
abline(a=0, b=1)
plot(post1$yhat.train.mean, post2$yhat.train.mean, asp=1,
     xlim=c(-Z, Z), ylim=c(-Z, Z))
abline(a=0, b=1)
## End(Not run)
```

ACTG175

AIDS Clinical Trials Group Study 175

# **Description**

ACTG 175 was a randomized clinical trial to compare monotherapy with zidovudine or didanosine with combination therapy with zidovudine and didanosine or zidovudine and zalcitabine in adults infected with the human immunodeficiency virus type I whose CD4 T cell counts were between 200 and 500 per cubic millimeter.

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## Usage

```
data(ACTG175)
```

#### **Format**

```
A data frame with 2139 observations on the following 27 variables:
pidnum patien ID number
age age in years at baseline
wtkg weight in kg at baseline
hemo hemophilia (0=no, 1=yes)
homo homosexual activity (0=no, 1=yes)
drugs history of intravenous drug use (0=no, 1=yes)
karnof Karnofsky score (on a scale of 0-100)
oprior non-zidovudine antiretroviral therapy prior to initiation of study treatment (0=no, 1=yes)
z30 zidovudine use in the 30 days prior to treatment initiation (0=no, 1=yes)
zprior zidovudine use prior to treatment initiation (0=no, 1=yes)
preanti number of days of previously received antiretroviral therapy
race race (0=white, 1=non-white)
gender gender (0=female, 1=male)
str2 antiretroviral history (0=naive, 1=experienced)
strat antiretroviral history stratification (1='antiretroviral naive', 2='> 1 but <= 52 weeks of prior
     antiretroviral therapy', 3='> 52 weeks')
symptom symptomatic indicator (0=asymptomatic, 1=symptomatic)
treat treatment indicator (0=zidovudine only, 1=other therapies)
offtrt indicator of off-treatment before 96+/-5 weeks (0=no,1=yes)
cd40 CD4 T cell count at baseline
cd420 CD4 T cell count at 20+/-5 weeks
cd496 CD4 T cell count at 96+/-5 weeks (=NA if missing)
r missing CD4 T cell count at 96+/-5 weeks (0=missing, 1=observed)
cd80 CD8 T cell count at baseline
cd820 CD8 T cell count at 20+/-5 weeks
cens indicator of observing the event in days
days number of days until the first occurrence of: (i) a decline in CD4 T cell count of at least 50
     (ii) an event indicating progression to AIDS, or (iii) death.
arms treatment arm (0=zidovudine, 1=zidovudine and didanosine, 2=zidovudine and zalcitabine,
     3=didanosine).
```

#### **Details**

The variable days contains right-censored time-to-event observations. The data set includes the following post-randomization covariates: CD4 and CD8 T cell count at 20+/-5 weeks and the indicator of whether or not the patient was taken off-treatment before 96+/-5 weeks.

10 alligator

#### References

Hammer SM, et al. (1996) A trial comparing nucleoside monotherapy with combination therapy in HIV-infected adults with CD4 cell counts from 200 to 500 per cubic millimeter. *New England Journal of Medicine* **335**, 1081-1090.

alligator

American alligator Food Choice

# **Description**

In 1985, American alligators were harvested by hunters from August 26 to September 30 in peninsular Florida from lakes Oklawaha (Putnam County), George (Putnam and Volusia counties), Hancock (Polk County) and Trafford (Collier County). Lake, length and sex were recorded for each alligator. Stomachs from a sample of alligators 1.09-3.89m long were frozen prior to analysis. After thawing, stomach contents were removed and separated and food items were identified and tallied. Volumes were determined by water displacement. The stomach contents of 219 alligators were classified into five categories of primary food choice: Fish (the most common primary food choice), Invertebrate (snails, insects, crayfish, etc.), Reptile (turtles, alligators), Bird, and Other (amphibians, plants, household pets, stones, and other debris).

# Usage

data(alligator)

## Format

A data frame with 80 observations on the following 5 variables.

lake a factor with levels George Hancock Oklawaha Trafford sex a factor with levels female male size alligator size, a factor with levels large (>2.3m) small (<=2.3m) food primary food choice, a factor with levels bird fish invert other reptile count cell frequency, a numeric vector

#### **Details**

The table contains a fair number of 0 counts. food is the response variable. fish is the most frequent choice, and often taken as a baseline category in multinomial response models.

## Source

Agresti, A. (2002). Categorical Data Analysis, New York: Wiley, 2nd Ed., Table 7.1

#### References

Delany MF, Linda SB, Moore CT (1999). "Diet and condition of American alligators in 4 Florida lakes." In *Proceedings of the Annual Conference of the Southeastern Association of Fish and Wildlife Agencies*, **53**, 375–389.

alligator 11

## **Examples**

```
data(alligator)
## Not run:
library(nnet)
## nnet::multinom Multinomial logit model fit with neural nets
fit <- multinom(food ~ lake+size+sex, data=alligator, weights=count)</pre>
summary(fit$fitted.values)
## 1=bird, 2=fish, 3=invert, 4=other, 5=reptile
(L=length(alligator$count))
(N=sum(alligator$count))
y.train=integer(N)
x.train=matrix(nrow=N, ncol=3)
x.test=matrix(nrow=L, ncol=3)
k=1
for(i in 1:L) {
    x.test[i, ]=as.integer(
        c(alligator$lake[i], alligator$size[i], alligator$sex[i]))
    if(alligator$count[i]>0)
        for(j in 1:alligator$count[i]) {
            y.train[k]=as.integer(alligator$food[i])
            x.train[k, ]=as.integer(
                c(alligator$lake[i], alligator$size[i], alligator$sex[i]))
            k=k+1
        }
}
table(y.train)
##test mbart with token run to ensure installation works
set.seed(99)
check = mbart(x.train, y.train, nskip=1, ndpost=1)
set.seed(99)
check = mbart(x.train, y.train, nskip=1, ndpost=1)
post=mbart(x.train, y.train, x.test)
##post=mc.mbart(x.train, y.train, x.test, mc.cores=8, seed=99)
##check=predict(post, x.test, mc.cores=8)
##print(cor(post$prob.test.mean, check$prob.test.mean)^2)
par(mfrow=c(3, 2))
K=5
for(j in 1:5) {
   h=seq(j, L*K, K)
    print(cor(fit$fitted.values[ , j], post$prob.test.mean[h])^2)
    plot(fit$fitted.values[ , j], post$prob.test.mean[h],
         xlim=0:1, ylim=0:1,
         xlab=paste0('NN: Est. Prob. j=', j),
         ylab=paste0('BART: Est. Prob. j=', j))
    abline(a=0, b=1)
}
```

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```
par(mfrow=c(1, 1))
x.test=matrix(nrow=L, ncol=3)
k=1
for(size in 1:2)
    for(sex in 1:2)
        for(lake in 1:4) {
            x.test[k, ]=c(lake, size, sex)
            k=k+1
        }
x.test
## two sizes: 1=large: >2.3m, 2=small: <=2.3m
pred=predict(post, x.test)
##pred=predict(post, x.test, mc.cores=8)
ndpost=nrow(pred$prob.test)
size.test=matrix(nrow=ndpost, ncol=K*2)
for(i in 1:K) {
    j=seq(i, L*K/2, K) ## large
    size.test[ , i]=apply(pred$prob.test[ , j], 1, mean)
    j=j+L*K/2 ## small
    size.test[ , i+K]=apply(pred$prob.test[ , j], 1, mean)
}
size.test.mean=apply(size.test, 2, mean)
size.test.025=apply(size.test, 2, quantile, probs=0.025)
size.test.975=apply(size.test, 2, quantile, probs=0.975)
plot(factor(1:K, labels=c('bird', 'fish', 'invert', 'other', 'reptile')),
     rep(1, K), col=1:K, type='n', lwd=1, lty=0,
             xlim=c(1, K), ylim=c(0, 0.5), ylab='Prob.',
     sub="Multinomial BART\nFriedman's partial dependence function")
points(1:K, size.test.mean[1:K+K], col=1)
lines(1:K, size.test.025[1:K+K], col=1, lty=2)
lines(1:K, size.test.975[1:K+K], col=1, lty=2)
points(1:K, size.test.mean[1:K], col=2)
lines(1:K, size.test.025[1:K], col=2, lty=2)
lines(1:K, size.test.975[1:K], col=2, lty=2)
## legend('topright', legend=c('Small', 'Large'),
          pch=1, col=1:2)
## End(Not run)
```

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# **Description**

This data set was created from the National Health and Nutrition Examination Survey (NHANES) 2009-2010 Arthritis Questionnaire.

## Usage

data(arq)

#### **Details**

We have two outcomes of interest. Chronic neck pain: Yes arq010a=1 vs.\ No arq010a=0. Chronic lower-back/buttock pain: Yes arq010d=1 vs.\ No arq010d=0. Seqn is a unique survey respondent identifier. wtint2yr is the survey sampling weight. riagendr is gender: 1 for males, 2 for females. ridageyr is age in years. There are several anthropometric measurements: bmxwt, weight in kg; bmxht, height in cm; bmxbmi, body mass index in kg/ $m^2$ ; and bmxwaist, waist circumference in cm. The data was subsetted to ensure non-missing values of these variables.

#### References

National Health and Nutrition Examination Survey (NHANES) 2009-2010 Arthritis Questionnaire. https://wwwn.cdc.gov/nchs/nhanes/2009-2010/ARQ\_F.htm

bartModelMatrix	
Dai tiloattilati ix	

Create a matrix out of a vector or data.frame

# Description

The external BART functions operate on matrices in memory. Therefore, if the user submits a vector or data.frame, then this function converts it to a matrix. Also, it determines the number of cutpoints necessary for each column when asked to do so.

#### Usage

# **Arguments**

Χ	A vector or data.frame to create the matrix from.
numcut	The maximum number of cutpoints to consider. If numcut=0, then just return a matrix; otherwise, return a list containing a matrix X, a vector numcut and a list xinfo.
usequants	If usequants is FALSE, then the cutpoints in xinfo are generated uniformly; otherwise, if TRUE, then quantiles are used for the cutpoints.
type	Determines which quantile algorithm is employed.
rm.const	Whether or not to remove constant variables.

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cont

Whether or not to assume all variables are continuous.

xinfo

You can provide the cutpoints to BART or let BART choose them for you. To provide them, use the xinfo argument to specify a list (matrix) where the items (rows) are the covariates and the contents of the items (columns) are the cutpoints.

## See Also

```
class.ind
```

# **Examples**

```
set.seed(99)
a <- rbinom(10, 4, 0.4)
table(a)
x <- runif(10)
df <- data.frame(a=factor(a), x=x)
b <- bartModelMatrix(df)
b
b <- bartModelMatrix(df, numcut=9)
b
b <- bartModelMatrix(df, numcut=9, usequants=TRUE)
b
## Not run:
    f <- bartModelMatrix(as.character(a))
## End(Not run)</pre>
```

bladder

Bladder Cancer Recurrences

# **Description**

This interesting example is from a clinical trial conducted by the Veterans Administration Cooperative Urological Research Group. This data on recurrence of bladder cancer has been used by many to demonstrate methodology for recurrent events modelling. In this study, all patients had superficial bladder tumors when they entered the trial. These tumors were removed transurethrally and patients were randomly assigned to one of three treatments: placebo, thiotepa or pyridoxine

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(vitamin B6). Many patients had multiple recurrences of tumors during the study and new tumors were removed at each visit. For each patient, their recurrence time, if any, was measured from the beginning of treatment.

bladder is the data set that appears most commonly in the literature. It uses only the 85 subjects with nonzero follow-up who were assigned to either thiotepa or placebo and only the first four recurrences for any patient. The status variable is 1 for recurrence and 0 for everything else (including death for any reason). The data set is laid out in the competing risks format of the paper by Wei, Lin, and Weissfeld (WLW).

bladder1 is the full data set from the study. It contains all three treatment arms and all recurrences for 118 subjects; the maximum observed number of recurrences is 9.

bladder2 uses the same subset of subjects as bladder, but formated in the (start, stop] or Anderson-Gill (AG) style. Note that in transforming from the WLW to the AG style data set there is a quite common programming mistake that leads to extra follow-up time for 12 subjects: all those with follow-up beyond their fourth recurrence. Over this extended time these subjects are by definition not at risk for another event in the WLW data set.

#### **Format**

#### bladder

id: Patient id

rx: Treatment 1=placebo 2=thiotepa

number: Initial number of tumours (8=8 or more) size: size (cm) of largest initial tumour stop: recurrence or censoring time enum: which recurrence (up to 4)

#### bladder1

id: Patient id

treatment: Placebo, pyridoxine (vitamin B6), or thiotepa number: Initial number of tumours (8=8 or more) size: Size (cm) of largest initial tumour

recur: Number of recurrences

start,stop: The start and end time of each time interval status: End of interval code, 0=censored, 1=recurrence,

2=death from bladder disease, 3=death other/unknown cause

rtumor: Number of tumors found at the time of a recurrence

rsize: Size of largest tumor at a recurrence

enum: Event number (observation number within patient)

# bladder2

id: Patient id

rx: Treatment 1=placebo 2=thiotepa

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number: Initial number of tumours (8=8 or more) size: size (cm) of largest initial tumour

start: start of interval (0 or previous recurrence time)

stop: recurrence or censoring time enum: which recurrence (up to 4)

## References

Byar, DP (1980), "The Veterans Administration Study of Chemoprophylaxis for Recurrent Stage I Bladder Tumors: Comparisons of Placebo, Pyridoxine, and Topical Thiotepa," in *Bladder Tumors and Other Topics in Urological Oncology*, eds. M Pavone-Macaluso, PH Smith, and F Edsmyn, New York: Plenum, pp. 363-370.

Andrews DF, Hertzberg AM (1985), DATA: A Collection of Problems from Many Fields for the Student and Research Worker, New York: Springer-Verlag.

LJ Wei, DY Lin, L Weissfeld (1989), Regression analysis of multivariate incomplete failure time data by modeling marginal distributions. *Journal of the American Statistical Association*, **84**.

## **Examples**

data(bladder)

class.ind

Generates Class Indicator Matrix from a Factor

## **Description**

Generates a class indicator function from a given factor.

# Usage

class.ind(cl)

# **Arguments**

cl

factor or vector of classes for cases.

# Value

a matrix which is zero except for the column corresponding to the class.

#### References

Venables, W. N. and Ripley, B. D. (2002) Modern Applied Statistics with S. Fourth edition. Springer.

#### **Examples**

```
set.seed(99)
a <- rbinom(20, 4, 0.5)
table(a)
b <- class.ind(a)
str(b)
t(cbind(a, b))</pre>
```

crisk.bart

BART for competing risks

# **Description**

Here we have implemented a simple and direct approach to utilize BART for competing risks that is very flexible, and is akin to discrete-time survival analysis. Following the capabilities of BART, we allow for maximum flexibility in modeling the dependence of competing failure times on covariates. In particular, we do not impose proportional hazards.

To elaborate, consider data in the form:  $(s_i, \delta_i, x_i)$  where  $s_i$  is the event time;  $\delta_i$  is an indicator distinguishing events,  $\delta_i = h$  due to cause hin1, 2, from right-censoring,  $\delta_i = 0$ ;  $x_i$  is a vector of covariates; and i = 1, ..., N indexes subjects.

We denote the K distinct event/censoring times by  $0 < t_{(1)} < ... < t_{(K)} < \infty$  thus taking  $t_{(j)}$  to be the  $j^{th}$  order statistic among distinct observation times and, for convenience,  $t_{(0)} = 0$ . Now consider event indicators for cause h:  $y_{hij}$  for each subject i at each distinct time  $t_{(j)}$  up to and including the subject's last observation time  $s_i = t_{(n_i)}$  with  $n_i = \arg\max_j [t_{(j)} \le s_i]$  for cause 1, but only up to  $n_i - y_{1ij}$  for cause 2.

We then denote by  $p_{hij}$  the probability of an event at time  $t_{(j)}$  conditional on no previous event. We now write the model for  $y_{hij}$  as a nonparametric probit (or logistic) regression of  $y_{hij}$  on the time  $t_{(j)}$  and the covariates  $x_{hi}$ , and then utilize BART for binary responses. Specifically,  $y_{hij} = I[\delta_i = h]I[s_i = t_{(j)}], \ j = 1, ..., n_i - I[h = 2]y_{1ij}$ . Therefore, we have  $p_{hij} = F(mu_{hij}), \ mu_{hij} = mu_h + f_h(t_{(j)}, x_{hi})$  where F denotes the Normal (or Logistic) cdf. As in the binary response case,  $f_h$  is the sum of many tree models. Finally, based on these probabilities,  $p_{hij}$ , we can construct targets of inference such as the cumulative incidence functions.

## Usage

```
a=0.5, b=1, augment=FALSE,
           rho=NULL, rho2=NULL,
           xinfo=matrix(0,0,0), xinfo2=matrix(0,0,0),
           usequants=FALSE,
           rm.const=TRUE, type='pbart',
           ntype=as.integer(
               factor(type, levels=c('wbart', 'pbart', 'lbart'))),
           k=2, power=2, base=0.95,
           offset=NULL, offset2=NULL,
           tau.num=c(NA, 3, 6)[ntype],
           ntree=50, numcut=100, ndpost=1000, nskip=250,
           keepevery = 10L,
           printevery=100L,
           id=NULL,
                      ## crisk.bart only
           seed=99, ## mc.crisk.bart only
           mc.cores=2, ## mc.crisk.bart only
           nice=19L ## mc.crisk.bart only
          )
mc.crisk.bart(x.train=matrix(0,0,0), y.train=NULL,
              x.train2=x.train, y.train2=NULL,
              times=NULL, delta=NULL, K=NULL,
              x.test=matrix(0,0,0), x.test2=x.test, cond=NULL,
              sparse=FALSE, theta=0, omega=1,
              a=0.5, b=1, augment=FALSE,
              rho=NULL, rho2=NULL,
              xinfo=matrix(0,0,0), xinfo2=matrix(0,0,0),
              usequants=FALSE,
              rm.const=TRUE, type='pbart',
              ntype=as.integer(
                  factor(type, levels=c('wbart', 'pbart', 'lbart'))),
              k=2, power=2, base=0.95,
              offset=NULL, offset2=NULL,
              tau.num=c(NA, 3, 6)[ntype],
              ntree=50, numcut=100, ndpost=1000, nskip=250,
              keepevery = 10L,
              printevery=100L,
              id=NULL, ## crisk.bart only
```

```
seed=99, ## mc.crisk.bart only
mc.cores=2, ## mc.crisk.bart only
nice=19L ## mc.crisk.bart only
)
```

#### Arguments

x. train Covariates for training (in sample) data of cause 1.

Must be a data frame or a matrix with rows corresponding to observations and columns to variables.

crisk.bart will generate draws of  $f_1(t, x)$  for each x which is a row of x. train (note that the definition of x. train is dependent on whether y. train has been specified; see below).

y.train Cause 1 binary response for training (in sample) data.

If y.train is NULL, then y.train (x.train and x.test, if specified) are generated by a call to crisk.pre.bart (which require that times and delta be provided: see below); otherwise, y.train (x.train and x.test, if specified) are utilized as given assuming that the data construction has already been performed.

x.train2 Covariates for training (in sample) data of cause 2. Similar to x.train above.

y.train2 Cause 2 binary response for training (in sample) data, i.e., failure from any cause

besides the cause of interest which is cause 1. Similar to y. train above.

times The time of event or right-censoring,  $s_i$ .

If y. train is NULL, then times (and delta) must be provided.

delta The event indicator: 1 for cause 1, 2 for cause 2 and 0 is censored.

If y. train is NULL, then delta (and times) must be provided.

K If provided, then coarsen times per the quantiles 1/K, 2/K, ..., K/K.

x.test Covariates for test (out of sample) data of cause 1.

Must be a data.frame or a matrix and have the same structure as x.train. crisk.bart will generate draws of  $f_1(t,x)$  for each x which is a row of x.test.

x.test2 Covariates for test (out of sample) data of cause 2. Similar to x.test above.

cond A vector of indices for y. train2 indicating subjects who did not suffer a cause

1 event and, therefore, are eligible for cause 2.

sparse Whether to perform variable selection based on a sparse Dirichlet prior; see

Linero 2016.

theta Set *theta* parameter; zero means random.

omega Set *omega* parameter; zero means random.

a Sparse parameter for Beta(a,b) prior:  $0.5 \le a \le 1$  where lower values

inducing more sparsity.

b Sparse parameter for Beta(a, b) prior; typically, b=1.

rho Sparse parameter: typically rho=p where p is the number of covariates in x. train.

rho2 Sparse parameter: typically rho2=p where p is the number of covariates in

x.train2.

augment Whether data augmentation is to be performed in sparse variable selection.

xinfo You can provide the cutpoints to BART or let BART choose them for you. To

provide them, use the xinfo argument to specify a list (matrix) where the items (rows) are the covariates and the contents of the items (columns) are the cut-

points.

xinfo2 Cause 2 cutpoints.

usequants If usequants=FALSE, then the cutpoints in xinfo are generated uniformly; oth-

erwise, if TRUE, uniform quantiles are used for the cutpoints.

rm.const Whether or not to remove constant variables.

type Whether to employ probit BART via Albert-Chib, 'pbart', or logistic BART

by Holmes-Held, 'lbart'.

ntype The integer equivalent of type where 'wbart' is 1, 'pbart' is 2 and 'lbart'

is 3.

k k is the number of prior standard deviations  $f_h(t,x)$  is away from +/-3. The

bigger k is, the more conservative the fitting will be.

power Power parameter for tree prior.

base Base parameter for tree prior.

offset Cause 1 binary offset.
offset2 Cause 2 binary offset.

tau.num The numerator in the tau definition.

ntree The number of trees in the sum.

numcut The number of possible values of cutpoints (see usequants). If a single num-

ber if given, this is used for all variables. Otherwise a vector with length equal to ncol(x.train) is required, where the  $i^{th}$  element gives the number of cutpoints used for the  $i^{th}$  variable in x.train. If usequants is FALSE, numcut equally spaced cutoffs are used covering the range of values in the corresponding column of x.train. If usequants is TRUE, then min(numcut, the number of unique values in the corresponding columns of x.train - 1) cutpoint values.

ues are used.

ndpost The number of posterior draws returned.

nskip Number of MCMC iterations to be treated as burn in. keepevery Every keepevery draw is kept to be returned to the user.

printevery As the MCMC runs, a message is printed every printevery draws.

id crisk.bart only: unique identifier added to returned list.

seed mc.crisk.bart only: seed required for reproducible MCMC.
mc.cores mc.crisk.bart only: number of cores to employ in parallel.

nice mc.crisk.bart only: set the job niceness. The default niceness is 19: niceness

goes from 0 (highest priority) to 19 (lowest priority).

#### Value

crisk.bart returns an object of type criskbart which is essentially a list. Besides the items listed below, the list has offset, offset2, times which are the unique times, K which is the number of unique times, tx.train and tx.test, if any.

```
yhat.train
                   A matrix with ndpost rows and nrow(x.train) columns. Each row corre-
                   sponds to a draw f_1^* from the posterior of f_1 and each column corresponds to a
                   row of x. train. The (i,j) value is f_1^*(t,x) for the i^{th} kept draw of f_1 and the
                  j^{th} row of x. train. Burn-in is dropped.
                   Same as yhat. train but now the x's are the rows of the test data.
yhat.test
                   test data fits for the survival function, S(t, x).
surv.test
                  mean of surv. test over the posterior samples.
surv.test.mean
prob.test
                  The probability of suffering cause 1.
prob.test2
                  The probability of suffering cause 2.
cif.test
                  The cumulative incidence function of cause 1, F_1(t, x).
cif.test2
                  The cumulative incidence function of cause 2, F_2(t, x).
cif.test.mean
                  mean of cif. test columns for cause 1.
cif.test2.mean mean of cif.test2 columns for cause 2.
varcount
                  a matrix with ndpost rows and nrow(x.train) columns. Each row is for a
                  draw. For each variable (corresponding to the columns), the total count of the
                  number of times this variable is used for cause 1 in a tree decision rule (over all
                   trees) is given.
varcount2
                  For each variable the total count of the number of times this variable is used for
                   cause 2 in a tree decision rule is given.
```

#### See Also

```
crisk.pre.bart, predict.criskbart, mc.crisk.pwbart, crisk2.bart
```

# **Examples**

```
data(transplant)
pfit <- survfit(Surv(futime, event) ~ abo, transplant)</pre>
# competing risks for type 0
plot(pfit[4,], xscale=7, xmax=735, col=1:3, lwd=2, ylim=c(0, 1),
       xlab='t (weeks)', ylab='Aalen-Johansen (AJ) CI(t)')
    legend(450, .4, c("Death", "Transplant", "Withdrawal"), col=1:3, lwd=2)
## plot(pfit[4,], xscale=30.5, xmax=735, col=1:3, lwd=2, ylim=c(0, 1),
          xlab='t (months)', ylab='Aalen-Johansen (AJ) CI(t)')
       legend(450, .4, c("Death", "Transplant", "Withdrawal"), col=1:3, lwd=2)
##
delta <- (as.numeric(transplant$event)-1)</pre>
## recode so that delta=1 is cause of interest; delta=2 otherwise
delta[delta==1] <- 4
delta[delta==2] <- 1
delta[delta>1] <- 2
table(delta, transplant$event)
times <- pmax(1, ceiling(transplant$futime/7)) ## weeks</pre>
##times <- pmax(1, ceiling(transplant$futime/30.5)) ## months
```

```
table(times)
type0 <- 1*(transplant$abo=='0')</pre>
typeA <- 1*(transplant$abo=='A')</pre>
typeB <- 1*(transplant$abo=='B')</pre>
typeAB <- 1*(transplant$abo=='AB')</pre>
table(typeA, type0)
x.train <- cbind(type0, typeA, typeB, typeAB)</pre>
x.test <- cbind(1, 0, 0, 0)
dimnames(x.test)[[2]] <- dimnames(x.train)[[2]]</pre>
##test BART with token run to ensure installation works
set.seed(99)
post <- crisk.bart(x.train=x.train, times=times, delta=delta,</pre>
                   x.test=x.test, nskip=1, ndpost=1, keepevery=1)
## Not run:
## run one long MCMC chain in one process
## set.seed(99)
## post <- crisk.bart(x.train=x.train, times=times, delta=delta, x.test=x.test)</pre>
## in the interest of time, consider speeding it up by parallel processing
## run "mc.cores" number of shorter MCMC chains in parallel processes
post <- mc.crisk.bart(x.train=x.train, times=times, delta=delta,</pre>
                       x.test=x.test, seed=99, mc.cores=8)
K <- post$K
typeO.cif.mean <- apply(post$cif.test, 2, mean)</pre>
type0.cif.025 <- apply(post$cif.test, 2, quantile, probs=0.025)</pre>
typeO.cif.975 <- apply(post$cif.test, 2, quantile, probs=0.975)</pre>
plot(pfit[4,], xscale=7, xmax=735, col=1:3, lwd=2, ylim=c(0, 0.8),
       xlab='t (weeks)', ylab='CI(t)')
points(c(0, post\$times)*7, c(0, type0.cif.mean), col=4, type='s', lwd=2)
points(c(0, post\$times)*7, c(0, type0.cif.025), col=4, type='s', lwd=2, lty=2)
points(c(0, post\$times)*7, c(0, type0.cif.975), col=4, type='s', lwd=2, lty=2)
     legend(450, .4, c("Transplant(BART)", "Transplant(AJ)",
                        "Death(AJ)", "Withdrawal(AJ)"),
            col=c(4, 2, 1, 3), lwd=2)
##dev.copy2pdf(file='../vignettes/figures/liver-BART.pdf')
## plot(pfit[4,], xscale=30.5, xmax=735, col=1:3, lwd=2, ylim=c(0, 0.8),
          xlab='t (months)', ylab='CI(t)')
## points(c(0, post$times)*30.5, c(0, type0.cif.mean), col=4, type='s', lwd=2)
## points(c(0, post$times)*30.5, c(0, typeO.cif.025), col=4, type='s', lwd=2, lty=2)
## points(c(0, post$times)*30.5, c(0, type0.cif.975), col=4, type='s', lwd=2, lty=2)
        legend(450, .4, c("Transplant(BART)", "Transplant(AJ)",
##
                           "Death(AJ)", "Withdrawal(AJ)"),
##
               col=c(4, 2, 1, 3), lwd=2)
##
```

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## End(Not run)

crisk.pre.bart

Data construction for competing risks with BART

# **Description**

Competing risks contained in  $(t, \delta, x)$  must be translated to data suitable for the BART competing risks model; see crisk.bart for more details.

# Usage

```
\label{eq:crisk.pre.bart(times, delta, x.train=NULL, x.test=NULL, x.train2=x.train, x.test2=x.test, K=NULL)}
```

# **Arguments**

times	The time of event or right-censoring.
delta	The event indicator: 1 is a cause 1 event, 2 a cause 2 while 0 is censored.
x.train	Explanatory variables for training (in sample) data of cause 1. If provided, must be a matrix with (as usual) rows corresponding to observations and columns to variables.
x.test	Explanatory variables for test (out of sample) data of cause 1. If provided, must be a matrix and have the same structure as x.train.
x.train2	Explanatory variables for training (in sample) data of cause 2. If provided, must be a matrix with (as usual) rows corresponding to observations and columns to variables.
x.test2	Explanatory variables for test (out of sample) data of cause 2. If provided, must be a matrix and have the same structure as x.train.
K	If provided, then coarsen times per the quantiles $1/K, 2/K,, K/K$ .

# Value

surv.pre.bart returns a list. Besides the items listed below, the list has a times component giving the unique times and K which is the number of unique times.

y.train	A vector of binary responses for cause 1.
v.train2	A vector of binary responses for cause 2.

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cond	A vector of indices of y. train indicating censored subjects.
binaryOffset	The binary offset for y.train.
binaryOffset2	The binary offset for y.train2.
tx.train	A matrix with rows consisting of time and the covariates of the training data for cause 1.
tx.train2	A matrix with rows consisting of time and the covariates of the training data for cause 2.
tx.test	A matrix with rows consisting of time and the covariates of the test data, if any, for cause 1.
tx.test2	A matrix with rows consisting of time and the covariates of the test data, if any, for cause 2.

#### See Also

```
crisk.bart
```

# **Examples**

```
data(transplant)
delta <- (as.numeric(transplant$event)-1)</pre>
delta[delta==1] <- 4
delta[delta==2] <- 1
delta[delta>1] <- 2</pre>
table(delta, transplant$event)
table(1+floor(transplant$futime/30.5)) ## months
times <- 1+floor(transplant$futime/30.5)</pre>
type0 <- 1*(transplant$abo=='0')</pre>
typeA <- 1*(transplant$abo=='A')</pre>
typeB <- 1*(transplant$abo=='B')</pre>
typeAB <- 1*(transplant$abo=='AB')</pre>
table(typeA, type0)
x.train <- cbind(type0, typeA, typeB, typeAB)</pre>
N <- nrow(x.train)
x.test <- x.train
 \texttt{x.test[1:N, 1:4]} \leftarrow \texttt{matrix(c(1, 0, 0, 0), nrow=N, ncol=4, byrow=TRUE)} 
pre <- crisk.pre.bart(x.train=x.train, times=times, delta=delta, x.test=x.test)</pre>
```

crisk2.bart

BART for competing risks

## Description

Here we have implemented another approach to utilize BART for competing risks that is very flexible, and is akin to discrete-time survival analysis. Following the capabilities of BART, we allow for maximum flexibility in modeling the dependence of competing failure times on covariates. In particular, we do not impose proportional hazards.

Similar to crisk.bart, we utilize two BART models, yet they are two different BART models than previously considered. First, given an event of either cause occurred, we employ a typical binary BART model to discriminate between cause 1 and 2. Next, we proceed as if it were a typical survival analysis with BART for an absorbing event from either cause.

To elaborate, consider data in the form:  $(s_i, \delta_i, x_i)$  where  $s_i$  is the event time;  $\delta_i$  is an indicator distinguishing events,  $\delta_i = h$  due to cause hin1, 2, from right-censoring,  $\delta_i = 0$ ;  $x_i$  is a vector of covariates; and i = 1, ..., N indexes subjects. We denote the K distinct event/censoring times by  $0 < t_{(1)} < ... < t_{(K)} < \infty$  thus taking  $t_{(j)}$  to be the  $j^{th}$  order statistic among distinct observation times and, for convenience,  $t_{(0)} = 0$ .

First, consider event indicators for an event from either cause:  $y_{1ij}$  for each subject i at each distinct time  $t_{(j)}$  up to and including the subject's last observation time  $s_i=t_{(n_i)}$  with  $n_i=\arg\max_j[t_{(j)}\leq s_i]$ . We denote by  $p_{1ij}$  the probability of an event at time  $t_{(j)}$  conditional on no previous event. We now write the model for  $y_{1ij}$  as a nonparametric probit (or logistic) regression of  $y_{1ij}$  on the time  $t_{(j)}$  and the covariates  $x_{1i}$ , and then utilize BART for binary responses. Specifically,  $y_{1ij}=I[\delta_i>0]I[s_i=t_{(j)}],\ j=1,...,n_i$ . Therefore, we have  $p_{1ij}=F(mu_{1ij}),\ mu_{1ij}=mu_1+f_1(t_{(j)},x_{1i})$  where F denotes the Normal (or Logistic) cdf.

Next, we denote by  $p_{2i}$  the probability of a cause 1 event at time  $s_i$  conditional on an event having occurred. We now write the model for  $y_{2i}$  as a nonparametric probit (or logistic) regression of  $y_{2i}$  on the time  $s_i$  and the covariates  $x_{2i}$ , via BART for binary responses. Specifically,  $y_{2i} = I[\delta_i = 1]$ . Therefore, we have  $p_{2i} = F(mu_{2i})$ ,  $mu_{2i} = mu_2 + f_2(s_i, x_{2i})$  where F denotes the Normal (or Logistic) cdf. Although, we modeled  $p_{2i}$  at the time of an event,  $s_i$ , we can estimate this probability at any other time points on the grid via  $p(t_{(j)}, x_2) = F(mu_2 + f_2(t_{(j)}, x_2))$ . Finally, based on these probabilities,  $p_{hij}$ , we can construct targets of inference such as the cumulative incidence functions.

## Usage

```
ntype=as.integer(
               factor(type, levels=c('wbart', 'pbart', 'lbart'))),
           k=2, power=2, base=0.95,
           offset=NULL, offset2=NULL,
           tau.num=c(NA, 3, 6)[ntype],
           ntree=50, numcut=100, ndpost=1000, nskip=250,
           keepevery = 10L,
           printevery=100L,
           id=NULL, ## crisk2.bart only
           seed=99,
                     ## mc.crisk2.bart only
          mc.cores=2, ## mc.crisk2.bart only
           nice=19L ## mc.crisk2.bart only
          )
mc.crisk2.bart(x.train=matrix(0,0,0), y.train=NULL,
              x.train2=x.train, y.train2=NULL,
              times=NULL, delta=NULL, K=NULL,
              x.test=matrix(0,0,0), x.test2=x.test,
              sparse=FALSE, theta=0, omega=1,
              a=0.5, b=1, augment=FALSE,
              rho=NULL, rho2=NULL,
              xinfo=matrix(0,0,0), xinfo2=matrix(0,0,0),
              usequants=FALSE,
              rm.const=TRUE, type='pbart',
              ntype=as.integer(
                  factor(type, levels=c('wbart', 'pbart', 'lbart'))),
              k=2, power=2, base=0.95,
              offset=NULL, offset2=NULL,
              tau.num=c(NA, 3, 6)[ntype],
              ntree=50, numcut=100, ndpost=1000, nskip=250,
              keepevery = 10L,
              printevery=100L,
              id=NULL,
                         ## crisk2.bart only
              seed=99,
                        ## mc.crisk2.bart only
              mc.cores=2, ## mc.crisk2.bart only
              nice=19L ## mc.crisk2.bart only
             )
```

#### **Arguments**

xinfo

points.

x.train Covariates for training (in sample) data for an event. Must be a data frame or a matrix with rows corresponding to observations and columns to variables. crisk2.bart will generate draws of  $f_1(t,x)$  for each x which is a row of x.train (note that the definition of x.train is dependent on whether y.train has been specified; see below). Event binary response for training (in sample) data. y.train If y. train is NULL, then y. train (x. train and x. test, if specified) are generated by a call to surv.pre.bart (which require that times and delta be provided: see below); otherwise, y.train (x.train and x.test, if specified) are utilized as given assuming that the data construction has already been performed. x.train2 Covariates for training (in sample) data of for a cause 1 event. Similar to x.train above. y.train2 Cause 1 event binary response for training (in sample) data. Similar to y. train above. times The time of event or right-censoring,  $s_i$ . If y. train is NULL, then times (and delta) must be provided. delta The event indicator: 1 for cause 1, 2 for cause 2 and 0 is censored. If y. train is NULL, then delta (and times) must be provided. K If provided, then coarsen times per the quantiles 1/K, 2/K, ..., K/K. x.test Covariates for test (out of sample) data of an event. Must be a data.frame or a matrix and have the same structure as x. train. crisk2.bart will generate draws of  $f_1(t,x)$  for each x which is a row of x.test. x.test2 Covariates for test (out of sample) data of a cause 1 event. Similar to x.test Whether to perform variable selection based on a sparse Dirichlet prior; see sparse Linero 2016. theta Set *theta* parameter; zero means random. Set *omega* parameter; zero means random. omega Sparse parameter for Beta(a,b) prior: 0.5 <= a <= 1 where lower values а inducing more sparsity. b Sparse parameter for Beta(a, b) prior; typically, b=1. Sparse parameter: typically rho=p where p is the number of covariates in x. train. rho rho2 Sparse parameter: typically rho2=p where p is the number of covariates in x.train2. augment Whether data augmentation is to be performed in sparse variable selection.

You can provide the cutpoints to BART or let BART choose them for you. To provide them, use the xinfo argument to specify a list (matrix) where the items (rows) are the covariates and the contents of the items (columns) are the cut-

xinfo2 Cause 2 cutpoints.

usequants If usequants=FALSE, then the cutpoints in xinfo are generated uniformly; oth-

erwise, if TRUE, uniform quantiles are used for the cutpoints.

rm. const Whether or not to remove constant variables.

type Whether to employ probit BART via Albert-Chib, 'pbart', or logistic BART

by Holmes-Held, 'lbart'.

ntype The integer equivalent of type where 'wbart' is 1, 'pbart' is 2 and 'lbart'

is 3.

k is the number of prior standard deviations  $f_h(t,x)$  is away from +/-3. The

bigger k is, the more conservative the fitting will be.

power Power parameter for tree prior.

Base parameter for tree prior.

offset Cause 1 binary offset.
offset2 Cause 2 binary offset.

tau.num The numerator in the tau definition.

ntree The number of trees in the sum.

numcut The number of possible values of cutpoints (see usequants). If a single num-

ber if given, this is used for all variables. Otherwise a vector with length equal to ncol(x.train) is required, where the  $i^{th}$  element gives the number of cutpoints used for the  $i^{th}$  variable in x.train. If usequants is FALSE, numcut equally spaced cutoffs are used covering the range of values in the corresponding column of x.train. If usequants is TRUE, then min(numcut, the number of unique values in the corresponding columns of x.train - 1) cutpoint values.

ues are used.

ndpost The number of posterior draws returned.

nskip Number of MCMC iterations to be treated as burn in.

keepevery Every keepevery draw is kept to be returned to the user.

printevery As the MCMC runs, a message is printed every printevery draws.

id crisk2.bart only: unique identifier added to returned list.seed mc.crisk2.bart only: seed required for reproducible MCMC.mc.crisk2.bart only: number of cores to employ in parallel.

nice mc.crisk2.bart only: set the job niceness. The default niceness is 19: niceness

goes from 0 (highest priority) to 19 (lowest priority).

## Value

crisk2.bart returns an object of type crisk2bart which is essentially a list. Besides the items listed below, the list has offset, offset2, times which are the unique times, K which is the number of unique times, tx.train and tx.test, if any.

yhat.train A matrix with ndpost rows and nrow(x.train) columns. Each row corre-

sponds to a draw  $f_1^*$  from the posterior of  $f_1$  and each column corresponds to a row of x.train. The (i,j) value is  $f_1^*(t,x)$  for the  $i^{th}$  kept draw of  $f_1$  and the

 $j^{th}$  row of x. train. Burn-in is dropped.

yhat.test Same as yhat. train but now the x's are the rows of the test data. surv.test test data fits for the survival function, S(t, x). mean of surv. test over the posterior samples. surv.test.mean prob.test The probability of suffering an event. prob.test2 The probability of suffering a cause 1 event. cif.test The cumulative incidence function of cause 1,  $F_1(t, x)$ . cif.test2 The cumulative incidence function of cause 2,  $F_2(t, x)$ . cif.test.mean mean of cif. test columns for cause 1. cif.test2.mean mean of cif.test2 columns for cause 2. a matrix with ndpost rows and nrow(x.train) columns. Each row is for a varcount draw. For each variable (corresponding to the columns), the total count of the number of times this variable is used for an event in a tree decision rule (over all trees) is given. varcount2 For each variable the total count of the number of times this variable is used for a cause 1 event in a tree decision rule is given.

#### See Also

```
surv.pre.bart, predict.crisk2bart, mc.crisk2.pwbart, crisk.bart
```

## **Examples**

```
data(transplant)
pfit <- survfit(Surv(futime, event) ~ abo, transplant)</pre>
# competing risks for type 0
plot(pfit[4,], xscale=7, xmax=735, col=1:3, lwd=2, ylim=c(0, 1),
       xlab='t (weeks)', ylab='Aalen-Johansen (AJ) CI(t)')
    legend(450, .4, c("Death", "Transplant", "Withdrawal"), col=1:3, lwd=2)
## plot(pfit[4,], xscale=30.5, xmax=735, col=1:3, lwd=2, ylim=c(0, 1),
##
          xlab='t (months)', ylab='Aalen-Johansen (AJ) CI(t)')
##
       legend(450, .4, c("Death", "Transplant", "Withdrawal"), col=1:3, lwd=2)
delta <- (as.numeric(transplant$event)-1)</pre>
## recode so that delta=1 is cause of interest; delta=2 otherwise
delta[delta==1] <- 4
delta[delta==2] <- 1
delta[delta>1] <- 2</pre>
table(delta, transplant$event)
times <- pmax(1, ceiling(transplant$futime/7)) ## weeks
##times <- pmax(1, ceiling(transplant$futime/30.5)) ## months
table(times)
type0 <- 1*(transplant$abo=='0')</pre>
typeA <- 1*(transplant$abo=='A')</pre>
typeB <- 1*(transplant$abo=='B')
```

```
typeAB <- 1*(transplant$abo=='AB')</pre>
table(typeA, type0)
x.train <- cbind(type0, typeA, typeB, typeAB)</pre>
x.test <- cbind(1, 0, 0, 0)
dimnames(x.test)[[2]] <- dimnames(x.train)[[2]]</pre>
##test BART with token run to ensure installation works
set.seed(99)
post <- crisk2.bart(x.train=x.train, times=times, delta=delta,</pre>
                   x.test=x.test, nskip=1, ndpost=1, keepevery=1)
## Not run:
## run one long MCMC chain in one process
## set.seed(99)
## post <- crisk2.bart(x.train=x.train, times=times, delta=delta, x.test=x.test)</pre>
## in the interest of time, consider speeding it up by parallel processing
## run "mc.cores" number of shorter MCMC chains in parallel processes
post <- mc.crisk2.bart(x.train=x.train, times=times, delta=delta,</pre>
                      x.test=x.test, seed=99, mc.cores=8)
K <- post$K
typeO.cif.mean <- apply(post$cif.test, 2, mean)</pre>
typeO.cif.025 <- apply(post$cif.test, 2, quantile, probs=0.025)</pre>
typeO.cif.975 <- apply(post$cif.test, 2, quantile, probs=0.975)</pre>
plot(pfit[4,], xscale=7, xmax=735, col=1:3, lwd=2, ylim=c(0, 0.8),
       xlab='t (weeks)', ylab='CI(t)')
points(c(0, post$times)*7, c(0, type0.cif.mean), col=4, type='s', lwd=2)
points(c(0, post$times)*7, c(0, type0.cif.025), col=4, type='s', lwd=2, lty=2)
points(c(0, post\$times)*7, c(0, type0.cif.975), col=4, type='s', lwd=2, lty=2)
     legend(450, .4, c("Transplant(BART)", "Transplant(AJ)",
                        "Death(AJ)", "Withdrawal(AJ)"),
            col=c(4, 2, 1, 3), lwd=2)
##dev.copy2pdf(file='../vignettes/figures/liver-BART.pdf')
## plot(pfit[4,], xscale=30.5, xmax=735, col=1:3, lwd=2, ylim=c(0, 0.8),
          xlab='t (months)', ylab='CI(t)')
## points(c(0, post$times)*30.5, c(0, type0.cif.mean), col=4, type='s', lwd=2)
## points(c(0, post$times)*30.5, c(0, type0.cif.025), col=4, type='s', lwd=2, lty=2)
## points(c(0, post$times)*30.5, c(0, type0.cif.975), col=4, type='s', lwd=2, lty=2)
##
        legend(450, .4, c("Transplant(BART)", "Transplant(AJ)",
                           "Death(AJ)", "Withdrawal(AJ)"),
##
##
               col=c(4, 2, 1, 3), lwd=2)
```

## End(Not run)

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Testing truncated Normal sampling

# **Description**

Truncated Normal latents with non-unit variance are necessary for logistic BART.

# Usage

```
draw_lambda_i(lambda, mean, kmax=1000, thin=1)
```

# **Arguments**

lambda Previous value of lambda.mean Mean of truncated Normal.

kmax The number of terms in the mixture.

thin The thinning parameter.

#### Value

Returns the variance for a truncated Normal, i.e., N(mean, lambda)I(tau, infinity).

# See Also

```
rtnorm, lbart
```

## **Examples**

```
set.seed(12)
draw_lambda_i(1, 2)
rtnorm(1, 2, sqrt(6.773462), 6)
draw_lambda_i(6.773462, 2)
```

gbart

Generalized BART for continuous and binary outcomes

# Description

```
BART is a Bayesian "sum-of-trees" model. For a numeric response y, we have y=f(x)+\epsilon, where \epsilon \sim N(0,\sigma^2).
```

f is the sum of many tree models. The goal is to have very flexible inference for the uknown function f.

In the spirit of "ensemble models", each tree is constrained by a prior to be a weak learner so that it contributes a small amount to the overall fit.

# Usage

```
gbart(
      x.train, y.train,
      x.test=matrix(0,0,0), type='wbart',
      ntype=as.integer(
          factor(type, levels=c('wbart', 'pbart', 'lbart'))),
      sparse=FALSE, theta=0, omega=1,
      a=0.5, b=1, augment=FALSE, rho=NULL,
      xinfo=matrix(0,0,0), usequants=FALSE,
      rm.const=TRUE,
      sigest=NA, sigdf=3, sigquant=0.90,
      k=2, power=2, base=0.95,
      lambda=NA, tau.num=c(NA, 3, 6)[ntype],
      offset=NULL, w=rep(1, length(y.train)),
      ntree=c(200L, 50L, 50L)[ntype], numcut=100L,
      ndpost=1000L, nskip=100L,
      keepevery=c(1L, 10L, 10L)[ntype],
      printevery=100L, transposed=FALSE,
      hostname=FALSE,
      mc.cores = 1L, ## mc.gbart only
      nice = 19L,
                   ## mc.gbart only
      seed = 99L
                    ## mc.gbart only
)
mc.gbart(
         x.train, y.train,
        x.test=matrix(0,0,0), type='wbart',
         ntype=as.integer(
             factor(type, levels=c('wbart', 'pbart', 'lbart'))),
         sparse=FALSE, theta=0, omega=1,
         a=0.5, b=1, augment=FALSE, rho=NULL,
         xinfo=matrix(0,0,0), usequants=FALSE,
         rm.const=TRUE,
         sigest=NA, sigdf=3, sigquant=0.90,
         k=2, power=2, base=0.95,
         lambda=NA, tau.num=c(NA, 3, 6)[ntype],
         offset=NULL, w=rep(1, length(y.train)),
         ntree=c(200L, 50L, 50L)[ntype], numcut=100L,
         ndpost=1000L, nskip=100L,
         keepevery=c(1L, 10L, 10L)[ntype],
         printevery=100L, transposed=FALSE,
         hostname=FALSE,
         mc.cores = 2L, nice = 19L, seed = 99L
)
```

# **Arguments**

x.train Explanatory variables for training (in sample) data.

May be a matrix or a data frame, with (as usual) rows corresponding to obser-

vations and columns to variables.

If a variable is a factor in a data frame, it is replaced with dummies. Note that q dummies are created if q>2 and one dummy created if q=2 where q is the number of levels of the factor. gbart will generate draws of f(x) for each x

which is a row of x. train.

y.train Continuous or binary dependent variable for training (in sample) data.

If y is numeric, then a continuous BART model is fit (Normal errors).

If y is binary (has only 0's and 1's), then a binary BART model with a probit link is fit by default: you can over-ride the default via the argument type to specify

a logit BART model.

x.test Explanatory variables for test (out of sample) data. Should have same structure

as x.train. gbart will generate draws of f(x) for each x which is a row of

x.test.

type You can use this argument to specify the type of fit. 'wbart' for continuous

BART, 'pbart' for probit BART or 'lbart' for logit BART.

ntype The integer equivalent of type where 'wbart' is 1, 'pbart' is 2 and 'lbart'

is 3.

sparse Whether to perform variable selection based on a sparse Dirichlet prior rather

than simply uniform; see Linero 2016.

theta Set *theta* parameter; zero means random.

omega Set *omega* parameter; zero means random.

a Sparse parameter for Beta(a,b) prior: 0.5 <= a <= 1 where lower values

inducing more sparsity.

b Sparse parameter for Beta(a, b) prior; typically, b = 1.

rho Sparse parameter: typically rho = p where p is the number of covariates under

consideration.

augment Whether data augmentation is to be performed in sparse variable selection.

xinfo You can provide the cutpoints to BART or let BART choose them for you. To

provide them, use the xinfo argument to specify a list (matrix) where the items (rows) are the covariates and the contents of the items (columns) are the cut-

points.

usequants If usequants=FALSE, then the cutpoints in xinfo are generated uniformly; oth-

erwise, if TRUE, uniform quantiles are used for the cutpoints.

rm.const Whether or not to remove constant variables.

sigest The prior for the error variance  $(sigma^2)$  is inverted chi-squared (the standard

conditionally conjugate prior). The prior is specified by choosing the degrees of freedom, a rough estimate of the corresponding standard deviation and a quantile to put this rough estimate at. If sigest=NA then the rough estimate will be the usual least squares estimator. Otherwise the supplied value will be used. Not

used if y is binary.

sigdf Degrees of freedom for error variance prior. Not used if y is binary.

sigguant The quantile of the prior that the rough estimate (see sigest) is placed at. The

closer the quantile is to 1, the more aggresive the fit will be as you are putting more prior weight on error standard deviations (sigma) less than the rough es-

timate. Not used if y is binary.

k For numeric y, k is the number of prior standard deviations E(Y|x) = f(x) is

away from +/-0.5. For binary y, k is the number of prior standard deviations f(x) is away from +/-3. The bigger k is, the more conservative the fitting will

be.

power Power parameter for tree prior.

Base parameter for tree prior.

lambda The scale of the prior for the variance. If lambda is zero, then the variance is to

be considered fixed and known at the given value of sigest. Not used if y is

binary.

tau.num The numerator in the tau definition, i.e., tau=tau.num/(k\*sqrt(ntree)).

offset Continuous BART operates on y.train centered by offset which defaults to

mean(y.train). With binary BART, the centering is P(Y=1|x)=F(f(x)+offset) where offset defaults to F^{-1}(mean(y.train)). You can use the

offset parameter to over-ride these defaults.

We Vector of weights which multiply the standard deviation. Not used if y is binary.

ntree The number of trees in the sum.

number of possible values of c (see usequants). If a single number if

given, this is used for all variables. Otherwise a vector with length equal to ncol(x.train) is required, where the  $i^{th}$  element gives the number of c used for the  $i^{th}$  variable in x.train. If usequants is false, numcut equally spaced cutoffs are used covering the range of values in the corresponding column of

 $\verb|x.train|. If use quants is true, then $min(numcut, the number of unique values in the corresponding content is true, then $min(numcut, the number of unique values in the corresponding content is true, then $min(numcut, the number of unique values in the corresponding content is true, then $min(numcut, the number of unique values in the corresponding content is true, then $min(numcut, the number of unique values in the corresponding content is true, then $min(numcut, the number of unique values in the corresponding content is true, then $min(numcut, the number of unique values in the corresponding content is true, then $min(numcut, the number of unique values in the corresponding content is true, the corresponding content is the corresponding content is true, the corresponding content is true, the corresponding content is the corresponding content is true, the corresponding content is the corresponding content is true, the corresponding content is the correspon$ 

1) values are used.

ndpost The number of posterior draws returned.

nskip Number of MCMC iterations to be treated as burn in.

printevery As the MCMC runs, a message is printed every printevery draws.

keepevery Every keepevery draw is kept to be returned to the user.

transposed When running gbart in parallel, it is more memory-efficient to transpose x.train

and x. test, if any, prior to calling mc.gbart.

hostname When running on a cluster occasionally it is useful to track on which node each

chain is running; to do so set this argument to TRUE.

seed Setting the seed required for reproducible MCMC.

mc.cores Number of cores to employ in parallel.

nice Set the job niceness. The default niceness is 19: niceness goes from 0 (highest)

to 19 (lowest).

#### **Details**

BART is a Bayesian MCMC method. At each MCMC interation, we produce a draw from the joint posterior  $(f, \sigma)|(x, y)$  in the numeric y case and just f in the binary y case.

Thus, unlike a lot of other modelling methods in R, we do not produce a single model object from which fits and summaries may be extracted. The output consists of values  $f^*(x)$  (and  $\sigma^*$  in the numeric case) where \* denotes a particular draw. The x is either a row from the training data, x.train or the test data, x.test.

For x.train/x.test with missing data elements, gbart will singly impute them with hot decking. For one or more missing covariates, record-level hot-decking imputation deWaPann11 is employed that is biased towards the null, i.e., nonmissing values from another record are randomly selected regardless of the outcome. Since mc.gbart runs multiple gbart threads in parallel, mc.gbart performs multiple imputation with hot decking, i.e., a separate imputation for each thread. This record-level hot-decking imputation is biased towards the null, i.e., nonmissing values from another record are randomly selected regardless of y.train.

#### Value

gbart returns an object of type gbart which is essentially a list. In the numeric y case, the list has components:

 $yhat.train \qquad A \ matrix \ with \ ndpost \ rows \ and \ nrow(x.train) \ columns. \ Each \ row \ corresponds$ 

to a draw  $f^*$  from the posterior of f and each column corresponds to a row of x.train. The (i,j) value is  $f^*(x)$  for the  $i^{th}$  kept draw of f and the  $j^{th}$  row of

x.train.

Burn-in is dropped.

yhat. test Same as yhat.train but now the x's are the rows of the test data.

yhat.train.mean

train data fits = mean of yhat.train columns.

yhat.test.mean test data fits = mean of yhat.test columns.

sigma post burn in draws of sigma, length = ndpost.

first.sigma burn-in draws of sigma.

varcount a matrix with ndpost rows and nrow(x.train) columns. Each row is for a draw.

For each variable (corresponding to the columns), the total count of the number of times that variable is used in a tree decision rule (over all trees) is given.

sigest The rough error standard deviation ( $\sigma$ ) used in the prior.

#### See Also

pbart

# **Examples**

```
##simulate data (example from Friedman MARS paper) f = function(x) \{ \\ 10*sin(pi*x[,1]*x[,2]) + 20*(x[,3]-.5)^2+10*x[,4]+5*x[,5] \}
```

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```
sigma = 1.0 \# y = f(x) + sigma*z, z^N(0,1)
             #number of observations
n = 100
set.seed(99)
x=matrix(runif(n*10),n,10) #10 variables, only first 5 matter
Ey = f(x)
y=Ey+sigma*rnorm(n)
lmFit = lm(y^{-}, data.frame(x,y)) #compare lm fit to BART later
##test BART with token run to ensure installation works
set.seed(99)
bartFit = wbart(x,y,nskip=5,ndpost=5)
## Not run:
##run BART
set.seed(99)
bartFit = wbart(x,y)
##compare BART fit to linear matter and truth = Ey
fitmat = cbind(y,Ey,lmFit$fitted,bartFit$yhat.train.mean)
colnames(fitmat) = c('y', 'Ey', 'lm', 'bart')
print(cor(fitmat))
## End(Not run)
```

gewekediag

Geweke's convergence diagnostic

#### **Description**

Geweke (1992) proposed a convergence diagnostic for Markov chains based on a test for equality of the means of the first and last part of a Markov chain (by default the first 10% and the last 50%). If the samples are drawn from the stationary distribution of the chain, the two means are equal and Geweke's statistic has an asymptotically standard normal distribution.

The test statistic is a standard Z-score: the difference between the two sample means divided by its estimated standard error. The standard error is estimated from the spectral density at zero and so takes into account any autocorrelation.

The Z-score is calculated under the assumption that the two parts of the chain are asymptotically independent, which requires that the sum of frac1 and frac2 be strictly less than 1.

Adapted from the geweke.diag function of the coda package which passes mcmc objects as arguments rather than matrices.

## Usage

```
gewekediag(x, frac1=0.1, frac2=0.5)
```

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#### **Arguments**

x Matrix of MCMC chains: the rows are the samples and the columns are different

"parameters". For BART, generally, the columns are estimates of f. For pbart, they are different subjects. For surv.bart, they are different subjects at a grid

of times.

frac1 fraction to use from beginning of chain

frac2 fraction to use from end of chain

#### Value

Z-scores for a test of equality of means between the first and last parts of the chain. A separate statistic is calculated for each variable in each chain.

#### References

Geweke J. (1992) Evaluating the Accuracy of Sampling-Based Approaches to the Calculation of Posterior Moments. In JM Bernado, JO Berger, AP Dawid, AFM Smith (eds.), Bayesian Statistics 4, pp. 169-193. Oxford University Press, Oxford.

Plummer M., Best N., Cowles K. and Vines K. (2006) CODA: Convergence Diagnosis and Output Analysis for MCMC. R News, vol 6, 7-11.

#### See Also

spectrum0ar.

```
## load survival package for the advanced lung cancer example
data(lung)
group <- -which(is.na(lung[ , 7])) ## remove missing row for ph.karno</pre>
times <- lung[group, 2]
                         ##lung$time
delta <- lung[group, 3]-1 ##lung$status: 1=censored, 2=dead</pre>
                           ##delta: 0=censored, 1=dead
## this study reports time in days rather than months like other studies
## coarsening from days to months will reduce the computational burden
times <- ceiling(times/30)</pre>
summary(times)
table(delta)
x.train <- as.matrix(lung[group, c(4, 5, 7)]) ## matrix of observed covariates
## lung$age:
                    Age in years
                    Male=1 Female=2
## lung$sex:
## lung$ph.karno:
                    Karnofsky performance score (dead=0:normal=100:by=10)
##
                    rated by physician
dimnames(x.train)[[2]] \leftarrow c('age(yr)', 'M(1):F(2)', 'ph.karno(0:100:10)')
```

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```
summary(x.train[ , 1])
table(x.train[ , 2])
table(x.train[ , 3])
x.test <- matrix(nrow=84, ncol=3) ## matrix of covariate scenarios</pre>
dimnames(x.test)[[2]] <- dimnames(x.train)[[2]]</pre>
i <- 1
for(age in 5*(9:15)) for(sex in 1:2) for(ph.karno in 10*(5:10)) {
    x.test[i, ] <- c(age, sex, ph.karno)</pre>
    i <- i+1
}
## Not run:
    set.seed(99)
   post <- surv.bart(x.train=x.train, times=times, delta=delta, x.test=x.test)</pre>
    ## in the interest of time, consider speeding it up by parallel processing
    ## run "mc.cores" number of shorter MCMC chains in parallel processes
    ## post <- mc.surv.bart(x.train=x.train, times=times, delta=delta,</pre>
                             x.test=x.test, mc.cores=8, seed=99)
   N <- nrow(x.test)
   K <- post$K
    ## select 10 lung cancer patients uniformly spread out over the data set
    h \leftarrow seq(1, N*K, floor(N/10)*K)
    for(i in h) {
        post.mcmc \leftarrow post\yhat.test[ , (i-1)+1:K]
        z <- gewekediag(post.mcmc)$z</pre>
        y \leftarrow max(c(4, abs(z)))
        \#\# plot the z scores vs. time for each patient
        if(i==1) plot(posttimes, z, ylim=c(-y, y), type='l',
                       xlab='t', ylab='z')
        else lines(post$times, z, type='l')
    ## add two-sided alpha=0.05 critical value lines
    lines(post$times, rep(-1.96, K), type='1', lty=2)
    lines(post$times, rep( 1.96, K), type='l', lty=2)
## End(Not run)
```

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## **Description**

```
BART is a Bayesian "sum-of-trees" model.
```

For numeric response y, we have  $y = f(x) + \epsilon$ , where  $\epsilon \sim Log(0, 1)$ .

For a binary response y, P(Y=1|x)=F(f(x)), where F denotes the standard Logistic CDF (logit link).

In both cases, f is the sum of many tree models. The goal is to have very flexible inference for the uknown function f.

In the spirit of "ensemble models", each tree is constrained by a prior to be a weak learner so that it contributes a small amount to the overall fit.

#### Usage

```
lbart(
    x.train, y.train, x.test=matrix(0.0,0,0),
    sparse=FALSE, a=0.5, b=1, augment=FALSE, rho=NULL,
    xinfo=matrix(0.0,0,0), usequants=FALSE,
    cont=FALSE, rm.const=TRUE, tau.interval=0.95,
    k=2.0, power=2.0, base=.95,
    binaryOffset=NULL,
    ntree=200L, numcut=100L,
    ndpost=1000L, nskip=100L,
    keepevery=1L,
    nkeeptrain=ndpost, nkeeptest=ndpost,

    nkeeptreedraws=ndpost,
    printevery=100L, transposed=FALSE
)
```

### **Arguments**

x.train Explanatory variables for training (in sample) data.

May be a matrix or a data frame, with (as usual) rows corresponding to observations and columns to variables.

If a variable is a factor in a data frame, it is replaced with dummies. Note that q dummies are created if q>2 and one dummy is created if q=2, where q is the number of levels of the factor. 1bart will generate draws of f(x) for each x which is a row of x.train.

y. train Binary dependent variable for training (in sample) data.

x. test Explanatory variables for test (out of sample) data.

Should have same structure as x.train.

lbart will generate draws of f(x) for each x which is a row of x.test.

sparse Whether to perform variable selection based on a sparse Dirichlet prior rather than simply uniform; see Linero 2016.

Sparse parameter for Beta(a,b) prior:  $0.5 \le a \le 1$  where lower values inducing more sparsity.

а

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Sparse parameter for Beta(a, b) prior; typically, b = 1. b

rho Sparse parameter: typically rho = p where p is the number of covariates under

consideration.

Whether data augmentation is to be performed in sparse variable selection. augment

xinfo You can provide the cutpoints to BART or let BART choose them for you. To

> provide them, use the xinfo argument to specify a list (matrix) where the items (rows) are the covariates and the contents of the items (columns) are the cut-

points.

If usequants=FALSE, then the cutpoints in xinfo are generated uniformly; othusequants

erwise, if TRUE, uniform quantiles are used for the cutpoints.

Whether or not to assume all variables are continuous. cont

Whether or not to remove constant variables. rm.const

tau.interval The width of the interval to scale the variance for the terminal leaf values.

For numeric y, k is the number of prior standard deviations E(Y|x) = f(x)

is away from +/-.5. For binary y, k is the number of prior standard deviations f(x) is away from +/-3. In both cases, the bigger k is, the more conservative the

fitting will be.

power Power parameter for tree prior. Base parameter for tree prior.

binaryOffset Used for binary y.

base

The model is P(Y = 1|x) = F(f(x) + binaryOffset).

The number of trees in the sum. ntree

The number of possible values of c (see usequants). If a single number if given, numcut

> this is used for all variables. Otherwise a vector with length equal to ncol(x.train) is required, where the  $i^{th}$  element gives the number of c used for the  $i^{th}$  variable in x.train. If usequants is false, numcut equally spaced cutoffs are used covering the range of values in the corresponding column of x.train. If usequants is true, then min(numcut, the number of unique values in the corresponding columns of

x.train - 1) c values are used.

ndpost The number of posterior draws returned.

Number of MCMC iterations to be treated as burn in. nskip

Number of MCMC iterations to be returned for train data. nkeeptrain

Number of MCMC iterations to be returned for test data. nkeeptest

nkeeptreedraws Number of MCMC iterations to be returned for tree draws.

Every keepevery draw is kept to be returned to the user. keepevery

printevery As the MCMC runs, a message is printed every printevery draws.

transposed When running 1bart in parallel, it is more memory-efficient to transpose x.train

and x. test, if any, prior to calling mc.lbart.

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#### **Details**

BART is an Bayesian MCMC method. At each MCMC interation, we produce a draw from the joint posterior f|(x, y) in the numeric y case and just f in the binary y case.

Thus, unlike a lot of other modelling methods in R, we do not produce a single model object from which fits and summaries may be extracted. The output consists of values  $f^*(x)$  where \* denotes a particular draw. The x is either a row from the training data (x.train) or the test data (x.test).

#### Value

lbart returns an object of type lbart which is essentially a list.

yhat.train A matrix with ndpost rows and nrow(x.train) columns. Each row corresponds

to a draw  $f^*$  from the posterior of f and each column corresponds to a row of x.train. The (i, j) value is  $f^*(x)$  for the  $i^{th}$  kept draw of f and the  $j^{th}$  row of

x.train.

Burn-in is dropped.

yhat.test Same as yhat.train but now the x's are the rows of the test data.

yhat.train.mean

train data fits = mean of yhat.train columns.

yhat.test.mean test data fits = mean of yhat.test columns.

varcount a matrix with ndpost rows and nrow(x.train) columns. Each row is for a draw.

For each variable (corresponding to the columns), the total count of the number of times that variable is used in a tree decision rule (over all trees) is given.

In addition, the list has a binaryOffset giving the value used.

Note that in the binary y, case yhat.train and yhat.test are f(x) + binaryOffset. If you want draws of the probability P(Y = 1|x) you need to apply the Logistic CDF (plogis) to these values.

#### See Also

wbart

```
data(ACTG175)
## exclude those who do not have CD4 count at 96 weeks
ex <- is.na(ACTG175$cd496)
table(ex)
## inclusion criteria are CD4 counts between 200 and 500
ACTG175$cd40 <- min(500, max(250, ACTG175$cd40))
## calculate relative CD4 decline
y <- ((ACTG175$cd496-ACTG175$cd40)/ACTG175$cd40)[!ex]
summary(y)
## 0=failure, 1=success</pre>
```

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```
y < -1*(y > -0.5)
## summarize CD4 outcomes
table(y, ACTG175$arms[!ex])
table(y, ACTG175$arms[!ex])/
    matrix(table(ACTG175$arms[!ex]), nrow=2, ncol=4, byrow=TRUE)
## drop unneeded and unwanted variables
## 1: 'pidnum' patient ID number
##14: 'str2' which will be handled by strat1 below
##15: 'strat' which will be handled by strat1-strat3 below
##17: 'treat' handled by arm0-arm3 below
##18: 'offtrt' indicator of off-treatment before 96 weeks
##20: 'cd420' CD4 T cell count at 20 weeks
##21: 'cd496' CD4 T cell count at 96 weeks
##22: 'r' missing CD4 T cell count at 96 weeks
##24: 'cd820' CD8 T cell count at 20 weeks
##25: 'cens' indicator of observing the event in days
##26: 'days' number of days until the primary endpoint
##27: 'arms' handled by arm0-arm3 below
train <- as.matrix(ACTG175)[!ex, -c(1, 14:15, 17, 18, 20:22, 24:27)]
train <- cbind(1*(ACTG175\$strat[!ex]==1), \ 1*(ACTG175\$strat[!ex]==2),
               1*(ACTG175$strat[!ex]==3), train)
dimnames(train)[[2]][1:3] <- paste0('strat', 1:3)</pre>
train <- cbind(1*(ACTG175*arms[!ex]==0), 1*(ACTG175*arms[!ex]==1),
               1*(ACTG175$arms[!ex]==2), 1*(ACTG175$arms[!ex]==3), train)
dimnames(train)[[2]][1:4] \leftarrow paste0('arm', 0:3)
N <- nrow(train)
test0 <- train; test0[ , 1:4] <- 0; test0[ , 1] <- 1
test1 <- train; test1[ , 1:4] <- 0; test1[ , 2] <- 1
test2 <- train; test2[ , 1:4] <- 0; test2[ , 3] <- 1
test3 <- train; test3[ , 1:4] <- 0; test3[ , 4] <- 1
test <- rbind(test0, test1, test2, test3)</pre>
##test BART with token run to ensure installation works
## set.seed(21)
## post <- lbart(train, y, test, nskip=5, ndpost=5)</pre>
## Not run:
set.seed(21)
post <- lbart(train, y, test)</pre>
## turn z-scores into probabilities
post$prob.test <- plogis(post$yhat.test)</pre>
## average over the posterior samples
post$prob.test.mean <- apply(post$prob.test, 2, mean)</pre>
## place estimates for arms 0-3 next to each other for convenience
```

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```
itr <- cbind(post$prob.test.mean[(1:N)], post$prob.test.mean[N+(1:N)],</pre>
             post$prob.test.mean[2*N+(1:N)], post$prob.test.mean[3*N+(1:N)])
## find the BART ITR for each patient
itr.pick <- integer(N)</pre>
for(i in 1:N) itr.pick[i] <- which(itr[i, ]==max(itr[i, ]))-1</pre>
## arms 0 and 3 (monotherapy) are never chosen
table(itr.pick)
## do arms 1 and 2 show treatment heterogeneity?
\label{eq:diff. <-apply(post$prob.test[ , 2*N+(1:N)]-post$prob.test[ , N+(1:N)], 2, mean)}
plot(sort(diff.), type='h', main='ACTG175 trial: 50% CD4 decline from baseline at 96 weeks',
     xlab='Arm 2 (1) Preferable to the Right (Left)', ylab='Prob.Diff.: Arms 2 - 1')
library(rpart)
library(rpart.plot)
## make data frame for nicer names in the plot
var <- as.data.frame(train[ , -(1:4)])</pre>
dss <- rpart(diff. ~ var$age+var$gender+var$race+var$wtkg+var$cd40+var$cd80+
                   var$karnof+var$symptom+var$hemo+var$homo+var$drugs+var$z30+
                    var$zprior+var$oprior+var$strat1+var$strat2+var$strat3,
               method='anova', control=rpart.control(cp=0.1))
rpart.plot(dss, type=3, extra=101)
## if strat1==1 (antiretroviral naive), then arm 2 is better
## otherwise, arm 1
print(dss)
all0 <- apply(post$prob.test[ , (1:N)], 1, mean)</pre>
all1 <- apply(post$prob.test[ , N+(1:N)], 1, mean)</pre>
all2 <- apply(postprob.test[ , 2*N+(1:N)], 1, mean)
all3 <- apply(post$prob.test[ , 3*N+(1:N)], 1, mean)</pre>
## BART ITR
BART.itr <- apply(post$prob.test[ , c(N+which(itr.pick==1), 2*N+which(itr.pick==2))], 1, mean)
test <- train
test[ , 1:4] <- 0
test[test[ , 5]==0, 2] <- 1
test[test[ , 5]==1, 3] <- 1
## BART ITR simple
BART.itr.simp <- pwbart(test, post$treedraws)</pre>
BART.itr.simp <- apply(plogis(BART.itr.simp), 1, mean)</pre>
plot(density(BART.itr), xlab='Value', xlim=c(0.475, 0.775), lwd=2,
     main='ACTG175 trial: 50% CD4 decline from baseline at 96 weeks')
lines(density(BART.itr.simp), col='brown', lwd=2)
lines(density(all0), col='green', lwd=2)
lines(density(all1), col='red', lwd=2)
```

44 leukemia

leukemia

Bone marrow transplantation for leukemia and multi-state models

## Description

137 patients with acute myelocytic leukemia (AML) and acute lymphoblastic leukemia (ALL) were given oral busulfan (Bu) 4 mg/kg on each of 4 days and intravenous cyclophosphamide (Cy) 60 mg/kg on each of 2 days (BuCy2) followed by allogeneic bone marrow transplantation from an HLA-identical or one antigen disparate sibling.

## Usage

data(leukemia)

### Format

A data frame with 137 subjects on the following 22 variables.

- G Disease Group (1=ALL, 2=AML Low Risk in first remission, 3=AML High Risk not in first remission)
- TD Time To Death Or On Study Time
- TB Disease Free Survival Time (Time To Relapse, Death Or End Of Study)
- D Death Indicator (0=Alive, 1=Dead)
- R Relapse Indicator (0=Disease Free, 1=Relapsed)
- B Disease Free Survival Indicator (0=Alive and Disease Free, 1=Dead or Relapsed)
- TA Time To Acute Graft-Versus-Host Disease (GVHD)
- A Acute GVHD Indicator (0=Never Developed Acute GVHD, 1=Developed Acute GVHD)
- TC Time To Chronic Graft-Versus-Host Disease (GVHD)
- C Chronic GVHD Indicator (0=Never Developed Chronic GVHD, 1=Developed Chronic GVHD)
- TP Time of Platelets Returning to Normal Levels
- P Platelet Recovery Indicator (0=Platelets Never Returned to Normal, 1=Platelets Returned To Normal)
- X1 Patient Age In Years
- X2 Donor Age In Years

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- X3 Patient Gender (0=female, 1=male)
- X4 Donor Gender (0=female, 1=male)
- X5 Patient Cytomegalovirus (CMV) Immune Status (0=CMV Negative, 1=CMV Positive)
- X6 Donor Cytomegalovirus (CMV) Immune Status (0=CMV Negative, 1=CMV Positive)
- X7 Waiting Time to Transplant In Days
- X8 AML Patients with Elevated Risk By French-American-British (FAB) Classification (0=Not AML/Elevated, 1=FAB M4 Or M5 with AML)
- X9 Hospital (1=The Ohio State University in Columbus, 2=Alfred in Melbourne, 3=St. Vincent in Sydney, 4=Hahnemann University in Philadelphia)
- X10 Methotrexate Used as a Graft-Versus-Host Disease Prophylactic (0=No, 1=Yes)

#### **Source**

Klein J. and Moeschberger M.L. (2003) *Survival Analysis: Techniques for Censored and Truncated Data*, New York: Springer-Verlag, 2nd Ed., Section 1.3.

#### References

Copelan E., Biggs J., Thompson J., Crilley P., Szer J., Klein, J., Kapoor N., Avalos, B., Cunningham I. and Atkinson, K. (1991) "Treatment for acute myelocytic leukemia with allogeneic bone marrow transplantation following preparation with BuCy2". *Blood*, **78**(3), pp.838-843.

lung

NCCTG Lung Cancer Data

## **Description**

Survival in patients with advanced lung cancer from the North Central Cancer Treatment Group. Performance scores rate how well the patient can perform usual daily activities.

#### **Format**

inst: Institution code time: Survival time in days

status: censoring status 1=censored, 2=dead

age: Age in years sex: Male=1 Female=2

ph.ecog: ECOG performance score (0=good 5=dead)

ph.karno: Karnofsky performance score (bad=0-good=100) rated by physician

pat.karno: Karnofsky performance score as rated by patient

meal.cal: Calories consumed at meals wt.loss: Weight loss in last six months

#### **Source**

Terry Therneau

#### References

Loprinzi CL. Laurie JA. Wieand HS. Krook JE. Novotny PJ. Kugler JW. Bartel J. Law M. Bateman M. Klatt NE. et al. Prospective evaluation of prognostic variables from patient-completed questionnaires. North Central Cancer Treatment Group. Journal of Clinical Oncology. 12(3):601-7, 1994.

#### **Examples**

data(lung)

mbart

Multinomial BART for categorical outcomes with fewer categories

## **Description**

BART is a Bayesian "sum-of-trees" model.

For numeric response y, we have  $y = f(x) + \epsilon$ , where  $\epsilon \sim N(0, 1)$ .

For a multinomial response y, P(Y = y|x) = F(f(x)), where F denotes the standard Normal CDF (probit link) or the standard Logistic CDF (logit link).

In both cases, f is the sum of many tree models. The goal is to have very flexible inference for the uknown function f.

In the spirit of "ensemble models", each tree is constrained by a prior to be a weak learner so that it contributes a small amount to the overall fit.

#### Usage

```
mbart(
      x.train, y.train,
      x.test=matrix(0,0,0), type='pbart',
      ntype=as.integer(
          factor(type,
                 levels=c('wbart', 'pbart', 'lbart'))),
      sparse=FALSE, theta=0, omega=1,
      a=0.5, b=1, augment=FALSE, rho=NULL,
      xinfo=matrix(0,0,0), usequants=FALSE,
      rm.const=TRUE,
      k=2, power=2, base=0.95,
      tau.num=c(NA, 3, 6)[ntype],
      offset=NULL,
      ntree=c(200L, 50L, 50L)[ntype], numcut=100L,
      ndpost=1000L, nskip=100L,
      keepevery=c(1L, 10L, 10L)[ntype],
```

```
printevery=100L, transposed=FALSE,
      hostname=FALSE,
      mc.cores = 2L, ## mc.bart only
                   ## mc.bart only
      nice = 19L,
      seed = 99L
                     ## mc.bart only
     )
mc.mbart(
         x.train, y.train,
         x.test=matrix(0,0,0), type='pbart',
         ntype=as.integer(
             factor(type,
                    levels=c('wbart', 'pbart', 'lbart'))),
         sparse=FALSE, theta=0, omega=1,
         a=0.5, b=1, augment=FALSE, rho=NULL,
         xinfo=matrix(0,0,0), usequants=FALSE,
         rm.const=TRUE,
         k=2, power=2, base=0.95,
         tau.num=c(NA, 3, 6)[ntype],
         offset=NULL,
         ntree=c(200L, 50L, 50L)[ntype], numcut=100L,
         ndpost=1000L, nskip=100L,
         keepevery=c(1L, 10L, 10L)[ntype],
         printevery=100L, transposed=FALSE,
         hostname=FALSE,
         mc.cores = 2L, ## mc.bart only
        nice = 19L,
                        ## mc.bart only
         seed = 99L
                        ## mc.bart only
        )
```

## **Arguments**

x.train Explanatory variables for training (in sample) data.

May be a matrix or a data frame, with (as usual) rows corresponding to observations and columns to variables.

If a variable is a factor in a data frame, it is replaced with dummies. Note that q dummies are created if q>2 and one dummy is created if q=2, where q is the number of levels of the factor. mbart will generate draws of f(x) for each x which is a row of x.train.

y.train Categorical dependent variable for training (in sample) data.

x.test Explanatory variables for test (out of sample) data.

Should have same structure as x.train.

mbart will generate draws of f(x) for each x which is a row of x. test.

type You can use this argument to specify the type of fit. 'pbart' for probit BART

or 'lbart' for logit BART.

ntype The integer equivalent of type where 'pbart' is 2 and 'lbart' is 3.

sparse Whether to perform variable selection based on a sparse Dirichlet prior rather

than simply uniform; see Linero 2016.

theta Set *theta* parameter; zero means random.

omega Set *omega* parameter; zero means random.

Sparse parameter for Beta(a,b) prior:  $0.5 \le a \le 1$  where lower values

inducing more sparsity.

b Sparse parameter for Beta(a, b) prior; typically, b = 1.

rho Sparse parameter: typically rho = p where p is the number of covariates under

consideration.

augment Whether data augmentation is to be performed in sparse variable selection.

xinfo You can provide the cutpoints to BART or let BART choose them for you. To

provide them, use the xinfo argument to specify a list (matrix) where the items (rows) are the covariates and the contents of the items (columns) are the cut-

points.

usequants If usequants=FALSE, then the cutpoints in xinfo are generated uniformly; oth-

erwise, if TRUE, uniform quantiles are used for the cutpoints.

rm.const Whether or not to remove constant variables.

For categorical y. train, k is the number of prior standard deviations f(x) is

away from  $\pm$ /-3.

power Power parameter for tree prior.

Base parameter for tree prior.

tau.num The numerator in the tau definition, i.e., tau=tau.num/(k\*sqrt(ntree)).

offset With Multinomial BART, the centering is P(yj = 1|x) = F(fj(x) + offset[j])

where offset defaults to  $F^{-1}(mean(y.train))$ . You can use the offset

parameter to over-ride these defaults.

ntree The number of trees in the sum.

numcut The number of possible values of c (see usequants). If a single number if given,

this is used for all variables. Otherwise a vector with length equal to  $\operatorname{ncol}(x.\operatorname{train})$  is required, where the  $i^{th}$  element gives the number of c used for the  $i^{th}$  variable in x.train. If usequants is false, numcut equally spaced cutoffs are used covering the range of values in the corresponding column of x.train. If usequants is true, then  $\min(\operatorname{numcut}$ , the number of unique values in the corresponding columns of

x.train - 1) c values are used.

ndpost The number of posterior draws returned.

nskip Number of MCMC iterations to be treated as burn in.

keepevery Every keepevery draw is kept to be returned to the user.

printevery As the MCMC runs, a message is printed every printevery draws.

transposed When running mbart in parallel, it is more memory-efficient to transpose x.train

and x. test, if any, prior to calling mc.mbart.

hostname When running on a cluster occasionally it is useful to track on which node each

chain is running; to do so set this argument to TRUE.

seed Setting the seed required for reproducible MCMC.

mc.cores Number of cores to employ in parallel.

nice Set the job niceness. The default niceness is 19: niceness goes from 0 (highest)

to 19 (lowest).

#### **Details**

BART is an Bayesian MCMC method. At each MCMC interation, we produce a draw from f in the categorical y case.

Thus, unlike a lot of other modelling methods in R, we do not produce a single model object from which fits and summaries may be extracted. The output consists of values  $f^*(x)$  where \* denotes a particular draw. The x is either a row from the training data (x.train).

#### Value

mbart returns an object of type mbart which is essentially a list.

yhat.train

A matrix with ndpost rows and nrow(x.train)\*K columns. Each row corresponds to a draw  $f^*$  from the posterior of f and each column corresponds to an estimate for a row of x.train. For the ith row of x.train, we provide the corresponding (i-1)\*K+jth column of yhat.train where j=1,...,K indexes the categories.

Burn-in is dropped.

yhat.train.mean

train data fits = mean of yhat.train columns.

varcount

a matrix with ndpost rows and nrow(x.train) columns. Each row is for a draw. For each variable (corresponding to the columns), the total count of the number of times that variable is used in a tree decision rule (over all trees) is given.

In addition, the list has a offset vector giving the value used.

Note that in the multinomial y case yhat. train is f(x) + offset[j].

#### See Also

```
gbart, alligator
```

```
N=500
set.seed(12)
x1=runif(N)
x2=runif(N, max=1-x1)
x3=1-x1-x2
x.train=cbind(x1, x2, x3)
y.train=0
for(i in 1:N)
    y.train[i]=sum((1:3)*rmultinom(1, 1, x.train[i, ]))
table(y.train)/N
```

```
##test mbart with token run to ensure installation works
set.seed(99)
post = mbart(x.train, y.train, nskip=1, ndpost=1)

## Not run:
set.seed(99)
post=mbart(x.train, y.train, x.train)
##mc.post=mbart(x.train, y.train, x.test, mc.cores=8, seed=99)

K=3
i=seq(1, N*K, K)-1
for(j in 1:K)
    print(cor(x.train[ , j], post$prob.test.mean[i+j])^2)

## End(Not run)
```

mbart2

Multinomial BART for categorical outcomes with more categories

## Description

BART is a Bayesian "sum-of-trees" model.

For numeric response y, we have  $y = f(x) + \epsilon$ , where  $\epsilon \sim N(0, 1)$ .

For a multinomial response y, P(Y = y|x) = F(f(x)), where F denotes the standard Normal CDF (probit link) or the standard Logistic CDF (logit link).

In both cases, f is the sum of many tree models. The goal is to have very flexible inference for the uknown function f.

In the spirit of "ensemble models", each tree is constrained by a prior to be a weak learner so that it contributes a small amount to the overall fit.

## Usage

```
ndpost=1000L, nskip=100L,
     keepevery=c(1L, 10L, 10L)[ntype],
     printevery=100L, transposed=FALSE,
     hostname=FALSE,
     mc.cores = 2L, ## mc.bart only
     nice = 19L,
                    ## mc.bart only
     seed = 99L
                     ## mc.bart only
     )
mc.mbart2(
         x.train, y.train,
         x.test=matrix(0,0,0), type='lbart',
         ntype=as.integer(
             factor(type,
                    levels=c('wbart', 'pbart', 'lbart'))),
         sparse=FALSE, theta=0, omega=1,
         a=0.5, b=1, augment=FALSE, rho=NULL,
         xinfo=matrix(0,0,0), usequants=FALSE,
         rm.const=TRUE,
         k=2, power=2, base=0.95,
         tau.num=c(NA, 3, 6)[ntype],
         offset=NULL,
         ntree=c(200L, 50L, 50L)[ntype], numcut=100L,
         ndpost=1000L, nskip=100L,
         keepevery=c(1L, 10L, 10L)[ntype],
         printevery=100L, transposed=FALSE,
         hostname=FALSE,
         mc.cores = 2L, ## mc.bart only
         nice = 19L,
                       ## mc.bart only
         seed = 99L
                        ## mc.bart only
        )
```

## **Arguments**

x.train Explanatory variables for training (in sample) data.

May be a matrix or a data frame, with (as usual) rows corresponding to observations and columns to variables.

If a variable is a factor in a data frame, it is replaced with dummies. Note that q dummies are created if q>2 and one dummy is created if q=2, where q is the number of levels of the factor. mbart2 will generate draws of f(x) for each x which is a row of x.train.

y.train Categorical dependent variable for training (in sample) data.

x.test Explanatory variables for test (out of sample) data.
Should have same structure as x.train.

mbart2 will generate draws of f(x) for each x which is a row of x.test.

type You can use this argument to specify the type of fit. 'pbart' for probit BART

or 'lbart' for logit BART.

ntype The integer equivalent of type where 'pbart' is 2 and 'lbart' is 3.

sparse Whether to perform variable selection based on a sparse Dirichlet prior rather

than simply uniform; see Linero 2016.

theta Set *theta* parameter; zero means random.

omega Set *omega* parameter; zero means random.

a Sparse parameter for Beta(a,b) prior: 0.5 <= a <= 1 where lower values

inducing more sparsity.

b Sparse parameter for Beta(a, b) prior; typically, b = 1.

rho Sparse parameter: typically rho = p where p is the number of covariates under

consideration.

augment Whether data augmentation is to be performed in sparse variable selection.

xinfo You can provide the cutpoints to BART or let BART choose them for you. To

provide them, use the xinfo argument to specify a list (matrix) where the items (rows) are the covariates and the contents of the items (columns) are the cut-

points.

usequants If usequants=FALSE, then the cutpoints in xinfo are generated uniformly; oth-

erwise, if TRUE, uniform quantiles are used for the cutpoints.

rm. const Whether or not to remove constant variables.

k For categorical y train, k is the number of prior standard deviations f(x) is

away from  $\pm$ -3.

power Power parameter for tree prior.

base Base parameter for tree prior.

tau.num The numerator in the tau definition, i.e., tau=tau.num/(k\*sqrt(ntree)).

offset With Multinomial BART, the centering is P(yj = 1|x) = F(fj(x) + offset[j])

where offset defaults to  $F^{-1}(mean(y.train))$ . You can use the offset

parameter to over-ride these defaults.

ntree The number of trees in the sum.

numcut The number of possible values of c (see usequants). If a single number if given,

this is used for all variables. Otherwise a vector with length equal to ncol(x.train) is required, where the  $i^{th}$  element gives the number of c used for the  $i^{th}$  variable in x.train. If usequants is false, numcut equally spaced cutoffs are used covering the range of values in the corresponding column of x.train. If usequants is true, then min(numcut, the number of unique values in the corresponding columns of

x.train - 1) c values are used.

ndpost The number of posterior draws returned.

nskip Number of MCMC iterations to be treated as burn in. keepevery Every keepevery draw is kept to be returned to the user.

printevery As the MCMC runs, a message is printed every printevery draws.

transposed When running mbart2 in parallel, it is more memory-efficient to transpose x. train

and x. test, if any, prior to calling mc.mbart2.

hostname When running on a cluster occasionally it is useful to track on which node each

chain is running; to do so set this argument to TRUE.

seed Setting the seed required for reproducible MCMC.

mc. cores Number of cores to employ in parallel.

nice Set the job niceness. The default niceness is 19: niceness goes from 0 (highest)

to 19 (lowest).

#### **Details**

BART is an Bayesian MCMC method. At each MCMC interation, we produce a draw from f in the categorical y case.

Thus, unlike a lot of other modelling methods in R, we do not produce a single model object from which fits and summaries may be extracted. The output consists of values  $f^*(x)$  where \* denotes a particular draw. The x is either a row from the training data (x.train).

#### Value

mbart2 returns an object of type mbart2 which is essentially a list.

yhat.train

A matrix with ndpost rows and nrow(x.train)\*K columns. Each row corresponds to a draw  $f^*$  from the posterior of f and each column corresponds to an estimate for a row of x.train. For the ith row of x.train, we provide the corresponding (i-1)\*K+jth column of yhat.train where j=1,...,K indexes the categories.

Burn-in is dropped.

yhat.train.mean

train data fits = mean of yhat.train columns.

varcount

a matrix with ndpost rows and nrow(x.train) columns. Each row is for a draw. For each variable (corresponding to the columns), the total count of the number of times that variable is used in a tree decision rule (over all trees) is given.

In addition, the list has a offset vector giving the value used.

Note that in the multinomial y case yhat. train is f(x) + offset[j].

#### See Also

```
gbart, alligator
```

```
N=500
set.seed(12)
x1=runif(N)
x2=runif(N, max=1-x1)
x3=1-x1-x2
x.train=cbind(x1, x2, x3)
y.train=0
```

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```
for(i in 1:N)
    y.train[i]=sum((1:3)*rmultinom(1, 1, x.train[i, ]))
table(y.train)/N

##test mbart2 with token run to ensure installation works
set.seed(99)
post = mbart2(x.train, y.train, nskip=1, ndpost=1)

## Not run:
set.seed(99)
post=mbart2(x.train, y.train, x.train)
##mc.post=mbart2(x.train, y.train, x.test, mc.cores=8, seed=99)

K=3
i=seq(1, N*K, K)-1
for(j in 1:K)
    print(cor(x.train[ , j], post*prob.test.mean[i+j])^2)

## End(Not run)
```

mc.cores.openmp

Detecting OpenMP

#### **Description**

This package was designed for OpenMP. For example, the pwbart function can use OpenMP or the parallel R package for multi-threading. On UNIX/Unix-like systems, OpenMP, if available, is discovered at install time; for the details, see the configure.ac file which can be found in the source version of this package. However, we know of no GPL licensed code available to detect OpenMP on Windows (for Artistic licensed OpenMP detection code on Windows, see the Bioconductor R package rGADEM). To determine whether OpenMP is available at run time, we provide the function documented here.

## Usage

```
mc.cores.openmp()
```

#### Value

Returns a zero when OpenMP is not available, otherwise, an integer greater than zero when OpenMP is available (returns one unless you are running in a multi-threaded process).

#### See Also

pwbart

mc.crisk.pwbart 55

#### **Examples**

```
mc.cores.openmp()
```

mc.crisk.pwbart

Predicting new observations with a previously fitted BART model

## Description

```
BART is a Bayesian "sum-of-trees" model. For a numeric response y, we have y=f(x)+\epsilon, where \epsilon \sim N(0,\sigma^2).
```

f is the sum of many tree models. The goal is to have very flexible inference for the uknown function f.

In the spirit of "ensemble models", each tree is constrained by a prior to be a weak learner so that it contributes a small amount to the overall fit.

## Usage

#### **Arguments**

x.testMatrix of covariates to predict y for cause 1.x.test2Matrix of covariates to predict y for cause 2.

treedraws
treedraws2

\$treedraws for cause 1.
treedraws2

binaryOffset Mean to add on to y prediction for cause 1. binaryOffset2 Mean to add on to y prediction for cause 2.

mc.cores Number of threads to utilize.

type Whether to employ Albert-Chib, 'pbart', or Holmes-Held, 'lbart'.

transposed When running pwbart or mc.pwbart in parallel, it is more memory-efficient to

transpose x. test prior to calling the internal versions of these functions.

nice Set the job niceness. The default niceness is 19: niceness goes from 0 (highest)

to 19 (lowest).

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## **Details**

BART is an Bayesian MCMC method. At each MCMC interation, we produce a draw from the joint posterior  $(f, \sigma)|(x, y)$  in the numeric y case and just f in the binary y case.

Thus, unlike a lot of other modelling methods in R, we do not produce a single model object from which fits and summaries may be extracted. The output consists of values  $f^*(x)$  (and  $\sigma^*$  in the numeric case) where \* denotes a particular draw. The x is either a row from the training data (x.train) or the test data (x.test).

## Value

Returns an object of type criskbart which is essentially a list with components:

yhat.test	A matrix with ndpost rows and nrow(x.test) columns. Each row corresponds to a draw $f^*$ from the posterior of $f$ and each column corresponds to a row of x.train. The $(i,j)$ value is $f^*(x)$ for the $i^{th}$ kept draw of $f$ and the $j^{th}$ row of x.train. Burn-in is dropped.
surv.test	test data fits for survival probability.
surv.test.mean	mean of surv. test over the posterior samples.
prob.test	The probability of suffering cause 1 which is occasionally useful, e.g., in calculating the concordance.
prob.test2	The probability of suffering cause $2$ which is occasionally useful, e.g., in calculating the concordance.
cif.test	The cumulative incidence function of cause 1, $F_1(t,x)$ , where x's are the rows of the test data.
cif.test2	The cumulative incidence function of cause 2, $F_2(t,x)$ , where x's are the rows of the test data.
yhat.test.mean	test data fits = mean of yhat.test columns.
cif.test.mean	mean of cif.test columns for cause 1.
cif.test2.mean	mean of cif.test2 columns for cause 2.

#### See Also

```
pwbart, crisk.bart, mc.crisk.bart
```

```
data(transplant)

delta <- (as.numeric(transplant$event)-1)
## recode so that delta=1 is cause of interest; delta=2 otherwise
delta[delta==1] <- 4
delta[delta==2] <- 1
delta[delta>1] <- 2
table(delta, transplant$event)</pre>
```

mc.crisk.pwbart 57

```
times <- pmax(1, ceiling(transplant$futime/7)) ## weeks</pre>
##times <- pmax(1, ceiling(transplant$futime/30.5)) ## months</pre>
table(times)
type0 <- 1*(transplant$abo=='0')</pre>
typeA <- 1*(transplant$abo=='A')</pre>
typeB <- 1*(transplant$abo=='B')</pre>
typeAB <- 1*(transplant$abo=='AB')</pre>
table(typeA, type0)
x.train <- cbind(type0, typeA, typeB, typeAB)</pre>
x.test <- cbind(1, 0, 0, 0)
dimnames(x.test)[[2]] <- dimnames(x.train)[[2]]</pre>
## parallel::mcparallel/mccollect do not exist on windows
if(.Platform$OS.type=='unix') {
##test BART with token run to ensure installation works
        post <- mc.crisk.bart(x.train=x.train, times=times, delta=delta,</pre>
                                 seed=99, mc.cores=2, nskip=5, ndpost=5,
                                 keepevery=1)
        pre <- surv.pre.bart(x.train=x.train, x.test=x.test,</pre>
                               times=times, delta=delta)
        K <- post$K
        pred <- mc.crisk.pwbart(pre$tx.test, pre$tx.test,</pre>
                                  post$treedraws, post$treedraws2,
                                  post$binaryOffset, post$binaryOffset2)
}
## Not run:
## run one long MCMC chain in one process
## set.seed(99)
## post <- crisk.bart(x.train=x.train, times=times, delta=delta, x.test=x.test)</pre>
## in the interest of time, consider speeding it up by parallel processing
## run "mc.cores" number of shorter MCMC chains in parallel processes
post <- mc.crisk.bart(x.train=x.train,</pre>
                        times=times, delta=delta,
                        x.test=x.test, seed=99, mc.cores=8)
check <- mc.crisk.pwbart(post$tx.test, post$tx.test,</pre>
                           post$treedraws, post$treedraws2,
                           post$binaryOffset,
                           post$binaryOffset2, mc.cores=8)
## check <- predict(post, newdata=post$tx.test, newdata2=post$tx.test2,</pre>
                     mc.cores=8)
print(c(post$surv.test.mean[1], check$surv.test.mean[1],
        post$surv.test.mean[1]-check$surv.test.mean[1]), digits=22)
```

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mc.crisk2.pwbart

Predicting new observations with a previously fitted BART model

## **Description**

```
BART is a Bayesian "sum-of-trees" model. For a numeric response y, we have y=f(x)+\epsilon, where \epsilon \sim N(0,\sigma^2).
```

f is the sum of many tree models. The goal is to have very flexible inference for the uknown function f.

In the spirit of "ensemble models", each tree is constrained by a prior to be a weak learner so that it contributes a small amount to the overall fit.

# Usage

# Arguments

x.test Matrix of covariates to predict y for cause 1. x.test2 Matrix of covariates to predict y for cause 2. treedraws y for cause 1. treedraws for cause 2. mc.crisk2.pwbart 59

binaryOffset Mean to add on to y prediction for cause 1. binaryOffset2 Mean to add on to y prediction for cause 2.

mc.cores Number of threads to utilize.

type Whether to employ Albert-Chib, 'pbart', or Holmes-Held, 'lbart'.

transposed When running pwbart or mc.pwbart in parallel, it is more memory-efficient to

transpose x. test prior to calling the internal versions of these functions.

nice Set the job niceness. The default niceness is 19: niceness goes from 0 (highest)

to 19 (lowest).

#### **Details**

BART is an Bayesian MCMC method. At each MCMC interation, we produce a draw from the joint posterior  $(f, \sigma)|(x, y)$  in the numeric y case and just f in the binary y case.

Thus, unlike a lot of other modelling methods in R, we do not produce a single model object from which fits and summaries may be extracted. The output consists of values  $f^*(x)$  (and  $\sigma^*$  in the numeric case) where \* denotes a particular draw. The x is either a row from the training data (x.train) or the test data (x.test).

## Value

Returns an object of type crisk2bart which is essentially a list with components:

yhat.test	A matrix with ndpost rows and nrow(x.test) columns. Each row corresponds to a draw $f^*$ from the posterior of $f$ and each column corresponds to a row of x.train. The $(i,j)$ value is $f^*(x)$ for the $i^{th}$ kept draw of $f$ and the $j^{th}$ row of x.train. Burn-in is dropped.
surv.test	test data fits for survival probability.

surv.test.mean mean of surv.test over the posterior samples.

prob. test The probability of suffering cause 1 which is occasionally useful, e.g., in calcu-

lating the concordance.

prob. test2 The probability of suffering cause 2 which is occasionally useful, e.g., in calcu-

lating the concordance.

cif.test The cumulative incidence function of cause 1,  $F_1(t,x)$ , where x's are the rows

of the test data.

cif.test2 The cumulative incidence function of cause 2,  $F_2(t,x)$ , where x's are the rows

of the test data.

 $\begin{tabular}{lll} $\tt yhat.test.mean & test data fits = mean of yhat.test columns. \\ &\tt cif.test.mean & mean of cif.test columns for cause 1. \\ \end{tabular}$ 

cif.test2.mean mean of cif.test2 columns for cause 2.

### See Also

```
pwbart, crisk2.bart, mc.crisk2.bart
```

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```
data(transplant)
delta <- (as.numeric(transplant$event)-1)</pre>
## recode so that delta=1 is cause of interest; delta=2 otherwise
delta[delta==1] <- 4
delta[delta==2] <- 1
delta[delta>1] <- 2</pre>
table(delta, transplant$event)
times <- pmax(1, ceiling(transplant$futime/7)) ## weeks</pre>
##times <- pmax(1, ceiling(transplant$futime/30.5)) ## months
table(times)
type0 <- 1*(transplant$abo=='0')</pre>
typeA <- 1*(transplant$abo=='A')</pre>
typeB <- 1*(transplant$abo=='B')</pre>
typeAB <- 1*(transplant$abo=='AB')</pre>
table(typeA, type0)
x.train <- cbind(type0, typeA, typeB, typeAB)</pre>
x.test <- cbind(1, 0, 0, 0)
dimnames(x.test)[[2]] <- dimnames(x.train)[[2]]</pre>
## parallel::mcparallel/mccollect do not exist on windows
if(.Platform$OS.type=='unix') {
##test BART with token run to ensure installation works
        post <- mc.crisk2.bart(x.train=x.train, times=times, delta=delta,</pre>
                                 seed=99, mc.cores=2, nskip=5, ndpost=5,
                                 keepevery=1)
        pre <- surv.pre.bart(x.train=x.train, x.test=x.test,</pre>
                               times=times, delta=delta)
        K <- post$K
        pred <- mc.crisk2.pwbart(pre$tx.test, pre$tx.test,</pre>
                                  post$treedraws, post$treedraws2,
                                  post$binaryOffset, post$binaryOffset2)
}
## Not run:
## run one long MCMC chain in one process
## set.seed(99)
## post <- crisk2.bart(x.train=x.train, times=times, delta=delta, x.test=x.test)</pre>
## in the interest of time, consider speeding it up by parallel processing
## run "mc.cores" number of shorter MCMC chains in parallel processes
post <- mc.crisk2.bart(x.train=x.train,</pre>
                        times=times, delta=delta,
```

```
x.test=x.test, seed=99, mc.cores=8)
check <- mc.crisk2.pwbart(post$tx.test, post$tx.test,</pre>
                          post$treedraws, post$treedraws2,
                          post$binaryOffset,
                          post$binaryOffset2, mc.cores=8)
## check <- predict(post, newdata=post$tx.test, newdata2=post$tx.test2,</pre>
                    mc.cores=8)
print(c(post$surv.test.mean[1], check$surv.test.mean[1],
        post$surv.test.mean[1]-check$surv.test.mean[1]), digits=22)
print(all(round(post$surv.test.mean, digits=9)==
    round(check$surv.test.mean, digits=9)))
print(c(post$cif.test.mean[1], check$cif.test.mean[1],
        post$cif.test.mean[1]-check$cif.test.mean[1]), digits=22)
print(all(round(post$cif.test.mean, digits=9)==
    round(check$cif.test.mean, digits=9)))
print(c(post$cif.test2.mean[1], check$cif.test2.mean[1],
        post$cif.test2.mean[1]-check$cif.test2.mean[1]), digits=22)
print(all(round(post$cif.test2.mean, digits=9)==
    round(check$cif.test2.mean, digits=9)))
## End(Not run)
```

mc.lbart

Logit BART for dichotomous outcomes with Logistic latents and parallel computation

# **Description**

BART is a Bayesian "sum-of-trees" model.

For numeric response y, we have  $y = f(x) + \epsilon$ , where  $\epsilon \sim Log(0, 1)$ .

For a binary response y, P(Y = 1|x) = F(f(x)), where F denotes the standard Logistic CDF (logit link).

In both cases, f is the sum of many tree models. The goal is to have very flexible inference for the uknown function f.

In the spirit of "ensemble models", each tree is constrained by a prior to be a weak learner so that it contributes a small amount to the overall fit.

## Usage

```
mc.lbart(
    x.train, y.train, x.test=matrix(0.0,0,0),
    sparse=FALSE, a=0.5, b=1, augment=FALSE, rho=NULL,
    xinfo=matrix(0.0,0,0), usequants=FALSE,
    cont=FALSE, rm.const=TRUE, tau.interval=0.95,
    k=2.0, power=2.0, base=.95,
    binaryOffset=NULL,
    ntree=50L, numcut=100L,
    ndpost=1000L, nskip=100L,
    keepevery=1L, printevery=100,
    keeptrainfits=TRUE, transposed=FALSE,

mc.cores = 2L, nice = 19L,
    seed = 99L
)
```

## **Arguments**

x.train Explanatory variables for training (in sample) data.

May be a matrix or a data frame, with (as usual) rows corresponding to observations and columns to variables.

If a variable is a factor in a data frame, it is replaced with dummies. Note that q dummies are created if q>2 and one dummy is created if q=2, where q is the number of levels of the factor. 1bart will generate draws of f(x) for each x which is a row of x.train.

y.train Dependent variable for training (in sample) data.

If y is numeric a continous response model is fit (normal errors).

If y is a factor (or just has values 0 and 1) then a binary response model with a logit link is fit.

x.test Explanatory variables for test (out of sample) data.

Should have same structure as x.train.

lbart will generate draws of f(x) for each x which is a row of x.test.

sparse Whether to perform variable selection based on a sparse Dirichlet prior rather

than simply uniform; see Linero 2016.

Sparse parameter for Beta(a,b) prior:  $0.5 \le a \le 1$  where lower values

inducing more sparsity.

b Sparse parameter for Beta(a, b) prior; typically, b = 1.

rho Sparse parameter: typically rho = p where p is the number of covariates under

consideration.

augment Whether data augmentation is to be performed in sparse variable selection.

xinfo You can provide the cutpoints to BART or let BART choose them for you. To

provide them, use the xinfo argument to specify a list (matrix) where the items (rows) are the covariates and the contents of the items (columns) are the cut-

points.

usequants If usequants=FALSE, then the cutpoints in xinfo are generated uniformly; oth-

erwise, if TRUE, uniform quantiles are used for the cutpoints.

cont Whether or not to assume all variables are continuous.

rm. const Whether or not to remove constant variables.

tau.interval The width of the interval to scale the variance for the terminal leaf values.

For numeric y, k is the number of prior standard deviations E(Y|x) = f(x)

is away from +/-.5. For binary y, k is the number of prior standard deviations f(x) is away from +/-3. In both cases, the bigger k is, the more conservative the

fitting will be.

power Power parameter for tree prior.

base Base parameter for tree prior.

binaryOffset Used for binary y.

The model is P(Y = 1|x) = F(f(x) + binaryOffset).

ntree The number of trees in the sum.

numcut The number of possible values of c (see usequants). If a single number if given,

this is used for all variables. Otherwise a vector with length equal to  $\operatorname{ncol}(x.\operatorname{train})$  is required, where the  $i^{th}$  element gives the number of c used for the  $i^{th}$  variable in x.train. If usequants is false, numcut equally spaced cutoffs are used covering the range of values in the corresponding column of x.train. If usequants is true, then  $\min(\operatorname{numcut})$ , the number of unique values in the corresponding columns of

x.train - 1) c values are used.

ndpost The number of posterior draws returned.

nskip Number of MCMC iterations to be treated as burn in. keepevery Every keepevery draw is kept to be returned to the user.

printevery As the MCMC runs, a message is printed every printevery draws.

keeptrainfits Whether to keep yhat. train or not.

transposed When running lbart in parallel, it is more memory-efficient to transpose x.train

and x.test, if any, prior to calling mc.lbart.

seed Setting the seed required for reproducible MCMC.

mc. cores Number of cores to employ in parallel.

nice Set the job niceness. The default niceness is 19: niceness goes from 0 (highest)

to 19 (lowest).

#### **Details**

BART is an Bayesian MCMC method. At each MCMC interation, we produce a draw from the joint posterior  $(f, \sigma)|(x, y)$  in the numeric y case and just f in the binary y case.

Thus, unlike a lot of other modelling methods in R, we do not produce a single model object from which fits and summaries may be extracted. The output consists of values  $f^*(x)$  (and  $\sigma^*$  in the numeric case) where \* denotes a particular draw. The x is either a row from the training data (x.train) or the test data (x.test).

#### Value

mc.lbart returns an object of type lbart which is essentially a list.

yhat.train A matrix with ndpost rows and nrow(x.train) columns. Each row corresponds

to a draw  $f^*$  from the posterior of f and each column corresponds to a row of x.train. The (i,j) value is  $f^*(x)$  for the  $i^{th}$  kept draw of f and the  $j^{th}$  row of

x.train.

Burn-in is dropped.

yhat.test Same as yhat.train but now the x's are the rows of the test data.

yhat.train.mean

train data fits = mean of yhat.train columns.

yhat.test.mean test data fits = mean of yhat.test columns.

varcount a matrix with ndpost rows and nrow(x.train) columns. Each row is for a draw.

For each variable (corresponding to the columns), the total count of the number of times that variable is used in a tree decision rule (over all trees) is given.

In addition, the list has a binaryOffset giving the value used.

Note that in the binary y, case yhat.train and yhat.test are f(x)+binaryOffset. If you want draws of the probability P(Y=1|x) you need to apply the Logistic cdf (plogis) to these values.

#### See Also

1bart

```
set.seed(99)
n=5000
x = sort(-2+4*runif(n))
X=matrix(x,ncol=1)
f = function(x) \{ return((1/2)*x^3) \}
FL = function(x) \{ return(exp(x)/(1+exp(x))) \}
pv = FL(f(x))
y = rbinom(n, 1, pv)
np=100
xp=-2+4*(1:np)/np
Xp=matrix(xp,ncol=1)
## parallel::mcparallel/mccollect do not exist on windows
## if(.Platform$OS.type=='unix') {
## ##test BART with token run to ensure installation works
       mf = mc.lbart(X, y, nskip=5, ndpost=5, mc.cores=1, seed=99)
##
## }
## Not run:
set.seed(99)
pf = lbart(X,y,Xp)
plot(f(Xp), pf\$yhat.test.mean, xlim=c(-4, 4), ylim=c(-4, 4),
```

```
xlab='True f(x)', ylab='BART f(x)')
lines(c(-4, 4), c(-4, 4))
mf = mc.lbart(X,y,Xp, mc.cores=4, seed=99)
plot(f(Xp), mf\$yhat.test.mean, xlim=c(-4, 4), ylim=c(-4, 4),
     xlab='True f(x)', ylab='BART f(x)')
lines(c(-4, 4), c(-4, 4))
par(mfrow=c(2,2))
plot(range(xp),range(pf$yhat.test),xlab='x',ylab='f(x)',type='n')
lines(x,f(x),col='blue',lwd=2)
lines(xp,apply(pf$yhat.test,2,mean),col='red')
qpl = apply(pf$yhat.test,2,quantile,probs=c(.025,.975))
lines(xp,qpl[1,],col='green',lty=1)
lines(xp,qpl[2,],col='green',lty=1)
title(main='BART::lbart f(x) with 0.95 intervals')
plot(range(xp),range(mf$yhat.test),xlab='x',ylab='f(x)',type='n')
lines(x,f(x),col='blue',lwd=2)
lines(xp,apply(mf$yhat.test,2,mean),col='red')
qpl = apply(mf$yhat.test,2,quantile,probs=c(.025,.975))
lines(xp,qpl[1,],col='green',lty=1)
lines(xp,qpl[2,],col='green',lty=1)
title(main='BART::mc.lbart f(x) with 0.95 intervals')
plot(pf$yhat.test.mean,apply(mf$yhat.test,2,mean),xlab='BART::lbart',ylab='BART::mc.lbart')
abline(0,1,col='red')
title(main="BART::lbart f(x) vs. BART::mc.lbart f(x)")
## End(Not run)
```

mc.pbart

Probit BART for dichotomous outcomes with Normal latents and parallel computation

#### **Description**

BART is a Bayesian "sum-of-trees" model.

For a binary response y, P(Y=1|x)=F(f(x)), where F denotes the standard normal cdf (probit link).

In both cases, f is the sum of many tree models. The goal is to have very flexible inference for the uknown function f.

In the spirit of "ensemble models", each tree is constrained by a prior to be a weak learner so that it contributes a small amount to the overall fit.

#### Usage

```
mc.pbart(
    x.train, y.train, x.test=matrix(0.0,0,0),
    sparse=FALSE, theta=0, omega=1,
    a=0.5, b=1, augment=FALSE, rho=NULL,
    xinfo=matrix(0.0,0,0), usequants=FALSE,
    cont=FALSE, rm.const=TRUE,
    k=2.0, power=2.0, base=.95,
    binaryOffset=NULL,
    ntree=50L, numcut=100L,
    ndpost=1000L, nskip=100L,
    keepevery=1L, printevery=100,
    keeptrainfits=TRUE, transposed=FALSE,
    mc.cores = 2L, nice = 19L,
    seed = 99L
)
```

## **Arguments**

x.train Explanatory variables for training (in sample) data.

May be a matrix or a data frame, with (as usual) rows corresponding to obser-

vations and columns to variables.

If a variable is a factor in a data frame, it is replaced with dummies. Note that q dummies are created if q>2 and one dummy is created if q=2, where q is the number of levels of the factor. pbart will generate draws of f(x) for each x which is a row of x.train.

which is a fow of x.train.

y.train Binary dependent variable for training (in sample) data.

x. test Explanatory variables for test (out of sample) data.

Should have same structure as x.train.

pbart will generate draws of f(x) for each x which is a row of x.test.

sparse Whether to perform variable selection based on a sparse Dirichlet prior rather

than simply uniform; see Linero 2016.

theta Set *theta* parameter; zero means random.

omega Set *omega* parameter; zero means random.

a Sparse parameter for Beta(a,b) prior:  $0.5 \le a \le 1$  where lower values

inducing more sparsity.

b Sparse parameter for Beta(a, b) prior; typically, b = 1.

rho Sparse parameter: typically rho = p where p is the number of covariates under

consideration.

augment Whether data augmentation is to be performed in sparse variable selection.

xinfo You can provide the cutpoints to BART or let BART choose them for you. To

provide them, use the xinfo argument to specify a list (matrix) where the items (rows) are the covariates and the contents of the items (columns) are the cut-

points.

usequants If usequants=FALSE, then the cutpoints in xinfo are generated uniformly; oth-

erwise, if TRUE, uniform quantiles are used for the cutpoints.

cont Whether or not to assume all variables are continuous.

rm. const Whether or not to remove constant variables.

k For binary y, k is the number of prior standard deviations f(x) is away from

+/-3. The bigger k is, the more conservative the fitting will be.

power Power parameter for tree prior.

base Base parameter for tree prior.

binaryOffset Used for binary y.

The model is P(Y = 1|x) = F(f(x) + binaryOffset).

ntree The number of trees in the sum.

numcut The number of possible values of c (see usequants). If a single number if given,

this is used for all variables. Otherwise a vector with length equal to ncol(x.train) is required, where the  $i^{th}$  element gives the number of c used for the  $i^{th}$  variable in x.train. If usequants is false, numcut equally spaced cutoffs are used covering the range of values in the corresponding column of x.train. If usequants is true, then min(numcut, the number of unique values in the corresponding columns of

x.train - 1) c values are used.

ndpost The number of posterior draws returned.

nskip Number of MCMC iterations to be treated as burn in. keepevery Every keepevery draw is kept to be returned to the user.

printevery As the MCMC runs, a message is printed every printevery draws.

keeptrainfits Whether to keep yhat.train or not.

transposed When running pbart in parallel, it is more memory-efficient to transpose x.train

and x. test, if any, prior to calling mc.pbart.

seed Setting the seed required for reproducible MCMC.

mc. cores Number of cores to employ in parallel.

nice Set the job niceness. The default niceness is 19: niceness goes from 0 (highest)

to 19 (lowest).

#### **Details**

BART is an Bayesian MCMC method. At each MCMC interation, we produce a draw from f in the binary y case.

Thus, unlike a lot of other modelling methods in R, we do not produce a single model object from which fits and summaries may be extracted. The output consists of values  $f^*(x)$  where \* denotes a particular draw. The x is either a row from the training data (x.train) or the test data (x.test).

#### Value

mc.pbart returns an object of type pbart which is essentially a list.

yhat.train A matrix with ndpost rows and nrow(x.train) columns. Each row corresponds

to a draw  $f^*$  from the posterior of f and each column corresponds to a row of x.train. The (i,j) value is  $f^*(x)$  for the  $i^{th}$  kept draw of f and the  $j^{th}$  row of

x.train.

Burn-in is dropped.

yhat.test Same as yhat.train but now the x's are the rows of the test data.

varcount a matrix with ndpost rows and nrow(x.train) columns. Each row is for a draw.

For each variable (corresponding to the columns), the total count of the number of times that variable is used in a tree decision rule (over all trees) is given.

In addition the list has a binaryOffset component giving the value used.

Note that in the binary y, case yhat.train and yhat.test are f(x) + binaryOffset. If you want draws of the probability P(Y=1|x) you need to apply the normal cdf (pnorm) to these values.

#### See Also

pbart

```
set.seed(99)
n=5000
x = sort(-2+4*runif(n))
X=matrix(x,ncol=1)
f = function(x) \{return((1/2)*x^3)\}
FL = function(x) \{ return(exp(x)/(1+exp(x))) \}
pv = FL(f(x))
y = rbinom(n, 1, pv)
np=100
xp=-2+4*(1:np)/np
Xp=matrix(xp,ncol=1)
## parallel::mcparallel/mccollect do not exist on windows
if(.Platform$OS.type=='unix') {
##test BART with token run to ensure installation works
   mf = mc.pbart(X, y, nskip=5, ndpost=5, mc.cores=1, seed=99)
}
## Not run:
set.seed(99)
pf = pbart(X, y, Xp)
## plot(f(Xp), pf$yhat.test.mean, xlim=c(-4, 4), ylim=c(-4, 4),
        xlab='True f(x)', ylab='BART f(x)')
## lines(c(-4, 4), c(-4, 4))
mf = mc.pbart(X,y,Xp, mc.cores=4, seed=99)
## plot(f(Xp), mf$yhat.test.mean, xlim=c(-4, 4), ylim=c(-4, 4),
        xlab='True f(x)', ylab='BART f(x)')
## lines(c(-4, 4), c(-4, 4))
```

```
par(mfrow=c(2,2))
plot(range(xp),range(pf$yhat.test),xlab='x',ylab='f(x)',type='n')
lines(x,f(x),col='blue',lwd=2)
lines(xp,apply(pf$yhat.test,2,mean),col='red')
qpl = apply(pf$yhat.test,2,quantile,probs=c(.025,.975))
lines(xp,qpl[1,],col='green',lty=1)
lines(xp,qp1[2,],col='green',lty=1)
title(main='BART::pbart f(x) with 0.95 intervals')
plot(range(xp),range(mf$yhat.test),xlab='x',ylab='f(x)',type='n')
lines(x,f(x),col='blue',lwd=2)
lines(xp,apply(mf$yhat.test,2,mean),col='red')
qpl = apply(mf$yhat.test,2,quantile,probs=c(.025,.975))
lines(xp,qpl[1,],col='green',lty=1)
lines(xp,qp1[2,],col='green',lty=1)
title(main='BART::mc.pbart f(x) with 0.95 intervals')
## plot(pf$yhat.test.mean,apply(mf$yhat.test,2,mean),xlab='BART::pbart',ylab='BART::mc.pbart')
## abline(0,1,col='red')
## title(main="BART::pbart f(x) vs. BART::mc.pbart f(x)")
## End(Not run)
```

mc.surv.pwbart

Predicting new observations with a previously fitted BART model

## **Description**

```
BART is a Bayesian "sum-of-trees" model. For a numeric response y, we have y=f(x)+\epsilon, where \epsilon\sim N(0,\sigma^2).
```

f is the sum of many tree models. The goal is to have very flexible inference for the uknown function f.

In the spirit of "ensemble models", each tree is constrained by a prior to be a weak learner so that it contributes a small amount to the overall fit.

## Usage

#### Arguments

x.test Matrix of covariates to predict y for.

binaryOffset Mean to add on to y prediction.

treedraws \$treedraws returned from surv.bart, mc.surv.bart, recur.bart or mc.recur.bart.

mc.cores Number of threads to utilize.

type Whether to employ Albert-Chib, 'pbart', or Holmes-Held, 'lbart'.

transposed When running pwbart or mc.pwbart in parallel, it is more memory-efficient to

transpose x. test prior to calling the internal versions of these functions.

nice Set the job niceness. The default niceness is 19: niceness goes from 0 (highest)

to 19 (lowest).

#### **Details**

BART is an Bayesian MCMC method. At each MCMC interation, we produce a draw from the joint posterior  $(f, \sigma)|(x, y)$  in the numeric y case and just f in the binary y case.

Thus, unlike a lot of other modelling methods in R, we do not produce a single model object from which fits and summaries may be extracted. The output consists of values  $f^*(x)$  (and  $\sigma^*$  in the numeric case) where \* denotes a particular draw. The x is either a row from the training data (x.train) or the test data (x.test).

#### Value

Returns an object of type survbart which is essentially a list with components:

yhat.test A matrix with ndpost rows and nrow(x.test) columns. Each row corresponds to a draw  $f^*$  from the posterior of f and each column corresponds to a row of

x.train. The (i,j) value is  $f^*(x)$  for the  $i^{th}$  kept draw of f and the  $j^{th}$  row of x.train.

Burn-in is dropped.

surv.test test data fits for survival probability: not available for mc.recur.pwbart.

surv.test.mean mean of surv.test over the posterior samples: not available for mc.recur.pwbart.

haz.test test data fits for hazard: available for mc.recur.pwbart only.

haz.test.mean mean of haz.test over the posterior samples: available for mc.recur.pwbart

only

cum.test test data fits for cumulative hazard: available for mc.recur.pwbart only.

cum.test.mean mean of cum.test over the posterior samples: available for mc.recur.pwbart

only.

#### See Also

#### pwbart

```
## load the advanced lung cancer example
data(lung)
group <- -which(is.na(lung[ , 7])) ## remove missing row for ph.karno</pre>
times <- lung[group, 2] ##lung$time</pre>
delta <- lung[group, 3]-1 ##lung$status: 1=censored, 2=dead</pre>
                           ##delta: 0=censored, 1=dead
## this study reports time in days rather than months like other studies
## coarsening from days to months will reduce the computational burden
times <- ceiling(times/30)</pre>
summary(times)
table(delta)
x.train <- as.matrix(lung[group, c(4, 5, 7)]) ## matrix of observed covariates
## lung$age:
                    Age in years
## lung$sex:
                    Male=1 Female=2
## lung$ph.karno: Karnofsky performance score (dead=0:normal=100:by=10)
                    rated by physician
dimnames(x.train)[[2]] \leftarrow c('age(yr)', 'M(1):F(2)', 'ph.karno(0:100:10)')
summary(x.train[ , 1])
table(x.train[ , 2])
table(x.train[ , 3])
x.test <- matrix(nrow=84, ncol=3) ## matrix of covariate scenarios
dimnames(x.test)[[2]] <- dimnames(x.train)[[2]]</pre>
```

```
i <- 1
for(age in 5*(9:15)) for(sex in 1:2) for(ph.karno in 10*(5:10)) {
    x.test[i, ] <- c(age, sex, ph.karno)</pre>
    i <- i+1
}
## this x.test is relatively small, but often you will want to
## predict for a large x.test matrix which may cause problems
## due to consumption of RAM so we can predict separately
## mcparallel/mccollect do not exist on windows
if(.Platform$OS.type=='unix') {
##test BART with token run to ensure installation works
    set.seed(99)
  post <- surv.bart(x.train=x.train, times=times, delta=delta, nskip=5, ndpost=5, keepevery=1)</pre>
    pre <- surv.pre.bart(x.train=x.train, times=times, delta=delta, x.test=x.test)</pre>
    pred <- mc.surv.pwbart(pre$tx.test, post$treedraws, post$binaryOffset)</pre>
}
## Not run:
## run one long MCMC chain in one process
set.seed(99)
post <- surv.bart(x.train=x.train, times=times, delta=delta)</pre>
## run "mc.cores" number of shorter MCMC chains in parallel processes
## post <- mc.surv.bart(x.train=x.train, times=times, delta=delta,</pre>
##
                        mc.cores=8, seed=99)
pre <- surv.pre.bart(x.train=x.train, times=times, delta=delta, x.test=x.test)</pre>
pred <- surv.pwbart(pre$tx.test, post$treedraws, post$binaryOffset)</pre>
## let's look at some survival curves
## first, a younger group with a healthier KPS
## age 50 with KPS=90: males and females
## males: row 17, females: row 23
x.test[c(17, 23), ]
low.risk.males <- 16*post$K+1:post$K ## K=unique times including censoring
low.risk.females <- 22*post$K+1:post$K</pre>
plot(post$times, pred$surv.test.mean[low.risk.males], type='s', col='blue',
     main='Age 50 with KPS=90', xlab='t', ylab='S(t)', ylim=c(0, 1))
points(post$times, pred$surv.test.mean[low.risk.females], type='s', col='red')
## End(Not run)
```

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mc.wbart

BART for continuous outcomes with parallel computation

## **Description**

```
BART is a Bayesian "sum-of-trees" model. For numeric response y, we have y = f(x) + \epsilon, where \epsilon \sim N(0, \sigma^2).
```

In both cases, f is the sum of many tree models. The goal is to have very flexible inference for the uknown function f.

In the spirit of "ensemble models", each tree is constrained by a prior to be a weak learner so that it contributes a small amount to the overall fit.

## Usage

```
mc.wbart(
   x.train, y.train, x.test=matrix(0.0,0,0),
   sparse=FALSE, theta=0, omega=1,
   a=0.5, b=1, augment=FALSE, rho=NULL,
   xinfo=matrix(0.0,0,0), usequants=FALSE,
   cont=FALSE, rm.const=TRUE,
   sigest=NA, sigdf=3, sigquant=0.90,
   k=2.0, power=2.0, base=.95,
   sigmaf=NA, lambda=NA, fmean=mean(y.train),
   w=rep(1,length(y.train)),
   ntree=200L, numcut=100L,
   ndpost=1000L, nskip=100L,
   keepevery=1L, printevery=100,
   keeptrainfits=TRUE, transposed=FALSE,
   mc.cores = 2L, nice = 19L,
   seed = 99L
)
```

## Arguments

x.train

Explanatory variables for training (in sample) data.

May be a matrix or a data frame, with (as usual) rows corresponding to observations and columns to variables.

If a variable is a factor in a data frame, it is replaced with dummies. Note that q dummies are created if q>2 and one dummy is created if q=2, where q is the number of levels of the factor. whart will generate draws of f(x) for each x which is a row of x.train.

y.train

Dependent variable for training (in sample) data.

If y is numeric a continous response model is fit (normal errors).

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x.test Explanatory variables for test (out of sample) data.

Should have same structure as x.train.

wbart will generate draws of f(x) for each x which is a row of x.test.

sparse Whether to perform variable selection based on a sparse Dirichlet prior rather

than simply uniform; see Linero 2016.

theta Set *theta* parameter; zero means random.

omega Set *omega* parameter; zero means random.

Sparse parameter for Beta(a,b) prior:  $0.5 \le a \le 1$  where lower values

inducing more sparsity.

b Sparse parameter for Beta(a, b) prior; typically, b = 1.

rho Sparse parameter: typically rho = p where p is the number of covariates under

consideration.

augment Whether data augmentation is to be performed in sparse variable selection.

xinfo You can provide the cutpoints to BART or let BART choose them for you. To

provide them, use the xinfo argument to specify a list (matrix) where the items (rows) are the covariates and the contents of the items (columns) are the cut-

points.

usequants If usequants=FALSE, then the cutpoints in xinfo are generated uniformly; oth-

erwise, if TRUE, uniform quantiles are used for the cutpoints.

cont Whether or not to assume all variables are continuous.

rm. const Whether or not to remove constant variables.

signst The prior for the error variance ( $\sigma^2$ ) is inverted chi-squared (the standard con-

ditionally conjugate prior). The prior is specified by choosing the degrees of freedom, a rough estimate of the corresponding standard deviation and a quantile to put this rough estimate at. If sigest=NA then the rough estimate will be the usual least squares estimator. Otherwise the supplied value will be used.

sigdf Degrees of freedom for error variance prior.

sigguant The quantile of the prior that the rough estimate (see sigest) is placed at. The

closer the quantile is to 1, the more aggresive the fit will be as you are putting more prior weight on error standard deviations  $(\sigma)$  less than the rough estimate.

k For numeric y, k is the number of prior standard deviations E(Y|x) = f(x) is

away from +/-.5. The bigger k is, the more conservative the fitting will be.

power Power parameter for tree prior.

base Base parameter for tree prior.

sigmaf The SD of f.

lambda The scale of the prior for the variance.

fmean BART operates on y.train centered by fmean.

w Vector of weights which multiply the variance.

ntree The number of trees in the sum.

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numcut The number of possible values of c (see usequants). If a single number if given,

this is used for all variables. Otherwise a vector with length equal to ncol(x.train) is required, where the  $i^{th}$  element gives the number of c used for the  $i^{th}$  variable in x.train. If usequants is false, numcut equally spaced cutoffs are used covering the range of values in the corresponding column of x.train. If usequants is true, then min(numcut, the number of unique values in the corresponding columns of

x.train - 1) c values are used.

ndpost The number of posterior draws returned.

nskip Number of MCMC iterations to be treated as burn in. keepevery Every keepevery draw is kept to be returned to the user.

printevery As the MCMC runs, a message is printed every printevery draws.

keeptrainfits Whether to keep yhat.train or not.

transposed When running wbart in parallel, it is more memory-efficient to transpose x.train

and x.test, if any, prior to calling mc.wbart.

seed Setting the seed required for reproducible MCMC.

mc.cores Number of cores to employ in parallel.

nice Set the job niceness. The default niceness is 19: niceness goes from 0 (highest)

to 19 (lowest).

#### **Details**

BART is an Bayesian MCMC method. At each MCMC interation, we produce a draw from the joint posterior  $(f, \sigma)|(x, y)$  in the numeric y case.

Thus, unlike a lot of other modelling methods in R, we do not produce a single model object from which fits and summaries may be extracted. The output consists of values  $f^*(x)$  (and  $\sigma^*$  in the numeric case) where \* denotes a particular draw. The x is either a row from the training data (x.train) or the test data (x.test).

### Value

mc. wbart returns an object of type wbart which is essentially a list.

yhat.train A matrix with ndpost rows and nrow(x.train) columns. Each row corresponds

to a draw  $f^*$  from the posterior of f and each column corresponds to a row of x.train. The (i,j) value is  $f^*(x)$  for the  $i^{th}$  kept draw of f and the  $j^{th}$  row of

x.train.

Burn-in is dropped.

yhat.test Same as yhat.train but now the x's are the rows of the test data.

yhat.train.mean

train data fits = mean of yhat.train columns.

yhat.test.mean test data fits = mean of yhat.test columns.

varcount a matrix with ndpost rows and nrow(x.train) columns. Each row is for a draw.

For each variable (corresponding to the columns), the total count of the number of times that variable is used in a tree decision rule (over all trees) is given.

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## See Also

wbart

### **Examples**

```
##simulate data (example from Friedman MARS paper)
f = function(x){
10*sin(pi*x[,1]*x[,2]) + 20*(x[,3]-.5)^2+10*x[,4]+5*x[,5]
sigma = 1.0 \# y = f(x) + sigma*z , z^N(0,1)
n = 100
             #number of observations
set.seed(99)
x=matrix(runif(n*10),n,10) #10 variables, only first 5 matter
Ey = f(x)
y=Ey+sigma*rnorm(n)
lmFit = lm(y^{-}, data.frame(x,y)) #compare lm fit to BART later
## parallel::mcparallel/mccollect do not exist on windows
if(.Platform$OS.type=='unix') {
##test BART with token run to ensure installation works
    bartFit = mc.wbart(x,y,mc.cores=2,seed=99,nskip=5,ndpost=5)
}
## Not run:
##run BART
bartFit = mc.wbart(x,y,mc.cores=5,seed=99)
##compare BART fit to linear matter and truth = Ey
fitmat = cbind(y,Ey,lmFit$fitted,bartFit$yhat.train.mean)
colnames(fitmat) = c('y', 'Ey', 'lm', 'bart')
print(cor(fitmat))
## End(Not run)
```

mc.wbart.gse

Global SE variable selection for BART with parallel computation

## **Description**

Here we implement the global SE method for variable selection in nonparametric survival analysis with BART. Unfortunately, the method is very computationally intensive so we present some trade-offs below.

# Usage

mc.wbart.gse 77

```
seed=99L, mc.cores=2L, nice=19L
)
```

## Arguments

x. train Explanatory variables for training (in sample) data.

Must be a matrix with (as usual) rows corresponding to observations and columns

to variables.

surv.bart will generate draws of f(t, x) for each x which is a row of x.train.

y.train The continuous outcome.

P The number of permutations: typically 50 or 100.

R The number of replicates: typically 5 or 10.

ntree The number of trees. In variable selection, the number of trees is smaller than

what might be used for the best fit.

numcut The number of possible values of c (see usequants). If a single number if given,

this is used for all variables. Otherwise a vector with length equal to ncol(x.train) is required, where the  $i^{th}$  element gives the number of c used for the  $i^{th}$  variable in x.train. If usequants is false, numcut equally spaced cutoffs are used covering the range of values in the corresponding column of x.train. If usequants is true, then min(numcut, the number of unique values in the corresponding columns of

x.train - 1) c values are used.

C The starting value for the multiple of SE. You should not need to change this

except in rare circumstances.

alpha The global SE method relies on simultaneous 1-alpha coverage across the per-

mutations for all predictor variables.

k k is the number of prior standard deviations f(t,x) is away from +/-3. The

bigger k is, the more conservative the fitting will be.

power Power parameter for tree prior.

Base parameter for tree prior.

ndpost The number of posterior draws after burn in. In the global SE method, generally,

the method is repeated several times to establish the variable count probabilities. However, we take the alternative approach of simply running the MCMC chain longer which should result in the same stabilization of the estimates. Therefore, the number of posterior draws in variable selection should be set to a larger value

than would be typically anticipated for fitting.

nskip Number of MCMC iterations to be treated as burn in.

printevery As the MCMC runs, a message is printed every printevery draws.

keepevery Every keepevery draw is kept.

keeptrainfits If TRUE the draws of f(t, x) for x = rows of x.train are generated.

seed seed required for reproducible MCMC.
mc.cores Number of cores to employ in parallel.

nice Set the job priority. The default priority is 19: priorities go from 0 (highest) to

19 (lowest).

## Value

```
mc.wbart.gse returns a list.
```

#### References

Bleich, J., Kapelner, A., George, E.I., and Jensen, S.T. (2014). Variable selection for BART: an application to gene regulation. *The Annals of Applied Statistics*, **8:1750-81**.

### See Also

```
mc.wbart
```

## **Examples**

```
## Not run:
library(ElemStatLearn)
data(phoneme)
x.train <- matrix(NA, nrow=4509, ncol=257)
dimnames(x.train)[[2]] <- c(paste0('x.', 1:256), 'speaker')
x.train[ , 257] <- as.numeric(phoneme$speaker)
for(j in 1:256) x.train[ , j] <- as.numeric(phoneme[ , paste0('x.', j)])
gse <- mc.wbart.gse(x.train, as.numeric(phoneme$g), mc.cores=5, seed=99)
## important variables
dimnames(x.train)[[2]][gse$which]
## End(Not run)</pre>
```

pbart

Probit BART for dichotomous outcomes with Normal latents

## **Description**

BART is a Bayesian "sum-of-trees" model.

For a binary response y, P(Y = 1|x) = F(f(x)), where F denotes the standard Normal CDF (probit link).

In both cases, f is the sum of many tree models. The goal is to have very flexible inference for the uknown function f.

In the spirit of "ensemble models", each tree is constrained by a prior to be a weak learner so that it contributes a small amount to the overall fit.

## Usage

```
pbart(
    x.train, y.train, x.test=matrix(0.0,0,0),
    sparse=FALSE, theta=0, omega=1,
    a=0.5, b=1, augment=FALSE, rho=NULL,
    xinfo=matrix(0.0,0,0), usequants=FALSE,
    cont=FALSE, rm.const=TRUE,
    k=2.0, power=2.0, base=.95,
    binaryOffset=NULL,
    ntree=50L, numcut=100L,
    ndpost=1000L, nskip=100L, keepevery=1L,
    nkeeptrain=ndpost, nkeeptest=ndpost,
    nkeeptreedraws=ndpost,
    printevery=100L, transposed=FALSE
)
```

## **Arguments**

x.train Explanatory variables for training (in sample) data.

May be a matrix or a data frame, with (as usual) rows corresponding to obser-

vations and columns to variables.

If a variable is a factor in a data frame, it is replaced with dummies. Note that q dummies are created if q>2 and one dummy is created if q=2, where q is the number of levels of the factor. pbart will generate draws of f(x) for each x which is a row of x.train.

y.train Binary dependent variable for training (in sample) data.

x.test Explanatory variables for test (out of sample) data.

Should have same structure as x.train.

pbart will generate draws of f(x) for each x which is a row of x.test.

sparse Whether to perform variable selection based on a sparse Dirichlet prior rather

than simply uniform; see Linero 2016.

theta Set *theta* parameter; zero means random.

omega Set omega parameter; zero means random.

a Sparse parameter for Beta(a,b) prior: 0.5 <= a <= 1 where lower values

inducing more sparsity.

b Sparse parameter for Beta(a, b) prior; typically, b = 1.

rho Sparse parameter: typically rho = p where p is the number of covariates under

consideration.

augment Whether data augmentation is to be performed in sparse variable selection.

xinfo You can provide the cutpoints to BART or let BART choose them for you. To

provide them, use the xinfo argument to specify a list (matrix) where the items (rows) are the covariates and the contents of the items (columns) are the cut-

points.

usequants If usequants=FALSE, then the cutpoints in xinfo are generated uniformly; oth-

erwise, if TRUE, uniform quantiles are used for the cutpoints.

cont Whether or not to assume all variables are continuous.

rm. const Whether or not to remove constant variables.

k For binary y, k is the number of prior standard deviations f(x) is away from

+/-3. The bigger k is, the more conservative the fitting will be.

power Power parameter for tree prior.

base Base parameter for tree prior.

binaryOffset Used for binary y.

The model is P(Y = 1|x) = F(f(x) + binaryOffset).

ntree The number of trees in the sum.

numcut The number of possible values of c (see usequants). If a single number if given,

this is used for all variables. Otherwise a vector with length equal to ncol(x.train) is required, where the  $i^{th}$  element gives the number of c used for the  $i^{th}$  variable in x.train. If usequants is false, numcut equally spaced cutoffs are used covering the range of values in the corresponding column of x.train. If usequants is true, then min(numcut, the number of unique values in the corresponding columns of

x.train - 1) c values are used.

ndpost The number of posterior draws returned.

nskip Number of MCMC iterations to be treated as burn in.

Number of MCMC iterations to be returned for train data.

Number of MCMC iterations to be returned for test data.

Number of MCMC iterations to be returned for tree draws.

Number of MCMC iterations to be returned for tree draws.

Every keepevery draw is kept to be returned to the user.

printevery As the MCMC runs, a message is printed every printevery draws.

transposed When running pbart in parallel, it is more memory-efficient to transpose x.train

and x.test, if any, prior to calling mc.pbart.

## **Details**

BART is an Bayesian MCMC method. At each MCMC interation, we produce a draw from f in the binary y case.

Thus, unlike a lot of other modelling methods in R, we do not produce a single model object from which fits and summaries may be extracted. The output consists of values  $f^*(x)$  where \* denotes a particular draw. The x is either a row from the training data (x.train) or the test data (x.test).

### Value

pbart returns an object of type pbart which is essentially a list.

yhat.train A matrix with ndpost rows and nrow(x.train) columns. Each row corresponds

to a draw  $f^*$  from the posterior of f and each column corresponds to a row of x.train. The (i,j) value is  $f^*(x)$  for the  $i^{th}$  kept draw of f and the  $j^{th}$  row of

x.train.

Burn-in is dropped.

yhat. test Same as yhat.train but now the x's are the rows of the test data.

varcount a matrix with ndpost rows and nrow(x.train) columns. Each row is for a draw.

For each variable (corresponding to the columns), the total count of the number of times that variable is used in a tree decision rule (over all trees) is given.

In addition the list has a binaryOffset component giving the value used.

Note that in the binary y, case yhat.train and yhat.test are f(x) + binaryOffset. If you want draws of the probability P(Y=1|x) you need to apply the Normal CDF (pnorm) to these values.

### See Also

wbart

```
data(ACTG175)
## exclude those who do not have CD4 count at 96 weeks
ex <- is.na(ACTG175$cd496)
table(ex)
## inclusion criteria are CD4 counts between 200 and 500
ACTG175$cd40 <- min(500, max(250, ACTG175$cd40))
## calculate relative CD4 decline
y <- ((ACTG175$cd496-ACTG175$cd40)/ACTG175$cd40)[!ex]</pre>
summary(y)
## 0=failure, 1=success
y < -1*(y > -0.5)
## summarize CD4 outcomes
table(y, ACTG175$arms[!ex])
table(y, ACTG175$arms[!ex])/
    matrix(table(ACTG175$arms[!ex]), nrow=2, ncol=4, byrow=TRUE)
## drop unneeded and unwanted variables
## 1: 'pidnum' patient ID number
##14: 'str2' which will be handled by strat1 below
##15: 'strat' which will be handled by strat1-strat3 below
##17: 'treat' handled by arm0-arm3 below
##18: 'offtrt' indicator of off-treatment before 96 weeks
##20: 'cd420' CD4 T cell count at 20 weeks
##21: 'cd496' CD4 T cell count at 96 weeks
##22: 'r' missing CD4 T cell count at 96 weeks
##24: 'cd820' CD8 T cell count at 20 weeks
##25: 'cens' indicator of observing the event in days
##26: 'days' number of days until the primary endpoint
##27: 'arms' handled by arm0-arm3 below
train <- as.matrix(ACTG175)[!ex, -c(1, 14:15, 17, 18, 20:22, 24:27)]
train <- cbind(1*(ACTG175$strat[!ex]==1), 1*(ACTG175$strat[!ex]==2),</pre>
```

```
1*(ACTG175$strat[!ex]==3), train)
dimnames(train)[[2]][1:3] <- paste0('strat', 1:3)</pre>
train <- cbind(1*(ACTG175\$arms[!ex]==0), 1*(ACTG175\$arms[!ex]==1),
               1*(ACTG175$arms[!ex]==2), 1*(ACTG175$arms[!ex]==3), train)
dimnames(train)[[2]][1:4] \leftarrow paste0('arm', 0:3)
N <- nrow(train)
test0 <- train; test0[ , 1:4] <- 0; test0[ , 1] <- 1
test1 <- train; test1[ , 1:4] <- 0; test1[ , 2] <- 1
test2 <- train; test2[ , 1:4] <- 0; test2[ , 3] <- 1
test3 <- train; test3[ , 1:4] <- 0; test3[ , 4] <- 1
test <- rbind(test0, test1, test2, test3)</pre>
##test BART with token run to ensure installation works
set.seed(21)
post <- pbart(train, y, test, nskip=5, ndpost=5)</pre>
## Not run:
set.seed(21)
post <- pbart(train, y, test)</pre>
## turn z-scores into probabilities
post$prob.test <- pnorm(post$yhat.test)</pre>
## average over the posterior samples
post$prob.test.mean <- apply(post$prob.test, 2, mean)</pre>
## place estimates for arms 0-3 next to each other for convenience
itr <- cbind(post$prob.test.mean[(1:N)], post$prob.test.mean[N+(1:N)],</pre>
             post$prob.test.mean[2*N+(1:N)], post$prob.test.mean[3*N+(1:N)])
## find the BART ITR for each patient
itr.pick <- integer(N)</pre>
for(i in 1:N) itr.pick[i] <- which(itr[i, ]==max(itr[i, ]))-1</pre>
## arms 0 and 3 (monotherapy) are never chosen
table(itr.pick)
## do arms 1 and 2 show treatment heterogeneity?
\label{limits} diff. <- apply(post\$prob.test[ \ , \ 2*N+(1:N)]-post\$prob.test[ \ , \ N+(1:N)], \ 2, \ mean)
plot(sort(diff.), type='h', main='ACTG175 trial: 50% CD4 decline from baseline at 96 weeks',
     xlab='Arm 2 (1) Preferable to the Right (Left)', ylab='Prob.Diff.: Arms 2 - 1')
library(rpart)
library(rpart.plot)
## make data frame for nicer names in the plot
var <- as.data.frame(train[ , -(1:4)])</pre>
dss <- rpart(diff. ~ var$age+var$gender+var$race+var$wtkg+var$cd40+var$cd80+
                    var$karnof+var$symptom+var$hemo+var$homo+var$drugs+var$z30+
```

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```
var$zprior+var$oprior+var$strat1+var$strat2+var$strat3,
               method='anova', control=rpart.control(cp=0.1))
rpart.plot(dss, type=3, extra=101)
## if strat1==1 (antiretroviral naive), then arm 2 is better
## otherwise, arm 1
print(dss)
all0 <- apply(post$prob.test[ , (1:N)], 1, mean)</pre>
all1 <- apply(post$prob.test[ , N+(1:N)], 1, mean)</pre>
all2 <- apply(postprob.test[ , 2*N+(1:N)], 1, mean)
all3 <- apply(postprob.test[, 3*N+(1:N)], 1, mean)
BART.itr <- apply(post$prob.test[, c(N+which(itr.pick==1), 2*N+which(itr.pick==2))], 1, mean)
test <- train
test[ , 1:4] <- 0
test[test[ , 5]==0, 2] <- 1
test[test[ , 5]==1, 3] <- 1
## BART ITR simple
BART.itr.simp <- pwbart(test, post$treedraws)</pre>
BART.itr.simp <- apply(pnorm(BART.itr.simp), 1, mean)</pre>
plot(density(BART.itr), xlab='Value', xlim=c(0.475, 0.775), lwd=2,
     main='ACTG175 trial: 50% CD4 decline from baseline at 96 weeks')
lines(density(BART.itr.simp), col='brown', lwd=2)
lines(density(all0), col='green', lwd=2)
lines(density(all1), col='red', lwd=2)
lines(density(all2), col='blue', lwd=2)
lines(density(all3), col='yellow', lwd=2)
legend('topleft', legend=c('All Arm 0 (ZDV only)', 'All Arm 1 (ZDV+DDI)',
                            'All Arm 2 (ZDV+DDC)', 'All Arm 3 (DDI only)',
                            'BART ITR simple', 'BART ITR'),
       col=c('green', 'red', 'blue', 'yellow', 'brown', 'black'), lty=1, lwd=2)
## End(Not run)
```

predict.crisk2bart

Predicting new observations with a previously fitted BART model

# Description

```
BART is a Bayesian "sum-of-trees" model. For a numeric response y, we have y=f(x)+\epsilon, where \epsilon\sim N(0,\sigma^2).
```

f is the sum of many tree models. The goal is to have very flexible inference for the uknown function f.

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In the spirit of "ensemble models", each tree is constrained by a prior to be a weak learner so that it contributes a small amount to the overall fit.

### **Usage**

```
## S3 method for class 'crisk2bart'
predict(object, newdata, newdata2, mc.cores=1, openmp=(mc.cores.openmp()>0), ...)
```

## **Arguments**

object object returned from previous BART fit with crisk2.bart or mc.crisk2.bart. 
Matrix of covariates to predict the distribution of t1. 
Matrix of covariates to predict the distribution of t2. 
Mumber of threads to utilize. 
Openmp Logical value dictating whether OpenMP is utilized for parallel processing. Of course, this depends on whether OpenMP is available on your system which, by default, is verified with mc.cores.openmp.

Other arguments which will be passed on to pwbart.

#### **Details**

BART is an Bayesian MCMC method. At each MCMC interation, we produce a draw from the joint posterior  $(f, \sigma)|(x, y)$  in the numeric y case and just f in the binary y case.

Thus, unlike a lot of other modelling methods in R, we do not produce a single model object from which fits and summaries may be extracted. The output consists of values  $f^*(x)$  (and  $\sigma^*$  in the numeric case) where \* denotes a particular draw. The x is either a row from the training data (x.train) or the test data (x.test).

#### Value

Returns an object of type crisk2bart with predictions corresponding to newdata and newdata2.

### See Also

```
crisk2.bart, mc.crisk2.bart, mc.crisk2.pwbart, mc.cores.openmp
```

```
data(transplant)

delta <- (as.numeric(transplant$event)-1)
## recode so that delta=1 is cause of interest; delta=2 otherwise
delta[delta==1] <- 4
delta[delta==2] <- 1
delta[delta>1] <- 2
table(delta, transplant$event)

times <- pmax(1, ceiling(transplant$futime/7)) ## weeks
##times <- pmax(1, ceiling(transplant$futime/30.5)) ## months</pre>
```

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```
table(times)
type0 <- 1*(transplant$abo=='0')</pre>
typeA <- 1*(transplant$abo=='A')</pre>
typeB <- 1*(transplant$abo=='B')</pre>
typeAB <- 1*(transplant$abo=='AB')</pre>
table(typeA, type0)
x.train <- cbind(type0, typeA, typeB, typeAB)</pre>
x.test <- cbind(1, 0, 0, 0)
dimnames(x.test)[[2]] <- dimnames(x.train)[[2]]</pre>
## parallel::mcparallel/mccollect do not exist on windows
if(.Platform$OS.type=='unix') {
##test BART with token run to ensure installation works
        post <- mc.crisk2.bart(x.train=x.train, times=times, delta=delta,</pre>
                                 seed=99, mc.cores=2, nskip=5, ndpost=5,
                                 keepevery=1)
        pre <- surv.pre.bart(x.train=x.train, x.test=x.test,</pre>
                               times=times, delta=delta)
        K <- post$K
        pred <- mc.crisk2.pwbart(pre$tx.test, pre$tx.test,</pre>
                                  post$treedraws, post$treedraws2,
                                  post$binaryOffset, post$binaryOffset2)
}
## Not run:
## run one long MCMC chain in one process
## set.seed(99)
## post <- crisk2.bart(x.train=x.train, times=times, delta=delta, x.test=x.test)</pre>
## in the interest of time, consider speeding it up by parallel processing
## run "mc.cores" number of shorter MCMC chains in parallel processes
post <- mc.crisk2.bart(x.train=x.train,</pre>
                        times=times, delta=delta,
                        x.test=x.test, seed=99, mc.cores=8)
## check <- mc.crisk2.pwbart(post$tx.test, post$tx.test,</pre>
##
                              post$treedraws, post$treedraws2,
##
                              post$binaryOffset,
##
                              post$binaryOffset2, mc.cores=8)
check <- predict(post, newdata=post$tx.test, newdata2=post$tx.test2,</pre>
                  mc.cores=8)
print(c(post$surv.test.mean[1], check$surv.test.mean[1],
        post$surv.test.mean[1]-check$surv.test.mean[1]), digits=22)
print(all(round(post$surv.test.mean, digits=9)==
```

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predict.criskbart

Predicting new observations with a previously fitted BART model

# **Description**

```
BART is a Bayesian "sum-of-trees" model. For a numeric response y, we have y=f(x)+\epsilon, where \epsilon\sim N(0,\sigma^2).
```

f is the sum of many tree models. The goal is to have very flexible inference for the uknown function f.

In the spirit of "ensemble models", each tree is constrained by a prior to be a weak learner so that it contributes a small amount to the overall fit.

# Usage

```
## S3 method for class 'criskbart'
predict(object, newdata, newdata2, mc.cores=1, openmp=(mc.cores.openmp()>0), ...)
```

## **Arguments**

object	object returned from previous BART fit with ${\tt crisk.bart}$ or ${\tt mc.crisk.bart}$ .
newdata	Matrix of covariates to predict the distribution of $t1$ .
newdata2	Matrix of covariates to predict the distribution of $t2$ .
mc.cores	Number of threads to utilize.
openmp	Logical value dictating whether OpenMP is utilized for parallel processing. Of course, this depends on whether OpenMP is available on your system which, by default, is verified with mc.cores.openmp.
	Other arguments which will be passed on to pwbart.

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### **Details**

BART is an Bayesian MCMC method. At each MCMC interation, we produce a draw from the joint posterior  $(f, \sigma)|(x, y)$  in the numeric y case and just f in the binary y case.

Thus, unlike a lot of other modelling methods in R, we do not produce a single model object from which fits and summaries may be extracted. The output consists of values  $f^*(x)$  (and  $\sigma^*$  in the numeric case) where \* denotes a particular draw. The x is either a row from the training data (x.train) or the test data (x.test).

# Value

Returns an object of type criskbart with predictions corresponding to newdata and newdata2.

#### See Also

```
crisk.bart, mc.crisk.bart, mc.crisk.pwbart, mc.cores.openmp
```

```
data(transplant)
delta <- (as.numeric(transplant$event)-1)</pre>
## recode so that delta=1 is cause of interest; delta=2 otherwise
delta[delta==1] <- 4
delta[delta==2] <- 1
delta[delta>1] <- 2</pre>
table(delta, transplant$event)
times <- pmax(1, ceiling(transplant$futime/7)) ## weeks</pre>
##times <- pmax(1, ceiling(transplant$futime/30.5)) ## months</pre>
table(times)
type0 <- 1*(transplant$abo=='0')</pre>
typeA <- 1*(transplant$abo=='A')</pre>
typeB <- 1*(transplant$abo=='B')</pre>
typeAB <- 1*(transplant$abo=='AB')</pre>
table(typeA, type0)
x.train <- cbind(type0, typeA, typeB, typeAB)</pre>
x.test <- cbind(1, 0, 0, 0)
dimnames(x.test)[[2]] <- dimnames(x.train)[[2]]</pre>
## parallel::mcparallel/mccollect do not exist on windows
if(.Platform$OS.type=='unix') {
##test BART with token run to ensure installation works
        post <- mc.crisk.bart(x.train=x.train, times=times, delta=delta,</pre>
                                  seed=99, mc.cores=2, nskip=5, ndpost=5,
                                 keepevery=1)
        pre <- surv.pre.bart(x.train=x.train, x.test=x.test,</pre>
                               times=times, delta=delta)
```

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```
K <- post$K
        pred <- mc.crisk.pwbart(pre$tx.test, pre$tx.test,</pre>
                                 post$treedraws, post$treedraws2,
                                 post$binaryOffset, post$binaryOffset2)
}
## Not run:
## run one long MCMC chain in one process
## set.seed(99)
## post <- crisk.bart(x.train=x.train, times=times, delta=delta, x.test=x.test)</pre>
## in the interest of time, consider speeding it up by parallel processing
## run "mc.cores" number of shorter MCMC chains in parallel processes
post <- mc.crisk.bart(x.train=x.train,</pre>
                       times=times, delta=delta,
                       x.test=x.test, seed=99, mc.cores=8)
## check <- mc.crisk.pwbart(post$tx.test, post$tx.test,</pre>
##
                              post$treedraws, post$treedraws2,
##
                              post$binaryOffset,
##
                             post$binaryOffset2, mc.cores=8)
\verb|check| <- predict(post, newdata=post$tx.test, newdata2=post$tx.test2|, \\
                 mc.cores=8)
print(c(post$surv.test.mean[1], check$surv.test.mean[1],
        post$surv.test.mean[1]-check$surv.test.mean[1]), digits=22)
print(all(round(post$surv.test.mean, digits=9)==
    round(check$surv.test.mean, digits=9)))
print(c(post$cif.test.mean[1], check$cif.test.mean[1],
        post$cif.test.mean[1]-check$cif.test.mean[1]), digits=22)
print(all(round(post$cif.test.mean, digits=9)==
    round(check$cif.test.mean, digits=9)))
print(c(post$cif.test2.mean[1], check$cif.test2.mean[1],
        post$cif.test2.mean[1]-check$cif.test2.mean[1]), digits=22)
print(all(round(post$cif.test2.mean, digits=9)==
    round(check$cif.test2.mean, digits=9)))
## End(Not run)
```

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## **Description**

```
BART is a Bayesian "sum-of-trees" model. For a numeric response y, we have y = f(x) + \epsilon, where \epsilon \sim N(0, \sigma^2).
```

f is the sum of many tree models. The goal is to have very flexible inference for the uknown function f.

In the spirit of "ensemble models", each tree is constrained by a prior to be a weak learner so that it contributes a small amount to the overall fit.

# Usage

```
## S3 method for class 'lbart'
predict(object, newdata, mc.cores=1, openmp=(mc.cores.openmp()>0), ...)
```

## **Arguments**

object returned from previous BART fit with surv.bart or mc.surv.bart.

newdata Matrix of covariates to predict the distribution of t.

mc.cores Number of threads to utilize.

openmp Logical value dictating whether OpenMP is utilized for parallel processing. Of

course, this depends on whether OpenMP is available on your system which, by

default, is verified with mc.cores.openmp.

Other arguments which will be passed on to pwbart.

## **Details**

BART is an Bayesian MCMC method. At each MCMC interation, we produce a draw from the joint posterior  $(f, \sigma)|(x, y)$  in the numeric y case and just f in the binary y case.

Thus, unlike a lot of other modelling methods in R, we do not produce a single model object from which fits and summaries may be extracted. The output consists of values  $f^*(x)$  (and  $\sigma^*$  in the numeric case) where \* denotes a particular draw. The x is either a row from the training data (x.train) or the test data (x.test).

## Value

Returns an object of type 1bart with predictions corresponding to newdata.

### See Also

```
surv.bart, mc.surv.bart, surv.pwbart, mc.surv.pwbart, mc.cores.openmp
```

```
## load the advanced lung cancer example
data(lung)
group <- -which(is.na(lung[ , 7])) ## remove missing row for ph.karno</pre>
```

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```
times <- lung[group, 2] ##lung$time</pre>
delta <- lung[group, 3]-1 ##lung$status: 1=censored, 2=dead</pre>
                           ##delta: 0=censored, 1=dead
## this study reports time in days rather than months like other studies
## coarsening from days to months will reduce the computational burden
times <- ceiling(times/30)</pre>
summary(times)
table(delta)
x.train <- as.matrix(lung[group, c(4, 5, 7)]) ## matrix of observed covariates
## lung$age:
                    Age in years
                    Male=1 Female=2
## lung$sex:
## lung$ph.karno: Karnofsky performance score (dead=0:normal=100:by=10)
##
                    rated by physician
dimnames(x.train)[[2]] <- c('age(yr)', 'M(1):F(2)', 'ph.karno(0:100:10)')</pre>
summary(x.train[ , 1])
table(x.train[ , 2])
table(x.train[ , 3])
x.test <- matrix(nrow=84, ncol=3) ## matrix of covariate scenarios</pre>
dimnames(x.test)[[2]] <- dimnames(x.train)[[2]]</pre>
i <- 1
for(age in 5*(9:15)) for(sex in 1:2) for(ph.karno in 10*(5:10)) {
    x.test[i, ] <- c(age, sex, ph.karno)</pre>
    i <- i+1
}
## this x.test is relatively small, but often you will want to
## predict for a large x.test matrix which may cause problems
## due to consumption of RAM so we can predict separately
## mcparallel/mccollect do not exist on windows
if(.Platform$OS.type=='unix') {
##test BART with token run to ensure installation works
    set.seed(99)
  post <- surv.bart(x.train=x.train, times=times, delta=delta, nskip=5, ndpost=5, keepevery=1)</pre>
    pre <- surv.pre.bart(x.train=x.train, times=times, delta=delta, x.test=x.test)</pre>
   pred <- predict(post, pre$tx.test)</pre>
    ##pred. <- surv.pwbart(pre$tx.test, post$treedraws, post$binaryOffset)</pre>
}
## Not run:
## run one long MCMC chain in one process
```

predict.mbart 91

```
set.seed(99)
post <- surv.bart(x.train=x.train, times=times, delta=delta)</pre>
## run "mc.cores" number of shorter MCMC chains in parallel processes
## post <- mc.surv.bart(x.train=x.train, times=times, delta=delta,</pre>
                        mc.cores=5, seed=99)
pre <- surv.pre.bart(x.train=x.train, times=times, delta=delta, x.test=x.test)</pre>
pred <- predict(post, pre$tx.test)</pre>
## let's look at some survival curves
## first, a younger group with a healthier KPS
## age 50 with KPS=90: males and females
## males: row 17, females: row 23
x.test[c(17, 23), ]
low.risk.males <- 16*post$K+1:post$K ## K=unique times including censoring</pre>
low.risk.females <- 22*post$K+1:post$K</pre>
plot(post$times, pred$surv.test.mean[low.risk.males], type='s', col='blue',
     main='Age 50 with KPS=90', xlab='t', ylab='S(t)', ylim=c(0, 1))
points(post$times, pred$surv.test.mean[low.risk.females], type='s', col='red')
## End(Not run)
```

predict.mbart

Predicting new observations with a previously fitted BART model

# Description

```
BART is a Bayesian "sum-of-trees" model. For a numeric response y, we have y = f(x) + \epsilon, where \epsilon \sim N(0, \sigma^2).
```

f is the sum of many tree models. The goal is to have very flexible inference for the uknown function f.

In the spirit of "ensemble models", each tree is constrained by a prior to be a weak learner so that it contributes a small amount to the overall fit.

# Usage

```
## S3 method for class 'mbart'
predict(object, newdata, mc.cores=1, openmp=(mc.cores.openmp()>0), ...)
## S3 method for class 'mbart2'
predict(object, newdata, mc.cores=1, openmp=(mc.cores.openmp()>0), ...)
```

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## Arguments

object object returned from previous BART fit with mbart or mbart2.

newdata Matrix of covariates to predict the distribution of t.

mc.cores Number of threads to utilize.

openmp Logical value dictating whether OpenMP is utilized for parallel processing. Of

course, this depends on whether OpenMP is available on your system which, by

default, is verified with mc.cores.openmp.

... Other arguments which will be passed on to pwbart.

#### **Details**

BART is an Bayesian MCMC method. At each MCMC interation, we produce a draw from the joint posterior  $(f, \sigma)|(x, y)$  in the numeric y case and just f in the binary y case.

Thus, unlike a lot of other modelling methods in R, we do not produce a single model object from which fits and summaries may be extracted. The output consists of values  $f^*(x)$  (and  $\sigma^*$  in the numeric case) where \* denotes a particular draw. The x is either a row from the training data (x.train) or the test data (x.test).

#### Value

Returns an object of type mbart with predictions corresponding to newdata.

#### See Also

```
mbart, mbart2
```

```
## load the advanced lung cancer example
data(lung)
group <- -which(is.na(lung[ , 7])) ## remove missing row for ph.karno</pre>
times <- lung[group, 2] ##lung$time</pre>
delta <- lung[group, 3]-1 ##lung$status: 1=censored, 2=dead</pre>
                           ##delta: 0=censored, 1=dead
## this study reports time in days rather than months like other studies
## coarsening from days to months will reduce the computational burden
times <- ceiling(times/30)</pre>
summary(times)
table(delta)
x.train <- as.matrix(lung[group, c(4, 5, 7)]) ## matrix of observed covariates
## lung$age:
                    Age in years
## lung$sex:
                    Male=1 Female=2
## lung$ph.karno: Karnofsky performance score (dead=0:normal=100:by=10)
##
                    rated by physician
```

predict.mbart 93

```
dimnames(x.train)[[2]] \leftarrow c('age(yr)', 'M(1):F(2)', 'ph.karno(0:100:10)')
summary(x.train[ , 1])
table(x.train[ , 2])
table(x.train[ , 3])
x.test <- matrix(nrow=84, ncol=3) ## matrix of covariate scenarios
dimnames(x.test)[[2]] <- dimnames(x.train)[[2]]</pre>
i <- 1
for(age in 5*(9:15)) for(sex in 1:2) for(ph.karno in 10*(5:10)) {
    x.test[i, ] <- c(age, sex, ph.karno)</pre>
    i <- i+1
}
## this x.test is relatively small, but often you will want to
## predict for a large x.test matrix which may cause problems
## due to consumption of RAM so we can predict separately
## mcparallel/mccollect do not exist on windows
if(.Platform$OS.type=='unix') {
##test BART with token run to ensure installation works
    set.seed(99)
  post <- surv.bart(x.train=x.train, times=times, delta=delta, nskip=5, ndpost=5, keepevery=1)</pre>
    pre <- surv.pre.bart(x.train=x.train, times=times, delta=delta, x.test=x.test)</pre>
    pred <- predict(post, pre$tx.test)</pre>
    ##pred. <- surv.pwbart(pre$tx.test, post$treedraws, post$binaryOffset)</pre>
}
## Not run:
## run one long MCMC chain in one process
set.seed(99)
post <- surv.bart(x.train=x.train, times=times, delta=delta)</pre>
## run "mc.cores" number of shorter MCMC chains in parallel processes
## post <- mc.surv.bart(x.train=x.train, times=times, delta=delta,</pre>
##
                         mc.cores=5, seed=99)
pre <- surv.pre.bart(x.train=x.train, times=times, delta=delta, x.test=x.test)</pre>
pred <- predict(post, pre$tx.test)</pre>
## let's look at some survival curves
## first, a younger group with a healthier KPS
## age 50 with KPS=90: males and females
## males: row 17, females: row 23
x.test[c(17, 23), ]
```

94 predict.pbart

predict.pbart

Predicting new observations with a previously fitted BART model

# Description

```
BART is a Bayesian "sum-of-trees" model. For a numeric response y, we have y=f(x)+\epsilon, where \epsilon \sim N(0,\sigma^2).
```

f is the sum of many tree models. The goal is to have very flexible inference for the uknown function f.

In the spirit of "ensemble models", each tree is constrained by a prior to be a weak learner so that it contributes a small amount to the overall fit.

### Usage

```
## S3 method for class 'pbart'
predict(object, newdata, mc.cores=1, openmp=(mc.cores.openmp()>0), ...)
```

# **Arguments**

object object returned from previous BART fit with surv.bart or mc.surv.bart.

Newdata Matrix of covariates to predict the distribution of t.

mc.cores Number of threads to utilize.

openmp Logical value dictating whether OpenMP is utilized for parallel processing. Of

course, this depends on whether OpenMP is available on your system which, by

default, is verified with mc.cores.openmp.

... Other arguments which will be passed on to pwbart.

### **Details**

BART is an Bayesian MCMC method. At each MCMC interation, we produce a draw from the joint posterior  $(f, \sigma)|(x, y)$  in the numeric y case and just f in the binary y case.

Thus, unlike a lot of other modelling methods in R, we do not produce a single model object from which fits and summaries may be extracted. The output consists of values  $f^*(x)$  (and  $\sigma^*$  in the numeric case) where \* denotes a particular draw. The x is either a row from the training data (x.train) or the test data (x.test).

predict.pbart 95

### Value

Returns an object of type pbart with predictions corresponding to newdata.

#### See Also

```
surv.bart, mc.surv.bart, surv.pwbart, mc.surv.pwbart, mc.cores.openmp
```

```
## load the advanced lung cancer example
data(lung)
group <- -which(is.na(lung[ , 7])) ## remove missing row for ph.karno</pre>
times <- lung[group, 2] ##lung$time</pre>
delta <- lung[group, 3]-1 ##lung$status: 1=censored, 2=dead</pre>
                           ##delta: 0=censored, 1=dead
## this study reports time in days rather than months like other studies
## coarsening from days to months will reduce the computational burden
times <- ceiling(times/30)</pre>
summary(times)
table(delta)
x.train <- as.matrix(lung[group, c(4, 5, 7)]) ## matrix of observed covariates
## lung$age:
                    Age in years
## lung$sex:
                   Male=1 Female=2
## lung$ph.karno: Karnofsky performance score (dead=0:normal=100:by=10)
                    rated by physician
dimnames(x.train)[[2]] \leftarrow c('age(yr)', 'M(1):F(2)', 'ph.karno(0:100:10)')
summary(x.train[ , 1])
table(x.train[ , 2])
table(x.train[ , 3])
x.test <- matrix(nrow=84, ncol=3) ## matrix of covariate scenarios
dimnames(x.test)[[2]] <- dimnames(x.train)[[2]]</pre>
i <- 1
for(age in 5*(9:15)) for(sex in 1:2) for(ph.karno in 10*(5:10)) {
    x.test[i, ] <- c(age, sex, ph.karno)</pre>
    i <- i+1
## this x.test is relatively small, but often you will want to
## predict for a large x.test matrix which may cause problems
## due to consumption of RAM so we can predict separately
```

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```
## mcparallel/mccollect do not exist on windows
if(.Platform$OS.type=='unix') {
##test BART with token run to ensure installation works
    set.seed(99)
   post <- surv.bart(x.train=x.train, times=times, delta=delta, nskip=5, ndpost=5, keepevery=1)</pre>
    pre <- surv.pre.bart(x.train=x.train, times=times, delta=delta, x.test=x.test)</pre>
    pred <- predict(post, pre$tx.test)</pre>
    ##pred. <- surv.pwbart(pre$tx.test, post$treedraws, post$binaryOffset)</pre>
}
## Not run:
## run one long MCMC chain in one process
set.seed(99)
post <- surv.bart(x.train=x.train, times=times, delta=delta)</pre>
## run "mc.cores" number of shorter MCMC chains in parallel processes
## post <- mc.surv.bart(x.train=x.train, times=times, delta=delta,</pre>
                         mc.cores=5, seed=99)
pre <- surv.pre.bart(x.train=x.train, times=times, delta=delta, x.test=x.test)</pre>
pred <- predict(post, pre$tx.test)</pre>
## let's look at some survival curves
## first, a younger group with a healthier KPS
## age 50 with KPS=90: males and females
## males: row 17, females: row 23
x.test[c(17, 23), ]
low.risk.males <- 16*post$K+1:post$K ## K=unique times including censoring</pre>
low.risk.females <- 22*post$K+1:post$K</pre>
plot(post$times, pred$surv.test.mean[low.risk.males], type='s', col='blue',
     main='Age 50 with KPS=90', xlab='t', ylab='S(t)', ylim=c(0, 1))
points(post$times, pred$surv.test.mean[low.risk.females], type='s', col='red')
## End(Not run)
```

predict.recurbart

Predicting new observations with a previously fitted BART model

## **Description**

```
BART is a Bayesian "sum-of-trees" model. For a numeric response y, we have y = f(x) + \epsilon, where \epsilon \sim N(0, \sigma^2).
```

predict.recurbart 97

f is the sum of many tree models. The goal is to have very flexible inference for the uknown function f.

In the spirit of "ensemble models", each tree is constrained by a prior to be a weak learner so that it contributes a small amount to the overall fit.

### **Usage**

```
## S3 method for class 'recurbart'
predict(object, newdata, mc.cores=1, openmp=(mc.cores.openmp()>0), ...)
```

## **Arguments**

object object returned from previous BART fit with recur.bart or mc.recur.bart.

newdata Matrix of covariates to predict the distribution of t.

mc.cores Number of threads to utilize.

openmp Logical value dictating whether OpenMP is utilized for parallel processing. Of

course, this depends on whether OpenMP is available on your system which, by

default, is verified with mc.cores.openmp.

. . . Other arguments which will be passed on to pwbart.

#### **Details**

BART is an Bayesian MCMC method. At each MCMC interation, we produce a draw from the joint posterior  $(f, \sigma)|(x, y)$  in the numeric y case and just f in the binary y case.

Thus, unlike a lot of other modelling methods in R, we do not produce a single model object from which fits and summaries may be extracted. The output consists of values  $f^*(x)$  (and  $\sigma^*$  in the numeric case) where \* denotes a particular draw. The x is either a row from the training data (x.train) or the test data (x.test).

### Value

Returns an object of type recurbart with predictions corresponding to newdata.

## See Also

```
recur.bart, mc.recur.bart, recur.pwbart, mc.recur.pwbart, mc.cores.openmp
```

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```
## Not run:
set.seed(99)
post <- recur.bart(x.train=xdm20.train, y.train=ydm20.train)</pre>
## larger data sets can take some time so, if parallel processing
## is available, submit this statement instead
## post <- mc.recur.bart(x.train=xdm20.train, y.train=ydm20.train,</pre>
                        mc.cores=8, seed=99)
require(rpart)
require(rpart.plot)
dss <- rpart(post$yhat.train.mean~xdm20.train)</pre>
rpart.plot(dss)
## for the 20 percent sample, notice that the top splits
## involve cci_pvd and n
## for the full data set, notice that all splits
## involve ca, cci_pud, cci_pvd, ins270 and n
## (except one at the bottom involving a small group)
## compare patients treated with insulin (ins270=1) vs
## not treated with insulin (ins270=0)
N.train <- 50
N.test <- 50
K <- post$K ## 798 unique time points
## only testing set, i.e., remove training set
xdm20.test. <- xdm20.test[N.train*K+(1:(N.test*K)), ]</pre>
xdm20.test. <- rbind(xdm20.test., xdm20.test.)</pre>
xdm20.test.[ , 'ins270'] <- rep(0:1, each=N.test*K)
## multiple threads will be utilized if available
pred <- predict(post, xdm20.test., mc.cores=8)</pre>
## create Friedman's partial dependence function for the
## intensity/hazard by time and ins270
NK.test <- N.test*K
M <- nrow(pred$haz.test) ## number of MCMC samples, typically 1000
RI <- matrix(0, M, K)
for(i in 1:N.test)
    RI \leftarrow RI+(pred\haz.test[ , (N.test+i-1)*K+1:K]/
              pred$haz.test[ , (i-1)*K+1:K])/N.test
RI.lo <- apply(RI, 2, quantile, probs=0.025)
RI.mu <- apply(RI, 2, mean)
RI.hi <- apply(RI, 2, quantile, probs=0.975)
plot(post$times, RI.hi, type='l', lty=2, log='y',
     ylim=c(min(RI.lo, 1/RI.hi), max(1/RI.lo, RI.hi)),
     xlab='t', ylab='RI(t, x)',
```

predict.survbart 99

```
sub='insulin(ins270=1) vs. no insulin(ins270=0)',
    main='Relative intensity of hospital admissions for diabetics')
lines(post$times, RI.mu)
lines(post$times, RI.lo, lty=2)
lines(post$times, rep(1, K), col='darkgray')

## RI for insulin therapy seems fairly constant with time
mean(RI.mu)

## End(Not run)
```

predict.survbart

Predicting new observations with a previously fitted BART model

# **Description**

```
BART is a Bayesian "sum-of-trees" model. For a numeric response y, we have y=f(x)+\epsilon, where \epsilon\sim N(0,\sigma^2).
```

f is the sum of many tree models. The goal is to have very flexible inference for the uknown function f.

In the spirit of "ensemble models", each tree is constrained by a prior to be a weak learner so that it contributes a small amount to the overall fit.

## Usage

```
## S3 method for class 'survbart'
predict(object, newdata, mc.cores=1, openmp=(mc.cores.openmp()>0), ...)
```

### Arguments

object object returned from previous BART fit with surv.bart or mc.surv.bart.

newdata Matrix of covariates to predict the distribution of t.

mc.cores Number of threads to utilize.

openmp Logical value dictating whether OpenMP is utilized for parallel processing. Of

course, this depends on whether OpenMP is available on your system which, by

default, is verified with mc.cores.openmp.

. . . Other arguments which will be passed on to pwbart.

### **Details**

BART is an Bayesian MCMC method. At each MCMC interation, we produce a draw from the joint posterior  $(f, \sigma)|(x, y)$  in the numeric y case and just f in the binary y case.

Thus, unlike a lot of other modelling methods in R, we do not produce a single model object from which fits and summaries may be extracted. The output consists of values  $f^*(x)$  (and  $\sigma^*$  in the numeric case) where \* denotes a particular draw. The x is either a row from the training data (x.train) or the test data (x.test).

100 predict.survbart

### Value

Returns an object of type survbart with predictions corresponding to newdata.

#### See Also

```
surv.bart, mc.surv.bart, surv.pwbart, mc.surv.pwbart, mc.cores.openmp
```

```
## load the advanced lung cancer example
data(lung)
group <- -which(is.na(lung[ , 7])) ## remove missing row for ph.karno</pre>
times <- lung[group, 2] ##lung$time</pre>
delta <- lung[group, 3]-1 ##lung$status: 1=censored, 2=dead</pre>
                           ##delta: 0=censored, 1=dead
## this study reports time in days rather than months like other studies
## coarsening from days to months will reduce the computational burden
times <- ceiling(times/30)</pre>
summary(times)
table(delta)
x.train <- as.matrix(lung[group, c(4, 5, 7)]) ## matrix of observed covariates
## lung$age:
                    Age in years
                    Male=1 Female=2
## lung$sex:
## lung$ph.karno: Karnofsky performance score (dead=0:normal=100:by=10)
                    rated by physician
dimnames(x.train)[[2]] \leftarrow c('age(yr)', 'M(1):F(2)', 'ph.karno(0:100:10)')
summary(x.train[ , 1])
table(x.train[ , 2])
table(x.train[ , 3])
x.test <- matrix(nrow=84, ncol=3) ## matrix of covariate scenarios</pre>
dimnames(x.test)[[2]] <- dimnames(x.train)[[2]]</pre>
i <- 1
for(age in 5*(9:15)) for(sex in 1:2) for(ph.karno in 10*(5:10)) {
    x.test[i, ] <- c(age, sex, ph.karno)</pre>
    i <- i+1
## this x.test is relatively small, but often you will want to
## predict for a large x.test matrix which may cause problems
## due to consumption of RAM so we can predict separately
```

predict.wbart 101

```
## mcparallel/mccollect do not exist on windows
if(.Platform$OS.type=='unix') {
##test BART with token run to ensure installation works
    set.seed(99)
   post <- surv.bart(x.train=x.train, times=times, delta=delta, nskip=5, ndpost=5, keepevery=1)</pre>
    pre <- surv.pre.bart(x.train=x.train, times=times, delta=delta, x.test=x.test)</pre>
    pred <- predict(post, pre$tx.test)</pre>
    ##pred. <- surv.pwbart(pre$tx.test, post$treedraws, post$binaryOffset)</pre>
}
## Not run:
## run one long MCMC chain in one process
set.seed(99)
post <- surv.bart(x.train=x.train, times=times, delta=delta)</pre>
## run "mc.cores" number of shorter MCMC chains in parallel processes
## post <- mc.surv.bart(x.train=x.train, times=times, delta=delta,</pre>
                         mc.cores=5, seed=99)
pre <- surv.pre.bart(x.train=x.train, times=times, delta=delta, x.test=x.test)</pre>
pred <- predict(post, pre$tx.test)</pre>
## let's look at some survival curves
## first, a younger group with a healthier KPS
## age 50 with KPS=90: males and females
## males: row 17, females: row 23
x.test[c(17, 23), ]
low.risk.males <- 16*post$K+1:post$K ## K=unique times including censoring</pre>
low.risk.females <- 22*post$K+1:post$K</pre>
plot(post$times, pred$surv.test.mean[low.risk.males], type='s', col='blue',
     main='Age 50 with KPS=90', xlab='t', ylab='S(t)', ylim=c(0, 1))
points(post$times, pred$surv.test.mean[low.risk.females], type='s', col='red')
## End(Not run)
```

predict.wbart

Predicting new observations with a previously fitted BART model

## **Description**

```
BART is a Bayesian "sum-of-trees" model. For a numeric response y, we have y = f(x) + \epsilon, where \epsilon \sim N(0, \sigma^2).
```

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f is the sum of many tree models. The goal is to have very flexible inference for the uknown function f.

In the spirit of "ensemble models", each tree is constrained by a prior to be a weak learner so that it contributes a small amount to the overall fit.

### Usage

```
## S3 method for class 'wbart'
predict(object, newdata, mc.cores=1, openmp=(mc.cores.openmp()>0), ...)
```

## **Arguments**

object object returned from previous BART fit. newdata Matrix of covariates to predict y for.

mc.cores Number of threads to utilize.

openmp Logical value dictating whether OpenMP is utilized for parallel processing. Of

course, this depends on whether OpenMP is available on your system which, by

default, is verified with mc.cores.openmp.

. . . Other arguments which will be passed on to pwbart.

#### **Details**

BART is an Bayesian MCMC method. At each MCMC interation, we produce a draw from the joint posterior  $(f, \sigma)|(x, y)$  in the numeric y case and just f in the binary y case.

Thus, unlike a lot of other modelling methods in R, we do not produce a single model object from which fits and summaries may be extracted. The output consists of values  $f^*(x)$  (and  $\sigma^*$  in the numeric case) where \* denotes a particular draw. The x is either a row from the training data (x.train) or the test data (x.test).

### Value

Returns a matrix of predictions corresponding to newdata.

## See Also

```
wbart, mc.wbart, pwbart, mc.pwbart, mc.cores.openmp
```

```
##simulate data (example from Friedman MARS paper) f = function(x) \{ 10*sin(pi*x[,1]*x[,2]) + 20*(x[,3]-.5)^2+10*x[,4]+5*x[,5] \}  sigma = 1.0 #y = f(x) + sigma*z , z^N(0,1) n = 100 #number of observations set.seed(99) x=matrix(runif(n*10),n,10) #10 variables, only first 5 matter y=f(x)
```

```
##test BART with token run to ensure installation works
set.seed(99)
post = wbart(x,y,nskip=5,ndpost=5)
x.test = matrix(runif(500*10),500,10)

## Not run:
##run BART
set.seed(99)
post = wbart(x,y)
x.test = matrix(runif(500*10),500,10)
pred = predict(post, x.test, mu=mean(y))

plot(apply(pred, 2, mean), f(x.test))

## End(Not run)
```

pwbart

Predicting new observations with a previously fitted BART model

## Description

```
BART is a Bayesian "sum-of-trees" model. For a numeric response y, we have y=f(x)+\epsilon, where \epsilon\sim N(0,\sigma^2).
```

f is the sum of many tree models. The goal is to have very flexible inference for the uknown function f.

In the spirit of "ensemble models", each tree is constrained by a prior to be a weak learner so that it contributes a small amount to the overall fit.

## Usage

# Arguments

x.test Matrix of covariates to predict y for. treedraws streedraws returned from whart or phart. Mu Mean to add on to y prediction.

mc.cores Number of threads to utilize.

transposed When running pwbart or mc.pwbart in parallel, it is more memory-efficient to

transpose x. test prior to calling the internal versions of these functions.

dodraws Whether to return the draws themselves (the default), or whether to return the

mean of the draws as specified by dodraws=FALSE.

nice Set the job niceness. The default niceness is 19: niceness goes from 0 (highest)

to 19 (lowest).

#### **Details**

BART is an Bayesian MCMC method. At each MCMC interation, we produce a draw from the joint posterior  $(f, \sigma)|(x, y)$  in the numeric y case and just f in the binary y case.

Thus, unlike a lot of other modelling methods in R, we do not produce a single model object from which fits and summaries may be extracted. The output consists of values  $f^*(x)$  (and  $\sigma^*$  in the numeric case) where \* denotes a particular draw. The x is either a row from the training data (x.train) or the test data (x.test).

## Value

Returns a matrix of predictions corresponding to x. test.

#### See Also

```
wbart predict.wbart
```

```
##simulate data (example from Friedman MARS paper)
f = function(x){
10*sin(pi*x[,1]*x[,2]) + 20*(x[,3]-.5)^2+10*x[,4]+5*x[,5]
sigma = 1.0 \#y = f(x) + sigma*z , z^N(0,1)
n = 100
             #number of observations
set.seed(99)
x=matrix(runif(n*10),n,10) #10 variables, only first 5 matter
y=f(x)
##test BART with token run to ensure installation works
set.seed(99)
post = wbart(x,y,nskip=5,ndpost=5)
x.test = matrix(runif(500*10), 500, 10)
## Not run:
##run BART
set.seed(99)
post = wbart(x,y)
x.test = matrix(runif(500*10),500,10)
pred = pwbart(post$treedraws, x.test, mu=mean(y))
plot(apply(pred, 2, mean), f(x.test))
```

```
## End(Not run)
```

recur.bart

BART for recurrent events

## **Description**

Here we have implemented a simple and direct approach to utilize BART in survival analysis that is very flexible, and is akin to discrete-time survival analysis. Following the capabilities of BART, we allow for maximum flexibility in modeling the dependence of survival times on covariates. In particular, we do not impose proportional hazards.

To elaborate, consider data in the usual form:  $(t_i, \delta_i, x_i)$  where  $t_i$  is the event time,  $\delta_i$  is an indicator distinguishing events ( $\delta = 1$ ) from right-censoring ( $\delta = 0$ ),  $x_i$  is a vector of covariates, and i = 1, ..., N indexes subjects.

We denote the K distinct event/censoring times by  $0 < t_{(1)} < ... < t_{(K)} < \infty$  thus taking  $t_{(j)}$  to be the  $j^{th}$  order statistic among distinct observation times and, for convenience,  $t_{(0)} = 0$ . Now consider event indicators  $y_{ij}$  for each subject i at each distinct time  $t_{(j)}$  up to and including the subject's observation time  $t_i = t_{(n_i)}$  with  $n_i = \sum_j I[t_{(j)} \le t_i]$ . This means  $y_{ij} = 0$  if  $j < n_i$  and  $y_{in_i} = \delta_i$ .

We then denote by  $p_{ij}$  the probability of an event at time  $t_{(j)}$  conditional on no previous event. We now write the model for  $y_{ij}$  as a nonparametric probit regression of  $y_{ij}$  on the time  $t_{(j)}$  and the covariates  $x_i$ , and then utilize BART for binary responses. Specifically,  $y_{ij} = \delta_i I[t_i = t_{(j)}], \ j = 1, ..., n_i$ ; we have  $p_{ij} = F(\mu_{ij}), \ \mu_{ij} = \mu_0 + f(t_{(j)}, x_i)$  where F denotes the standard normal cdf (probit link). As in the binary response case, f is the sum of many tree models.

### Usage

```
recur.bart(x.train=matrix(0,0,0),
    y.train=NULL, times=NULL, delta=NULL,
    x.test=matrix(0,0,0), x.test.nogrid=FALSE,
    sparse=FALSE, theta=0, omega=1,
    a=0.5, b=1, augment=FALSE, rho=NULL,
    xinfo=matrix(0,0,0), usequants=FALSE,

rm.const=TRUE, type='pbart',
    ntype=as.integer(
        factor(type, levels=c('wbart', 'pbart', 'lbart'))),
    k=2, power=2, base=0.95,
    offset=NULL, tau.num=c(NA, 3, 6)[ntype],
    ntree=50, numcut = 100L, ndpost=1000, nskip=250,
    keepevery=10,
```

```
keeptrainfits = TRUE,
           seed=99, ## mc.recur.bart only
           mc.cores=2, ## mc.recur.bart only
           nice=19L ## mc.recur.bart only
mc.recur.bart(x.train=matrix(0,0,0),
              y.train=NULL, times=NULL, delta=NULL,
              x.test=matrix(0,0,0), x.test.nogrid=FALSE,
              sparse=FALSE, theta=0, omega=1,
              a=0.5, b=1, augment=FALSE, rho=NULL,
              xinfo=matrix(0,0,0), usequants=FALSE,
              rm.const=TRUE, type='pbart',
              ntype=as.integer(
                  factor(type, levels=c('wbart', 'pbart', 'lbart'))),
              k=2, power=2, base=0.95,
              offset=NULL, tau.num=c(NA, 3, 6)[ntype],
              ntree=50, numcut = 100L, ndpost=1000, nskip=250,
              keepevery=10,
              printevery = 100L,
              keeptrainfits = TRUE,
              seed=99, ## mc.recur.bart only
              mc.cores=2, ## mc.recur.bart only
              nice=19L ## mc.recur.bart only
```

# Arguments

x. train Explanatory variables for training (in sample) data.

Must be a matrix with (as usual) rows corresponding to observations and columns to variables.

recur.bart will generate draws of f(t,x) for each x which is a row of x.train (note that the definition of x.train is dependent on whether y.train has been specified; see below).

y.train Binary response dependent variable for training (in sample) data.

If y.train is NULL, then y.train (x.train and x.test, if specified) are generated by a call to recur.pre.bart (which require that times and delta be provided: see below); otherwise, y.train (x.train and x.test, if specified) are utilized as given assuming that the data construction has already been performed.

times The time of event or right-censoring.

If y. train is NULL, then times (and delta) must be provided.

delta The event indicator: 1 is an event while 0 is censored.

If y. train is NULL, then delta (and times) must be provided.

x.test Explanatory variables for test (out of sample) data.

Must be a matrix and have the same structure as x.train.

recur. bart will generate draws of f(t,x) for each x which is a row of x.test.

x.test.nogrid Occasionally, you do not need the entire time grid for x.test. If so, then for

performance reasons, you can set this argument to TRUE.

sparse Whether to perform variable selection based on a sparse Dirichlet prior rather

than simply uniform; see Linero 2016.

theta Set *theta* parameter; zero means random.

omega Set *omega* parameter; zero means random.

a Sparse parameter for Beta(a,b) prior:  $0.5 \le a \le 1$  where lower values

inducing more sparsity.

b Sparse parameter for Beta(a, b) prior; typically, b = 1.

rho Sparse parameter: typically rho = p where p is the number of covariates under

consideration.

augment Whether data augmentation is to be performed in sparse variable selection.

xinfo You can provide the cutpoints to BART or let BART choose them for you. To

provide them, use the xinfo argument to specify a list (matrix) where the items (rows) are the covariates and the contents of the items (columns) are the cut-

points.

usequants If usequants=FALSE, then the cutpoints in xinfo are generated uniformly; oth-

erwise, if TRUE, uniform quantiles are used for the cutpoints.

rm. const Whether or not to remove constant variables.

type Whether to employ Albert-Chib, 'pbart', or Holmes-Held, 'lbart'.

ntype The integer equivalent of type where 'wbart' is 1, 'pbart' is 2 and 'lbart'

is 3.

k is the number of prior standard deviations f(t,x) is away from +/-3. The

bigger k is, the more conservative the fitting will be.

power Power parameter for tree prior.

base Base parameter for tree prior.

offset With binary BART, the centering is P(Y = 1|x) = F(f(x) + offset) where

offset defaults to F^{-1}(mean(y.train)). You can use the offset parame-

ter to over-ride these defaults.

tau.num The numerator in the tau definition, i.e., tau=tau.num/(k\*sqrt(ntree)).

ntree The number of trees in the sum.

numcut The number of possible values of c (see usequants). If a single number if given,

this is used for all variables. Otherwise a vector with length equal to ncol(x.train) is required, where the  $i^{th}$  element gives the number of c used for the  $i^{th}$  variable in x.train. If usequants is false, numcut equally spaced cutoffs are used covering the range of values in the corresponding column of x.train. If usequants is true, then min(numcut, the number of unique values in the corresponding columns of

x.train - 1) c values are used.

ndpost The number of posterior draws returned.

nskip Number of MCMC iterations to be treated as burn in. keepevery Every keepevery draw is kept to be returned to the user.

printevery As the MCMC runs, a message is printed every printevery draws.

keeptrainfits Whether to keep yhat.train or not.

seed mc.recur.bart only: seed required for reproducible MCMC.
mc.cores mc.recur.bart only: number of cores to employ in parallel.

nice mc.recur.bart only: set the job niceness. The default niceness is 19: niceness

goes from 0 (highest) to 19 (lowest).

### Value

recur.bart returns an object of type recurbart which is essentially a list. Besides the items listed below, the list has a binaryOffset component giving the value used, a times component giving the unique times, K which is the number of unique times, tx.train and tx.test, if any.

yhat.train	A matrix with ndpost rows and $\operatorname{nrow}(x.\operatorname{train})$ columns. Each row corresponds to a draw $f^*$ from the posterior of $f$ and each column corresponds to a row of x.train. The $(i,j)$ value is $f^*(t,x)$ for the $i^{th}$ kept draw of $f$ and the $j^{th}$ row of x.train. Burn-in is dropped.
haz.train	The hazard function, $h(t x)$ , where x's are the rows of the training data.
cum.train	The cumulative hazard function, $h(t x)$ , where x's are the rows of the training data.
yhat.test	Same as yhat.train but now the x's are the rows of the test data.
haz.test	The hazard function, $h(t x)$ , where x's are the rows of the test data.
cum.test	The cumulative hazard function, $h(t x)$ , where x's are the rows of the test data.
varcount	a matrix with ndpost rows and nrow(x.train) columns. Each row is for a draw. For each variable (corresponding to the columns), the total count of the number of times that variable is used in a tree decision rule (over all trees) is given.

Note that yhat.train and yhat.test are f(t,x) + binaryOffset. If you want draws of the probability P(Y=1|t,x) you need to apply the normal cdf (pnorm) to these values.

## See Also

```
recur.pre.bart, predict.recurbart, recur.pwbart, mc.recur.pwbart
```

```
## load 20 percent random sample
data(xdm20.train)
data(xdm20.test)
data(ydm20.train)

##test BART with token run to ensure installation works
## with current technology even a token run will violate CRAN policy
```

recur.bart 109

```
## set.seed(99)
## post <- recur.bart(x.train=xdm20.train, y.train=ydm20.train,</pre>
                       nskip=1, ndpost=1, keepevery=1)
## Not run:
## set.seed(99)
## post <- recur.bart(x.train=xdm20.train, y.train=ydm20.train,</pre>
                       keeptrainfits=TRUE)
## larger data sets can take some time so, if parallel processing
## is available, submit this statement instead
post <- mc.recur.bart(x.train=xdm20.train, y.train=ydm20.train,</pre>
                       keeptrainfits=TRUE, mc.cores=8, seed=99)
require(rpart)
require(rpart.plot)
post$yhat.train.mean <- apply(post$yhat.train, 2, mean)</pre>
dss <- rpart(post$yhat.train.mean~xdm20.train)</pre>
rpart.plot(dss)
## for the 20 percent sample, notice that the top splits
## involve cci_pvd and n
## for the full data set, notice that all splits
## involve ca, cci_pud, cci_pvd, ins270 and n
## (except one at the bottom involving a small group)
## compare patients treated with insulin (ins270=1) vs
## not treated with insulin (ins270=0)
N <- 50 ## 50 training patients and 50 validation patients
K <- post$K ## 798 unique time points
NK <- 50*K
## only testing set, i.e., remove training set
xdm20.test. <- xdm20.test[NK+1:NK, post$rm.const]</pre>
xdm20.test. <- rbind(xdm20.test., xdm20.test.)</pre>
xdm20.test.[ , 'ins270'] <- rep(0:1, each=NK)</pre>
## multiple threads will be utilized if available
pred <- predict(post, xdm20.test., mc.cores=8)</pre>
## create Friedman's partial dependence function for the
## relative intensity for ins270 by time
M <- nrow(pred$haz.test) ## number of MCMC samples
RI <- matrix(0, M, K)
for(j in 1:K) {
    h \leftarrow seq(j, NK, by=K)
    RI[ , j] <- apply(pred$haz.test[ , h+NK]/</pre>
                       pred$haz.test[ , h], 1, mean)
}
RI.lo <- apply(RI, 2, quantile, probs=0.025)
```

```
RI.mu <- apply(RI, 2, mean)
RI.hi <- apply(RI, 2, quantile, probs=0.975)

plot(post$times, RI.hi, type='l', lty=2, log='y',
        ylim=c(min(RI.lo, 1/RI.hi), max(1/RI.lo, RI.hi)),
        xlab='t', ylab='RI(t, x)',
        sub='insulin(ins270=1) vs. no insulin(ins270=0)',
        main='Relative intensity of hospital admissions for diabetics')
lines(post$times, RI.mu)
lines(post$times, RI.lo, lty=2)
lines(post$times, rep(1, K), col='darkgray')

## RI for insulin therapy seems fairly constant with time
mean(RI.mu)

## End(Not run)</pre>
```

recur.pre.bart

Data construction for recurrent events with BART

#### **Description**

Recurrent event data contained in  $(t_1, \delta_1, ..., t_k, \delta_k, x)$  must be translated to data suitable for the BART model; see recur.bart for more details.

### Usage

```
recur.pre.bart( times, delta, x.train=NULL, tstop=NULL, last.value=TRUE )
```

# Arguments

times	Matrix of time to event or right-censoring.
delta	Matrix of event indicators: 1 is an event while 0 is censored.
x.train	Explanatory variables for training (in sample) data. If provided, must be a matrix with (as usual) rows corresponding to observations and columns to variables.
tstop	For non-instantaneous events, this the matrix of event stop times, i.e., between times[i, j] and tstop[i, j] subject i is not in the risk set for a recurrent event. N.B. This is NOT for counting process notation.
last.value	If last.value=TRUE, then the sojourn time, v, and the number of previous events, N, are carried forward assuming that no new events occur beyond censoring. If last.value=FALSE, then these variables are coded NA for easy iden-

tification allowing replacement with the desired values.

#### Value

recur.pre.bart returns a list. Besides the items listed below, the list has a times component giving the unique times and K which is the number of unique times.

y.train A vector of binary responses.tx.train A matrix with the rows of the training data.tx.test Generated from x.train (see discussion above included in the argument last.value).

#### See Also

recur.bart

```
data(bladder)
subset <- -which(bladder1$stop==0)</pre>
bladder0 <- bladder1[subset, ]</pre>
id <- unique(sort(bladder0$id))</pre>
N <- length(id)
L <- max(bladder0$enum)</pre>
times <- matrix(0, nrow=N, ncol=L)</pre>
dimnames(times)[[1]] <- paste0(id)</pre>
delta <- matrix(0, nrow=N, ncol=L)</pre>
dimnames(delta)[[1]] <- paste0(id)</pre>
x.train <- matrix(NA, nrow=N, ncol=3+2*L) ## add time-dependent cols too
dimnames(x.train)[[1]] <- paste0(id)</pre>
dimnames(x.train)[[2]] \leftarrow c('Pl', 'B6', 'Th', rep(c('number', 'size'), L))
for(i in 1:N) {
    h <- id[i]
    for(j in 1:L) {
         k \leftarrow which(bladder0$id==h & bladder0$enum==j)
         if(length(k)==1) {
             times[i, j] <- bladder0$stop[k]</pre>
             delta[i, j] <- (bladder0$status[k]==1)*1</pre>
             if(j==1) {
                  x.train[i, 1] <- as.numeric(bladder0$treatment[k])==1</pre>
                  x.train[i, 2] <- as.numeric(bladder0$treatment[k])==2</pre>
                  x.train[i, 3] <- as.numeric(bladder0$treatment[k])==3</pre>
                  x.train[i, 4] <- bladder0$number[k]</pre>
                  x.train[i, 5] <- bladder0$size[k]</pre>
             else if(delta[i, j]==1) {
                  if(bladder0$rtumor[k]!='.')
                      x.train[i, 2*j+2] <- as.numeric(bladder0$rtumor[k])</pre>
```

```
if(bladder0$rsize[k]!='.')
                     x.train[i, 2*j+3] <- as.numeric(bladder0$rsize[k])</pre>
            }
        }
    }
}
pre <- recur.pre.bart(times=times, delta=delta, x.train=x.train)</pre>
J <- nrow(pre$tx.train)</pre>
for(j in 1:J) {
    if(pre$tx.train[j, 3]>0) {
        pre$tx.train[j, 7] <- pre$tx.train[j, 7+pre$tx.train[j, 3]*2]</pre>
        pre$tx.train[j, 8] <- pre$tx.train[j, 8+pre$tx.train[j, 3]*2]</pre>
    }
}
pre$tx.train <- pre$tx.train[ , 1:8]</pre>
K <- pre$K
NK <- N*K
for(j in 1:NK) {
    if(pre$tx.test[j, 3]>0) {
        pre$tx.test[j, 7] <- pre$tx.test[j, 7+pre$tx.test[j, 3]*2]</pre>
        pre$tx.test[j, 8] <- pre$tx.test[j, 8+pre$tx.test[j, 3]*2]</pre>
    }
pre$tx.test <- pre$tx.test[ , 1:8]</pre>
## in bladder1 both number and size are recorded as integers
## from 1 to 8 however they are often missing for recurrences
## at baseline there are no missing and 1 is the mode of both
pre$tx.train[which(is.na(pre$tx.train[ , 7])), 7] <- 1</pre>
pre$tx.train[which(is.na(pre$tx.train[ , 8])), 8] <- 1</pre>
pre$tx.test[which(is.na(pre$tx.test[ , 7])), 7] <- 1</pre>
pre$tx.test[which(is.na(pre$tx.test[ , 8])), 8] <- 1</pre>
## it is a good idea to explore more sophisticated methods
## such as imputing the missing data with Sequential BART
## Xu, Daniels and Winterstein. Sequential BART for imputation of missing
## covariates. Biostatistics 2016 doi: 10.1093/biostatistics/kxw009
## http://biostatistics.oxfordjournals.org/content/early/2016/03/15/biostatistics.kxw009/suppl/DC1
## https://cran.r-project.org/package=sbart
## library(sbart)
## set.seed(21)
## train <- seqBART(xx=pre$tx.train, yy=NULL, datatype=rep(0, 6),</pre>
                   type=0, numskip=20, burn=1000)
## coarsen the imputed data same way as observed example data
## train$imputed5[which(train$imputed5[ , 7]<1), 7] <- 1</pre>
## train$imputed5[which(train$imputed5[ , 7]>8), 7] <- 8</pre>
## train$imputed5[ , 7] <- round(train$imputed5[ , 7])</pre>
## train$imputed5[which(train$imputed5[ , 8]<1), 8] <- 1</pre>
## train$imputed5[which(train$imputed5[ , 8]>8), 8] <- 8</pre>
```

```
## train$imputed5[ , 8] <- round(train$imputed5[ , 8])</pre>
## for Friedman's partial dependence, we need to estimate the whole cohort
## at each treatment assignment (and, average over those)
pre$tx.test <- rbind(pre$tx.test, pre$tx.test, pre$tx.test)</pre>
pre$tx.test[, 4] <- c(rep(1, NK), rep(0, 2*NK))
                                                             ## P1
pre$tx.test[ , 5] <- c(rep(0, NK), rep(1, NK), rep(0, NK))## B6</pre>
pre$tx.test[ , 6] <- c(rep(0, 2*NK), rep(1, NK))</pre>
## Not run:
## set.seed(99)
## post <- recur.bart(y.train=pre$y.train, x.train=pre$tx.train, x.test=pre$tx.test)</pre>
## depending on your performance, you may want to run in parallel if available
post <- mc.recur.bart(y.train=pre$y.train, x.train=pre$tx.train,</pre>
                       x.test=pre$tx.test, mc.cores=8, seed=99)
M <- nrow(post$yhat.test)</pre>
RI.B6.Pl <- matrix(0, nrow=M, ncol=K)
RI.Th.Pl <- matrix(0, nrow=M, ncol=K)
RI.Th.B6 <- matrix(0, nrow=M, ncol=K)
for(j in 1:K) {
    h \leftarrow seq(j, NK, K)
    RI.B6.Pl[ , j] <- apply(post$prob.test[ , h+NK]/</pre>
                             post$prob.test[ , h], 1, mean)
    RI.Th.Pl[ , j] <- apply(post$prob.test[ , h+2*NK]/</pre>
                             post$prob.test[ , h], 1, mean)
    \label{eq:richard} $\tt RI.Th.B6[\ ,\ j] <- apply(post*prob.test[\ ,\ h+2*NK]/
                             post$prob.test[ , h+NK], 1, mean)
}
RI.B6.Pl.mu <- apply(RI.B6.Pl, 2, mean)
RI.B6.Pl.025 <- apply(RI.B6.Pl, 2, quantile, probs=0.025)
RI.B6.Pl.975 <- apply(RI.B6.Pl, 2, quantile, probs=0.975)</pre>
RI.Th.Pl.mu <- apply(RI.Th.Pl, 2, mean)
RI.Th.Pl.025 <- apply(RI.Th.Pl, 2, quantile, probs=0.025)
RI.Th.Pl.975 <- apply(RI.Th.Pl, 2, quantile, probs=0.975)
RI.Th.B6.mu <- apply(RI.Th.B6, 2, mean)
RI.Th.B6.025 <- apply(RI.Th.B6, 2, quantile, probs=0.025)
RI.Th.B6.975 <- apply(RI.Th.B6, 2, quantile, probs=0.975)
plot(post$times, RI.Th.Pl.mu, col='blue',
     log='y', main='Bladder cancer ex: Thiotepa vs. Placebo',
     type='l', ylim=c(0.1, 10), ylab='RI(t)', xlab='t (months)')
lines(post$times, RI.Th.Pl.025, col='red')
lines(post$times, RI.Th.Pl.975, col='red')
abline(h=1)
plot(post$times, RI.B6.Pl.mu, col='blue',
     log='y', main='Bladder cancer ex: Vitamin B6 vs. Placebo',
     type='l', ylim=c(0.1, 10), ylab='RI(t)', xlab='t (months)')
```

```
lines(post$times, RI.B6.Pl.025, col='red')
lines(post$times, RI.B6.Pl.975, col='red')
abline(h=1)

plot(post$times, RI.Th.B6.mu, col='blue',
    log='y', main='Bladder cancer ex: Thiotepa vs. Vitamin B6',
    type='l', ylim=c(0.1, 10), ylab='RI(t)', xlab='t (months)')
lines(post$times, RI.Th.B6.025, col='red')
lines(post$times, RI.Th.B6.975, col='red')
abline(h=1)

## End(Not run)
```

rs.pbart

BART for dichotomous outcomes with parallel computation and stratified random sampling

## Description

BART is a Bayesian "sum-of-trees" model.

For numeric response y, we have  $y = f(x) + \epsilon$ , where  $\epsilon \sim N(0, \sigma^2)$ .

For a binary response y, P(Y = 1|x) = F(f(x)), where F denotes the standard normal cdf (probit link).

In both cases, f is the sum of many tree models. The goal is to have very flexible inference for the uknown function f.

In the spirit of "ensemble models", each tree is constrained by a prior to be a weak learner so that it contributes a small amount to the overall fit.

# Usage

```
rs.pbart(
    x.train, y.train, x.test=matrix(0.0,0,0),
    C=floor(length(y.train)/2000),
    k=2.0, power=2.0, base=.95,
    binaryOffset=0,
    ntree=50L, numcut=100L,
    ndpost=1000L, nskip=100L,
    keepevery=1L, printevery=100,
    keeptrainfits=FALSE, transposed=FALSE,

mc.cores = 2L, nice = 19L,
    seed = 99L
)
```

## Arguments

x.train Explanatory variables for training (in sample) data.

May be a matrix or a data frame, with (as usual) rows corresponding to obser-

vations and columns to variables.

If a variable is a factor in a data frame, it is replaced with dummies. Note that q dummies are created if q>2 and one dummy is created if q=2, where q is the number of levels of the factor. pbart will generate draws of f(x) for each x

which is a row of x.train.

y. train Dependent variable for training (in sample) data.

If y is numeric a continous response model is fit (normal errors).

If y is a factor (or just has values 0 and 1) then a binary response model with a

probit link is fit.

x.test Explanatory variables for test (out of sample) data.

Should have same structure as x.train.

pbart will generate draws of f(x) for each x which is a row of x.test.

C The number of shards to break the data into and analyze separately.

k For binary y, k is the number of prior standard deviations f(x) is away from

+/-3. In both cases, the bigger k is, the more conservative the fitting will be.

power Power parameter for tree prior.

Base parameter for tree prior.

binaryOffset Used for binary y.

The model is P(Y = 1|x) = F(f(x) + binaryOffset).

The idea is that f is shrunk towards 0, so the offset allows you to shrink towards

a probability other than .5.

ntree The number of trees in the sum.

numcut The number of possible values of c (see usequants). If a single number if given,

this is used for all variables. Otherwise a vector with length equal to  $\operatorname{ncol}(x.\operatorname{train})$  is required, where the  $i^{th}$  element gives the number of c used for the  $i^{th}$  variable in x.train. If usequants is false, numcut equally spaced cutoffs are used covering the range of values in the corresponding column of x.train. If usequants is true, then  $\min(\operatorname{numcut}$ , the number of unique values in the corresponding columns of

x.train - 1) c values are used.

ndpost The number of posterior draws returned.

nskip Number of MCMC iterations to be treated as burn in. keepevery Every keepevery draw is kept to be returned to the user.

printevery As the MCMC runs, a message is printed every printevery draws.

keeptrainfits Whether to keep yhat.train or not.

transposed When running poart in parallel, it is more memory-efficient to transpose x. train

and x. test, if any, prior to calling mc.pbart.

seed Setting the seed required for reproducible MCMC.

mc.cores Number of cores to employ in parallel.

nice Set the job niceness. The default niceness is 19: niceness goes from 0 (highest)

to 19 (lowest).

#### **Details**

BART is an Bayesian MCMC method. At each MCMC interation, we produce a draw from the joint posterior  $(f, \sigma)|(x, y)$  in the numeric y case and just f in the binary y case.

Thus, unlike a lot of other modelling methods in R, we do not produce a single model object from which fits and summaries may be extracted. The output consists of values  $f^*(x)$  (and  $\sigma^*$  in the numeric case) where \* denotes a particular draw. The x is either a row from the training data (x.train) or the test data (x.test).

#### Value

rs. pbart returns an object of type pbart which is essentially a list.

yhat.shard Estimates generated from the individual shards rather than from the whole. This

object is only useful for assessing convergence.

A matrix with ndpost rows and nrow(x.train) columns. Each row corresponds to a draw  $f^*$  from the posterior of f and each column corresponds to a row of x.train. The (i,j) value is  $f^*(x)$  for the  $i^{th}$  kept draw of f and the  $j^{th}$  row of

x.train.

Burn-in is dropped.

yhat.train Estimates generated from the whole if keeptrainfits=TRUE.

A matrix with ndpost rows and nrow(x.train) columns. Each row corresponds to a draw  $f^*$  from the posterior of f and each column corresponds to a row of x.train. The (i,j) value is  $f^*(x)$  for the  $i^{th}$  kept draw of f and the  $j^{th}$  row of

x.train.

Burn-in is dropped.

yhat.test Estimates generated from the whole if x.test is provided.

Same as yhat.train but now the x's are the rows of the test data.

varcount a matrix with ndpost rows and nrow(x.train) columns. Each row is for a draw.

For each variable (corresponding to the columns), the total count of the number

of times that variable is used in a tree decision rule (over all trees) is given.

In addition the list has a binaryOffset component giving the value used.

Note that in the binary y, case yhat.train and yhat.test are f(x) + binaryOffset. If you want draws of the probability P(Y=1|x) you need to apply the normal cdf (pnorm) to these values.

#### See Also

mc.pbart

```
##simulate from Friedman's five-dimensional test function
##Friedman JH. Multivariate adaptive regression splines
##(with discussion and a rejoinder by the author).
##Annals of Statistics 1991; 19:1-67.
```

```
f = function(x) #only the first 5 matter
```

```
sin(pi*x[, 1]*x[, 2]) + 2*(x[, 3]-.5)^2+x[, 4]+0.5*x[, 5]-1.5
sigma = 1.0 \# y = f(x) + sigma*z \ where z^N(0, 1)
k = 50
             #number of covariates
thin = 25
ndpost = 2500
nskip = 100
C = 10
m = 10
n = 10000
set.seed(12)
x.train=matrix(runif(n*k), n, k)
Ey.train = f(x.train)
y.train=(Ey.train+sigma*rnorm(n)>0)*1
table(y.train)/n
x \leftarrow x.train
x4 <- seq(0, 1, length.out=m)
for(i in 1:m) {
    x[, 4] \leftarrow x4[i]
    if(i==1) x.test <- x
    else x.test <- rbind(x.test, x)</pre>
}
## parallel::mcparallel/mccollect do not exist on windows
if(.Platform$OS.type=='unix') {
##test BART with token run to ensure installation works
    post = rs.pbart(x.train, y.train,
                C=C, mc.cores=4, keepevery=1,
                 seed=99, ndpost=1, nskip=1)
}
## Not run:
post = rs.pbart(x.train, y.train, x.test=x.test,
                C=C, mc.cores=8, keepevery=thin,
                 seed=99, ndpost=ndpost, nskip=nskip)
str(post)
par(mfrow=c(2, 2))
M <- nrow(post$yhat.test)</pre>
pred <- matrix(nrow=M, ncol=10)</pre>
for(i in 1:m) {
    h \leftarrow (i-1)*n+1:n
    pred[ , i] <- apply(pnorm(post$yhat.test[ , h]), 1, mean)</pre>
}
pred <- apply(pred, 2, mean)</pre>
```

```
plot(x4, qnorm(pred), xlab=expression(x[4]),
     ylab='partial dependence function', type='l')
i <- floor(seq(1, n, length.out=10))</pre>
j <- seq(-0.5, 0.4, length.out=10)
for(h in 1:10) {
    auto.corr <- acf(post$yhat.shard[ , i[h]], plot=FALSE)</pre>
    if(h==1) {
        max.lag <- max(auto.corr$lag[ , 1, 1])</pre>
        plot(1:max.lag+j[h], auto.corr$acf[1+(1:max.lag), 1, 1],
             type='h', xlim=c(0, max.lag+1), ylim=c(-1, 1),
             ylab='auto-correlation', xlab='lag')
    }
   else
        lines(1:max.lag+j[h], auto.corr$acf[1+(1:max.lag), 1, 1],
              type='h', col=h)
}
for(j in 1:10) {
    if(j==1)
        plot(pnorm(post$yhat.shard[ , i[j]]),
             type='l', ylim=c(0, 1),
             sub=paste0('N:', n, ', k:', k),
             ylab=expression(Phi(f(x))), xlab='m')
    else
        lines(pnorm(post$yhat.shard[ , i[j]]),
              type='l', col=j)
}
geweke <- gewekediag(post$yhat.shard)</pre>
j < -10^{(\log 10(n)-1)}
plot(geweke$z, pch='.', cex=2, ylab='z', xlab='i',
     sub=paste0('N:', n, ', k:', k),
     xlim=c(j, n), ylim=c(-5, 5))
lines(1:n, rep(-1.96, n), type='l', col=6)
lines(1:n, rep(+1.96, n), type='l', col=6)
lines(1:n, rep(-2.576, n), type='1', col=5)
lines(1:n, rep(+2.576, n), type='l', col=5)
lines(1:n, rep(-3.291, n), type='l', col=4)
lines(1:n, rep(+3.291, n), type='l', col=4)
lines(1:n, rep(-3.891, n), type='l', col=3)
lines(1:n, rep(+3.891, n), type='l', col=3)
lines(1:n, rep(-4.417, n), type='1', col=2)
lines(1:n, rep(+4.417, n), type='l', col=2)
text(c(1, 1), c(-1.96, 1.96), pos=2, cex=0.6, labels='0.95')
text(c(1, 1), c(-2.576, 2.576), pos=2, cex=0.6, labels='0.99')
text(c(1, 1), c(-3.291, 3.291), pos=2, cex=0.6, labels='0.999')
text(c(1, 1), c(-3.891, 3.891), pos=2, cex=0.6, labels='0.9999')
text(c(1, 1), c(-4.417, 4.417), pos=2, cex=0.6, labels='0.99999')
par(mfrow=c(1, 1))
```

rtgamma 119

```
##dev.copy2pdf(file='geweke.rs.pbart.pdf')
## End(Not run)
```

rtgamma

Testing truncated Gamma sampling

# Description

Truncated Gamma draws are needed for the standard deviation of the random effects Gibbs conditional

# Usage

```
rtgamma(n, shape, rate, a)
```

# **Arguments**

n	Number of samples.
shape	Sampling from a truncated Gamma where $E[x] = shape/rate$ .
rate	This parameter is the inverse of the scale which is an alternative representation for the Gamma distribution.
а	The truncation point, i.e., $a < x$ .

# Value

Returns n truncated Gamma, i.e., Gam(shape, rate)I(a, infinity).

# References

Gentle J. (2013) Random number generation and Monte Carlo methods. Springer, New York, NY.

```
set.seed(12)
rtgamma(1, 3, 1, 4)
rtgamma(1, 3, 1, 4)
a=rtgamma(10000, 10, 2, 1)
mean(a)
min(a)
```

120 rtnorm

rtnorm

Testing truncated Normal sampling

# Description

Truncated Normal latents are necessary to transform a binary BART into a continuous BART.

# Usage

```
rtnorm(n, mean, sd, tau)
```

# **Arguments**

n Number of samples.

mean Mean.

sd Standard deviation. tau Truncation point.

# Value

Returns n truncated Normals, i.e., N(mean, sd)I(tau, infinity).

# References

Robert C. (1995) Simulation of truncated normal variables. *Statistics and computing*, **5(2)**, 121–125.

## See Also

```
pbart, lbart
```

```
set.seed(12)
rtnorm(1, 0, 1, 3)
rtnorm(1, 0, 1, 3)
```

spectrum0ar 121

#### Description

The spectral density at frequency zero is estimated by fitting an autoregressive model. spectrum0(x)/length(x) estimates the variance of mean(x).

#### Usage

spectrum0ar(x)

## **Arguments**

Х

Matrix of MCMC chains: the rows are the samples and the columns are different "parameters". For BART, generally, the columns are estimates of f. For pbart, they are different subjects. For surv.bart, they are different subjects at a grid of times.

#### **Details**

The ar() function to fit an autoregressive model to the time series x. For multivariate time series, separate models are fitted for each column. The value of the spectral density at zero is then given by a well-known formula. Adapted from the spectrum0.ar function of the coda package which passes mcmc objects as arguments rather than matrices.

## Value

A list with the following values

spec The predicted value of the spectral density at frequency zero.

order The order of the fitted model

#### References

Martyn Plummer, Nicky Best, Kate Cowles and Karen Vines (2006). CODA: Convergence Diagnosis and Output Analysis for MCMC, R News, vol 6, 7-11.

BW Silverman (1986). Density estimation for statistics and data analysis. Chapman and Hall, London.

#### See Also

gewekediag

122 srstepwise

srstepwise	Stepwise Variable Selection Procedure for survreg	

# **Description**

This stepwise variable selection procedure can be applied to obtain the best candidates for a survreg fit.

# Usage

```
srstepwise(x, times, delta, sle = 0.15, sls = 0.15, dist='lognormal')
```

# **Arguments**

x	Matrix of variables to consider.
times	The time to an event, if any.
delta	The event indicator: 1 for event, 0 for no event.
sle	The chosen significance level for entering.
sls	The chosen significance level for staying.
dist	The distribution to be used by survreg.

## **Details**

Unfortunately, no stepwise procedure exists for survreg models. Therefore, we provide this brute force method.

# Value

Returns a list of indices of variables which have entered and stayed.

#### See Also

lung

```
names. <- names(lung)[-(2:3)]
status1 <- ifelse(lung$status==2,1,0)
X <- as.matrix(lung)[ , names.]
vars=srstepwise(X, lung$time, status1)
print(names.[vars])</pre>
```

stratrs 123

stratrs

Perform stratified random sampling to balance outcomes

# **Description**

This function is used to perform stratified random sampling to balance outcomes among the shards.

#### Usage

```
stratrs(y, C=5, P=0)
```

# Arguments

y The binary/categorical/continuous outcome.

C The number of shards to break the data set into.

P For continuous data, we break the range into P segments via the quantiles. Spec-

ifying, P=20 seems to work reasonably well.

# **Details**

To perform BART with large data sets, random sampling is employed to break the data into C shards. Each shard should be balanced with respect to the outcome. For binary/categorical outcomes, stratified random sampling is employed with this function.

# Value

A vector is returned with each element assigned to a shard.

#### See Also

```
rs.pbart
```

```
set.seed(12)
x <- rbinom(25000, 1, 0.1)
a <- stratrs(x)
table(a, x)
z <- pmin(rpois(25000, 0.8), 5)
b <- stratrs(z)
table(b, z)</pre>
```

surv.bart

Survival analysis with BART

# **Description**

Here we have implemented a simple and direct approach to utilize BART in survival analysis that is very flexible, and is akin to discrete-time survival analysis. Following the capabilities of BART, we allow for maximum flexibility in modeling the dependence of survival times on covariates. In particular, we do not impose proportional hazards.

To elaborate, consider data in the usual form:  $(t_i, \delta_i, x_i)$  where  $t_i$  is the event time,  $\delta_i$  is an indicator distinguishing events ( $\delta = 1$ ) from right-censoring ( $\delta = 0$ ),  $x_i$  is a vector of covariates, and i = 1, ..., N indexes subjects.

We denote the K distinct event/censoring times by  $0 < t_{(1)} < \ldots < t_{(K)} < \infty$  thus taking  $t_{(j)}$  to be the  $j^{th}$  order statistic among distinct observation times and, for convenience,  $t_{(0)} = 0$ . Now consider event indicators  $y_{ij}$  for each subject i at each distinct time  $t_{(j)}$  up to and including the subject's observation time  $t_i = t_{(n_i)}$  with  $n_i = \sum_j I[t_{(j)} \le t_i]$ . This means  $y_{ij} = 0$  if  $j < n_i$  and  $y_{in_i} = \delta_i$ .

We then denote by  $p_{ij}$  the probability of an event at time  $t_{(j)}$  conditional on no previous event. We now write the model for  $y_{ij}$  as a nonparametric probit regression of  $y_{ij}$  on the time  $t_{(j)}$  and the covariates  $x_i$ , and then utilize BART for binary responses. Specifically,  $y_{ij} = \delta_i I[t_i = t_{(j)}], \ j = 1, ..., n_i$ ; we have  $p_{ij} = F(\mu_{ij}), \ \mu_{ij} = \mu_0 + f(t_{(j)}, x_i)$  where F denotes the standard normal cdf (probit link). As in the binary response case, f is the sum of many tree models.

#### Usage

```
surv.bart( x.train=matrix(0,0,0),
    y.train=NULL, times=NULL, delta=NULL,
    x.test=matrix(0,0,0),
    K=NULL, events=NULL, ztimes=NULL, zdelta=NULL,
    sparse=FALSE, theta=0, omega=1,
    a=0.5, b=1, augment=FALSE, rho=NULL,
    xinfo=matrix(0,0,0), usequants=FALSE,

rm.const=TRUE, type='pbart',
    ntype=as.integer(
        factor(type, levels=c('wbart', 'pbart', 'lbart'))),
    k=2, power=2, base=.95,
    offset=NULL, tau.num=c(NA, 3, 6)[ntype],
    ntree=50, numcut=100, ndpost=1000, nskip=250,
    keepevery = 10L,
```

```
id=NULL,
                       ## surv.bart only
           seed=99,
                       ## mc.surv.bart only
           mc.cores=2, ## mc.surv.bart only
           nice=19L
                       ## mc.surv.bart only
mc.surv.bart(x.train=matrix(0,0,0),
              y.train=NULL, times=NULL, delta=NULL,
              x.test=matrix(0,0,0),
              K=NULL, events=NULL, ztimes=NULL, zdelta=NULL,
              sparse=FALSE, theta=0, omega=1,
              a=0.5, b=1, augment=FALSE, rho=NULL,
              xinfo=matrix(0,0,0), usequants=FALSE,
              rm.const=TRUE, type='pbart',
              ntype=as.integer(
                  factor(type, levels=c('wbart', 'pbart', 'lbart'))),
              k=2, power=2, base=.95,
              offset=NULL, tau.num=c(NA, 3, 6)[ntype],
              ntree=50, numcut=100, ndpost=1000, nskip=250,
              keepevery = 10L,
              printevery=100L,
                          ## surv.bart only
              id=NULL,
                          ## mc.surv.bart only
              seed=99,
              mc.cores=2, ## mc.surv.bart only
              nice=19L ## mc.surv.bart only
            )
```

#### **Arguments**

x.train

Explanatory variables for training (in sample) data.

Must be a matrix with (as usual) rows corresponding to observations and columns to variables.

surv.bart will generate draws of f(t,x) for each x which is a row of x.train (note that the definition of x.train is dependent on whether y.train has been specified; see below).

y.train

Binary response dependent variable for training (in sample) data.

If y.train is NULL, then y.train (x.train and x.test, if specified) are generated by a call to surv.pre.bart (which require that times and delta be provided: see below); otherwise, y.train (x.train and x.test, if specified) are utilized as given assuming that the data construction has already been performed.

times

The time of event or right-censoring.

If y.train is NULL, then times (and delta) must be provided.

delta The event indicator: 1 is an event while 0 is censored.

If y. train is NULL, then delta (and times) must be provided.

x. test Explanatory variables for test (out of sample) data.

Must be a matrix and have the same structure as x.train.

surv. bart will generate draws of f(t, x) for each x which is a row of x.test.

K If provided, then coarsen times per the quantiles 1/K, 2/K, ..., K/K.

events If provided, then use for the grid of time points.

ztimes If provided, then these columns of x.train (and x.test if any) are the times

for time-dependent covariates. They will be transformed into time-dependent

covariate sojourn times.

zdelta If provided, then these columns of x.train (and x.test if any) are the delta

for time-dependent covariates. They will be transformed into time-dependent

covariate binary events.

sparse Whether to perform variable selection based on a sparse Dirichlet prior rather

than simply uniform; see Linero 2016.

theta Set *theta* parameter; zero means random.

omega Set *omega* parameter; zero means random.

a Sparse parameter for Beta(a,b) prior: 0.5 <= a <= 1 where lower values

inducing more sparsity.

b Sparse parameter for Beta(a, b) prior; typically, b = 1.

rho Sparse parameter: typically rho = p where p is the number of covariates under

consideration.

augment Whether data augmentation is to be performed in sparse variable selection.

xinfo You can provide the cutpoints to BART or let BART choose them for you. To

provide them, use the xinfo argument to specify a list (matrix) where the items (rows) are the covariates and the contents of the items (columns) are the cut-

points.

usequants If usequants=FALSE, then the cutpoints in xinfo are generated uniformly; oth-

erwise, if TRUE, uniform quantiles are used for the cutpoints.

rm.const Whether or not to remove constant variables.

type Whether to employ Albert-Chib, 'pbart', or Holmes-Held, 'lbart'.

ntype The integer equivalent of type where 'wbart' is 1, 'pbart' is 2 and 'lbart'

is 3.

k is the number of prior standard deviations f(t,x) is away from +/-3. The

bigger k is, the more conservative the fitting will be.

power Power parameter for tree prior.

Base parameter for tree prior.

offset With binary BART, the centering is P(Y = 1|x) = F(f(x) + offset) where

offset defaults to F^{-1}(mean(y.train)). You can use the offset parame-

ter to over-ride these defaults.

tau.num The numerator in the tau definition, i.e., tau=tau.num/(k\*sqrt(ntree)).

ntree The number of trees in the sum.

ndpost The number of posterior draws returned.

nskip Number of MCMC iterations to be treated as burn in.

printevery As the MCMC runs, a message is printed every printevery draws.

keepevery Every keepevery draw is kept to be returned to the user.

A "draw" will consist of values  $f^*(t, x)$  at x = rows from the train(optionally)

and test data, where  $f^*$  denotes the current draw of f.

numcut The number of possible values of c (see usequants). If a single number if given,

this is used for all variables. Otherwise a vector with length equal to ncol(x.train) is required, where the  $i^{th}$  element gives the number of c used for the  $i^{th}$  variable in x.train. If usequants is false, numcut equally spaced cutoffs are used covering the range of values in the corresponding column of x.train. If usequants is true, then min(numcut, the number of unique values in the corresponding columns of

x.train - 1) c values are used.

id surv.bart only: unique identifier added to returned list.
seed mc.surv.bart only: seed required for reproducible MCMC.

mc.cores mc.surv.bart only: number of cores to employ in parallel.

nice mc.surv.bart only: set the job niceness. The default niceness is 19: niceness

goes from 0 (highest) to 19 (lowest).

#### Value

surv.bart returns an object of type survbart which is essentially a list. Besides the items listed below, the list has a binaryOffset component giving the value used, a times component giving the unique times, K which is the number of unique times, tx.train and tx.test, if any.

yhat.train A matrix with ndpost rows and nrow(x.train) columns. Each row corresponds

to a draw  $f^*$  from the posterior of f and each column corresponds to a row of x.train. The (i,j) value is  $f^*(t,x)$  for the  $i^{th}$  kept draw of f and the  $j^{th}$  row of

x.train.

Burn-in is dropped.

yhat.test Same as yhat.train but now the x's are the rows of the test data.

surv. test The survival function, S(t|x), where x's are the rows of the test data.

yhat.train.mean

train data fits = mean of yhat.train columns.

yhat.test.mean test data fits = mean of yhat.test columns.

surv.test.mean mean of surv.test columns.

varcount a matrix with ndpost rows and nrow(x.train) columns. Each row is for a draw.

For each variable (corresponding to the columns), the total count of the number of times that variable is used in a tree decision rule (over all trees) is given.

Note that yhat.train and yhat.test are f(t,x) + binaryOffset. If you want draws of the probability P(Y=1|t,x) you need to apply the normal cdf (pnorm) to these values.

## See Also

```
surv.pre.bart
```

```
## load survival package for the advanced lung cancer example
data(lung)
N <- length(lung$status)</pre>
table(lung$ph.karno, lung$pat.karno)
## if physician's KPS unavailable, then use the patient's
h <- which(is.na(lung$ph.karno))</pre>
lung$ph.karno[h] <- lung$pat.karno[h]</pre>
times <- lung$time</pre>
delta <- lung$status-1 ##lung$status: 1=censored, 2=dead</pre>
##delta: 0=censored, 1=dead
## this study reports time in days rather than weeks or months
## coarsening from days to weeks or months will reduce the computational burden
##times <- ceiling(times/30)</pre>
times <- ceiling(times/7) ## weeks</pre>
table(times)
table(delta)
## matrix of observed covariates
x.train <- cbind(lung$sex, lung$age, lung$ph.karno)</pre>
                     Male=1 Female=2
## lung$sex:
## lung$age:
                    Age in years
## lung$ph.karno: Karnofsky performance score (dead=0:normal=100:by=10)
                     rated by physician
dimnames(x.train)[[2]] \leftarrow c('M(1):F(2)', 'age(39:82)', 'ph.karno(50:100:10)')
table(x.train[ , 1])
summary(x.train[ , 2])
table(x.train[ , 3])
##test BART with token run to ensure installation works
set.seed(99)
post <- surv.bart(x.train=x.train, times=times, delta=delta,</pre>
                  nskip=1, ndpost=1, keepevery=1)
## Not run:
## run one long MCMC chain in one process
## set.seed(99)
## post <- surv.bart(x.train=x.train, times=times, delta=delta, x.test=x.test)</pre>
```

surv.pre.bart 129

```
## in the interest of time, consider speeding it up by parallel processing
## run "mc.cores" number of shorter MCMC chains in parallel processes
post <- mc.surv.bart(x.train=x.train, times=times, delta=delta,</pre>
                      mc.cores=8, seed=99)
pre <- surv.pre.bart(times=times, delta=delta, x.train=x.train,</pre>
                      x.test=x.train)
K <- pre$K
M <- nrow(post$yhat.train)</pre>
pre$tx.test <- rbind(pre$tx.test, pre$tx.test)</pre>
pre$tx.test[ , 2] <- c(rep(1, N*K), rep(2, N*K))
## sex pushed to col 2, since time is always in col 1
pred <- predict(post, newdata=pre$tx.test, mc.cores=8)</pre>
pd <- matrix(nrow=M, ncol=2*K)</pre>
for(j in 1:K) {
    h \leftarrow seq(j, N*K, by=K)
    pd[ , j] <- apply(pred$surv.test[ , h], 1, mean)</pre>
    pd[ , j+K] <- apply(pred$surv.test[ , h+N*K], 1, mean)</pre>
}
pd.mu <- apply(pd, 2, mean)
pd.025 <- apply(pd, 2, quantile, probs=0.025)
pd.975 <- apply(pd, 2, quantile, probs=0.975)
males <- 1:K
females <- males+K
plot(c(0, pre$times), c(1, pd.mu[males]), type='s', col='blue',
     ylim=0:1, ylab='S(t, x)', xlab='t (weeks)',
     main=paste('Advanced Lung Cancer ex. (BART::lung)',
                 "Friedman's partial dependence function",
                 'Male (blue) vs. Female (red)', sep='\n'))
lines(c(0, pre\frac{1}{2}times), c(1, pd.025[males]), col='blue', type='s', lty=2)
lines(c(0, pre$times), c(1, pd.975[males]), col='blue', type='s', lty=2)
lines(c(0, pre$times), c(1, pd.mu[females]), col='red', type='s')
lines(c(0, pre\frac{1}{2}times), c(1, pd.025[females]), col='red', type='s', lty=2)
lines(c(0, pre$times), c(1, pd.975[females]), col='red', type='s', lty=2)
## End(Not run)
```

surv.pre.bart

# **Description**

Survival data contained in  $(t, \delta, x)$  must be translated to data suitable for the BART survival analysis model; see surv.bart for more details.

# Usage

# Arguments

times	The time of event or right-censoring.
delta	The event indicator: 1 is an event while 0 is censored.
x.train	Explanatory variables for training (in sample) data. If provided, must be a matrix with (as usual) rows corresponding to observations and columns to variables.
x.test	Explanatory variables for test (out of sample) data. If provided, must be a matrix and have the same structure as x.train.
K	If provided, then coarsen times per the quantiles $1/K, 2/K,, K/K$ .
events	If provided, then use for the grid of time points.
ztimes	If provided, then these columns of $x.train$ (and $x.test$ if any) are the times for time-dependent covariates. They will be transformed into time-dependent covariate sojourn times.
zdelta	If provided, then these columns of $x.train$ (and $x.test$ if any) are the delta for time-dependent covariates. They will be transformed into time-dependent covariate binary events.

# Value

surv.pre.bart returns a list. Besides the items listed below, the list has a times component giving the unique times and K which is the number of unique times.

y.train	A vector of binary responses.
tx.train	A matrix with rows consisting of time and the covariates of the training data.
tx.test	A matrix with rows consisting of time and the covariates of the test data, if any.

# See Also

surv.bart

transplant 131

## **Examples**

```
## load the advanced lung cancer example
data(lung)
group \leftarrow -which(is.na(lung[ , 7]))  ## remove missing row for ph.karno
times <- lung[group, 2] ##lung$time</pre>
delta <- lung[group, 3]-1 ##lung$status: 1=censored, 2=dead</pre>
                           ##delta: 0=censored, 1=dead
summary(times)
table(delta)
x.train <- as.matrix(lung[group, c(4, 5, 7)]) ## matrix of observed covariates
## lung$age:
               Age in years
## lung$sex:
                    Male=1 Female=2
## lung$ph.karno: Karnofsky performance score (dead=0:normal=100:by=10)
                     rated by physician
dimnames(x.train)[[2]] \leftarrow c('age(yr)', 'M(1):F(2)', 'ph.karno(0:100:10)')
summary(x.train[ , 1])
table(x.train[ , 2])
table(x.train[ , 3])
x.test <- matrix(nrow=84, ncol=3) ## matrix of covariate scenarios</pre>
dimnames(x.test)[[2]] <- dimnames(x.train)[[2]]</pre>
i <- 1
for(age in 5*(9:15)) for(sex in 1:2) for(ph.karno in 10*(5:10)) {
    x.test[i, ] <- c(age, sex, ph.karno)</pre>
    i <- i+1
}
pre <- surv.pre.bart(times=times, delta=delta, x.train=x.train, x.test=x.test)</pre>
str(pre)
```

transplant

Liver transplant waiting list

# Description

Subjects on a liver transplant waiting list from 1990-1999, and their disposition: received a transplant, died while waiting, withdrew from the list, or censored.

## Usage

```
data("transplant")
```

#### **Format**

A data frame with 815 observations on the following 6 variables.

age age at addition to the waiting list

sex morf

abo blood type: A, B, AB or 0

year year in which they entered the waiting list

futime time from entry to final disposition

event final disposition: censored, death, ltx or withdraw

#### **Details**

This represents the transplant experience in a particular region, over a time period in which liver transplant became much more widely recognized as a viable treatment modality. The number of liver transplants rises over the period, but the number of subjects added to the liver transplant waiting list grew much faster. Important questions addressed by the data are the change in waiting time, who waits, and whether there was an consequent increase in deaths while on the list.

Blood type is an important consideration. Donor livers from subjects with blood type O can be used by patients with A, B, AB or O blood types, whereas a donor liver from the other types will only be transplanted to a matching recipient. Thus type O subjects on the waiting list are at a disadvantage, since the pool of competitors is larger for type O donor livers.

This data is of historical interest and provides a useful example of competing risks, but it has little relevance to current practice. Liver allocation policies have evolved and now depend directly on each individual patient's risk and need, assessments of which are regularly updated while a patient is on the waiting list. The overall organ shortage remains acute, however.

#### References

Kim WR, Therneau TM, Benson JT, Kremers WK, Rosen CB, Gores GJ, Dickson ER. Deaths on the liver transplant waiting list: An analysis of competing risks. Hepatology 2006 Feb; 43(2):345-51.

wbart

BART for continuous outcomes

# **Description**

```
BART is a Bayesian "sum-of-trees" model. For a numeric response y, we have y=f(x)+\epsilon, where \epsilon \sim N(0,\sigma^2).
```

f is the sum of many tree models. The goal is to have very flexible inference for the uknown function f.

In the spirit of "ensemble models", each tree is constrained by a prior to be a weak learner so that it contributes a small amount to the overall fit.

## Usage

```
wbart(
   x.train, y.train, x.test=matrix(0.0,0,0),
   sparse=FALSE, theta=0, omega=1,
   a=0.5, b=1, augment=FALSE, rho=NULL,
   xinfo=matrix(0.0,0,0), usequants=FALSE,
   cont=FALSE, rm.const=TRUE,
   sigest=NA, sigdf=3, sigquant=.90,
   k=2.0, power=2.0, base=.95,
   sigmaf=NA, lambda=NA,
   fmean=mean(y.train), w=rep(1,length(y.train)),
   ntree=200L, numcut=100L,
   ndpost=1000L, nskip=100L, keepevery=1L,
   nkeeptrain=ndpost, nkeeptest=ndpost,
   nkeeptestmean=ndpost, nkeeptreedraws=ndpost,
   printevery=100L, transposed=FALSE
)
```

#### **Arguments**

x.train Explanatory variables for training (in sample) data.

May be a matrix or a data frame, with (as usual) rows corresponding to observations and columns to variables

vations and columns to variables.

If a variable is a factor in a data frame, it is replaced with dummies. Note that q dummies are created if q>2 and one dummy is created if q=2, where q is the number of levels of the factor. whart will generate draws of f(x) for each x which is a row of x.train.

y.train Continuous dependent variable for training (in sample) data.

x. test Explanatory variables for test (out of sample) data.

Should have same structure as x.train.

wbart will generate draws of f(x) for each x which is a row of x.test.

sparse Whether to perform variable selection based on a sparse Dirichlet prior rather

than simply uniform; see Linero 2016.

theta Set *theta* parameter; zero means random.

omega Set *omega* parameter; zero means random.

a Sparse parameter for Beta(a,b) prior:  $0.5 \le a \le 1$  where lower values

inducing more sparsity.

b Sparse parameter for Beta(a, b) prior; typically, b = 1.

rho Sparse parameter: typically rho = p where p is the number of covariates under

consideration.

augment Whether data augmentation is to be performed in sparse variable selection.

xinfo You can provide the cutpoints to BART or let BART choose them for you. To

provide them, use the xinfo argument to specify a list (matrix) where the items (rows) are the covariates and the contents of the items (columns) are the cut-

points.

usequants If usequants=FALSE, then the cutpoints in xinfo are generated uniformly; oth-

erwise, if TRUE, uniform quantiles are used for the cutpoints.

cont Whether or not to assume all variables are continuous.

rm. const Whether or not to remove constant variables.

signst The prior for the error variance ( $\sigma^2$ ) is inverted chi-squared (the standard con-

ditionally conjugate prior). The prior is specified by choosing the degrees of freedom, a rough estimate of the corresponding standard deviation and a quantile to put this rough estimate at. If sigest=NA then the rough estimate will be the usual least squares estimator. Otherwise the supplied value will be used.

sigdf Degrees of freedom for error variance prior.

signuant The quantile of the prior that the rough estimate (see signst) is placed at. The

closer the quantile is to 1, the more aggresive the fit will be as you are putting more prior weight on error standard deviations  $(\sigma)$  less than the rough estimate.

k For numeric y, k is the number of prior standard deviations E(Y|x) = f(x) is

away from +/-.5. k is the number of prior standard deviations f(x) is away from

+/-3. The bigger k is, the more conservative the fitting will be.

power Power parameter for tree prior.

base Base parameter for tree prior.

sigmaf The SD of f.

lambda The scale of the prior for the variance.

fmean BART operates on y. train centered by fmean.

w Vector of weights which multiply the standard deviation.

ntree The number of trees in the sum.

numcut The number of possible values of c (see usequants). If a single number if given,

this is used for all variables. Otherwise a vector with length equal to  $\operatorname{ncol}(x.\operatorname{train})$  is required, where the  $i^{th}$  element gives the number of c used for the  $i^{th}$  variable in x.train. If usequants is false, numcut equally spaced cutoffs are used covering the range of values in the corresponding column of x.train. If usequants is true, then  $\min(\operatorname{numcut})$ , the number of unique values in the corresponding columns of

x.train - 1) c values are used.

ndpost The number of posterior draws returned.

nskip Number of MCMC iterations to be treated as burn in.

Number of MCMC iterations to be returned for train data.

Number of MCMC iterations to be returned for test data.

Number of MCMC iterations to be returned for test mean.

Number of MCMC iterations to be returned for tree draws.

printevery As the MCMC runs, a message is printed every printevery draws.

keepevery Every keepevery draw is kept to be returned to the user.

transposed When running wbart in parallel, it is more memory-efficient to transpose x.train

and x. test, if any, prior to calling mc.wbart.

#### **Details**

BART is an Bayesian MCMC method. At each MCMC interation, we produce a draw from the joint posterior  $(f, \sigma)|(x, y)$  in the numeric y case.

Thus, unlike a lot of other modelling methods in R, we do not produce a single model object from which fits and summaries may be extracted. The output consists of values  $f^*(x)$  (and  $\sigma^*$  in the numeric case) where \* denotes a particular draw. The x is either a row from the training data (x.train) or the test data (x.test).

#### Value

wbart returns an object of type wbart which is essentially a list. In the numeric y case, the list has components:

yhat.train A matrix with ndpost rows and nrow(x.train) columns. Each row corresponds

to a draw  $f^*$  from the posterior of f and each column corresponds to a row of x.train. The (i,j) value is  $f^*(x)$  for the  $i^{th}$  kept draw of f and the  $j^{th}$  row of

x.train.

Burn-in is dropped.

yhat.test Same as yhat.train but now the x's are the rows of the test data.

yhat.train.mean

train data fits = mean of yhat.train columns.

yhat.test.mean test data fits = mean of yhat.test columns.

sigma post burn in draws of sigma, length = ndpost.

first.sigma burn-in draws of sigma.

varcount a matrix with ndpost rows and nrow(x.train) columns. Each row is for a draw.

For each variable (corresponding to the columns), the total count of the number of times that variable is used in a tree decision rule (over all trees) is given.

sigest The rough error standard deviation  $(\sigma)$  used in the prior.

#### See Also

pbart

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```
##test BART with token run to ensure installation works
set.seed(99)
bartFit = wbart(x,y,nskip=5,ndpost=5)

## Not run:
##run BART
set.seed(99)
bartFit = wbart(x,y)

##compare BART fit to linear matter and truth = Ey
fitmat = cbind(y,Ey,lmFit$fitted,bartFit$yhat.train.mean)
colnames(fitmat) = c('y','Ey','lm','bart')
print(cor(fitmat))

## End(Not run)
```

xdm20.test

A data set used in example of recur.bart.

# Description

A matrix containing a 20% random sample of the testing set for a real data example of recurrent events survival analysis. There are 100 patients in the cohort: 50 in the training set and 50 in the testing set. See the Reference below (and the References therein) for more detailed information; a brief synopsis follows.

xdm20.test contains both the training set and the testing set. There are 798 unique time points so there are 50\*798=39900 rows of the training set followed by 50\*798=39900 rows of the testing set. For patient's who died prior to the end of follow-up, their external factors are last value carried forward. Therefore, we can use xdm20.test to estimate the cumulative hazard for all patients for all time points.

The full data set, xdm.test, can be obtained online at https://www.mcw.edu/-/media/MCW/Departments/Biostatistics/tr064zip.zip There are 488 patients in the full cohort: 235 in the training set and 253 in the testing set.

xdm. test contains both the training set and the testing set. There are 798 unique time points so there are 235\*798=187530 rows of the training set followed by 253\*798=201894 rows of the testing set. For patient's who died prior to the end of follow-up, their external factors are last value carried forward.

#### Usage

```
data(xdm20.test)
```

## References

Sparapani, Rein, Tarima, Jackson, Meurer (2020). Non-parametric recurrent events analysis with BART and an application to the hospital admissions of patients with diabetes. *Biostatistics* doi:10.1093/biostatistics/kxy032

xdm20.train

#### See Also

xdm20.train

# **Examples**

```
data(xdm20.test)
head(xdm20.test[ , 1:10])
```

xdm20.train

A real data example for recur.bart.

#### **Description**

A matrix containing a 20% random sample of the training set for a real data example of recurrent events survival analysis. There are 100 patients in the cohort: 50 in the training set and 50 in the testing set. The full data set, xdm.train, can be obtained online at https://www.mcw.edu/-/media/MCW/Departments/Biostatistics/tr064zip.zip There are 488 patients in the full cohort: 235 in the training set and 253 in the testing set. See the Reference below (and the References therein) for more detailed information; a brief synopsis follows.

We explored the hospital admissions for a cohort of patients with diabetes cared for by the Froedtert and Medical College of Wisconsin health network. These patients were identified via their Electronic Health Records (EHR) which include vital signs, diagnoses, procedures, laboratory values, pharmacy orders and billing data. This human subjects research and de-identified data release was approved by the Medical College of Wisconsin and Froedtert Hospital joint Institutional Review Board. To maintain patient privacy, roughly one fourth of patients were randomly sampled for inclusion as well as other de-identification procedures.

We identified likely incident diabetes mellitus type 2 patients by tabulating their first diagnosis code of primary diabetes (ICD-9 codes 250.x0 and 250.x2) in 2006 or 2007, i.e., no such codes were found for these patients prior to 2006 for as far back as each patient's records go which is variable. We restricted the population to adults aged 21 to 90 by 01/01/2008. Among the patients treated in this health system, the vast majority were racially self-identified as either white or black so our inclusion criteria is restricted to these groups. Since our interest is in patients with primary diabetes, we excluded those patients who were diagnosed with either secondary diabetes or gestational diabetes.

For this cohort, we identified every hospital admission between 01/01/2008 and 12/31/2012. For convenience, follow-up begins on 01/01/2008, rather than from each patient's actual incident diagnosis date which varied over the preceding 2 years. Following all patients concurrently allows us to temporally adapt, via our model, for seasonal/epidemic hospital admissions such as the H1N1 influenza outbreak in the US from April to June 2009.

We investigated the following risk factors: gender, race, age, insurance status (commercial, government or other), diabetes therapy (insulin, metformin and/or sulfonylurea), health care charges, relative value units (RVU), vital signs, laboratory values, comorbidity/complication diagnoses and procedures/surgeries (we will refer to vital signs and laboratory values collectively as signs; and comorbidity/complication diagnoses and procedures/surgeries collectively as conditions). In total, we considered 85 covariates of which 82 are external factors as described above and three are temporal

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factors: time, t, the counting process,  $N_i(t-)$ , and the sojourn time,  $v_i(t)$ . Among these potential predictors only gender, race and age are time-independent. The rest are defined as last value carried forward.

For insulin, metformin and sulfonylurea, we only had access to prescription orders (rather than prescription fills) and self-reported current status of prescription therapy during clinic office visits. Since, generally, orders are only required after every three fills, and each fill can be for up to 90 days, we define insulin, metformin and sulfonylurea as binary indicators which are one if there exists an order or current status indication within the prior 270 days; otherwise zero.

Health care charges and relative value units (RVU) are measures related to the services and procedures delivered. However, they are so closely related that recent charges/RVUs are of no practical value in this analysis. For example, just prior to a patient's hospital admission on a non-emergent basis, they often have a series of diagnostic tests and imaging. Similarly, for an emergent admission, the patient is often seen in the emergency department just prior to admission where similar services are conducted. We do not consider these charges/RVUs predictive of an admission because we are interested in identifying preventive opportunities. Therefore, we investigate charges/RVUs that are the sum total of the following moving windows of days prior to any given date: 31 to 90, 91 to 180, 181 to 300.

For many patients, some signs were not available for a given date so they were imputed; similarly, if a sign was not observed within the last 180 days, then it was imputed (except for height which never expires, weight extended to 365 days and body mass index which is a deterministic function of the two). We utilized the Sequential BART missing imputation method. However, instead of creating several imputed data sets, we imputed a new sign at each date when it was missing, i.e., in order to properly address uncertainty within one data set, a new value was imputed for each date that it was missing and never carried forward.

Conditions are binary indicators which are zero until the date of the first coding and then they are one from then on. Based on clinical rationale, we identified 26 conditions (23 comorbidities and 3 procedures/surgeries) which are potential risk factors for a hospital admission many of which are possible complications of diabetes; besides clinical merit, these conditions were chosen since they are present in more than just a few subjects so that they may be informative. Similarly, we employed 15 general conditions which are the Charlson diagnoses and 18 general conditions from the RxRisk adult diagnoses which are defined by prescription orders. Seven conditions are a composite of diagnosis codes and prescription orders.

#### Usage

data(xdm20.train)

#### References

Sparapani, Rein, Tarima, Jackson, Meurer (2020). Non-parametric recurrent events analysis with BART and an application to the hospital admissions of patients with diabetes. *Biostatistics* doi:10.1093/biostatistics/kxy032

#### See Also

xdm20.test

ydm20.train 139

## **Examples**

```
data(xdm20.train)
head(xdm20.train[ , 1:10])
```

ydm20.train

A data set used in example of recur.bart.

### **Description**

Two vectors containing the training and testing set outcomes for a 20% random sample for a real data example of recurrent events survival analysis. There are 100 patients in the cohort: 50 in the training set and 50 in the testing set. See the Reference below (and the References therein) for more detailed information; a brief synopsis follows.

ydm20. train contains the training set only. ydm20. test is provided for completeness; it contains both the training set and the testing set. There are 798 unique time points so there are 50\*798=39900 rows of the training set followed by 50\*798=39900 rows of the testing set.

The full data sets, ydm. train and ydm. test, can be obtained online at https://www.mcw.edu/-/media/MCW/Departments/Biostatistics/tr064zip.zip There are 488 patients in the full co-hort: 235 in the training set and 253 in the testing set.

ydm. train contains the training set only. ydm. test contains both the training set and the testing set. There are 798 unique time points so there are 235\*798=187530 rows of the training set followed by 253\*798=201894 rows of the testing set.

# Usage

```
data(ydm20.train)
data(ydm20.test)
```

#### References

Sparapani, Rein, Tarima, Jackson, Meurer (2020). Non-parametric recurrent events analysis with BART and an application to the hospital admissions of patients with diabetes. *Biostatistics* doi:10.1093/biostatistics/kxy032

#### See Also

xdm20.train

```
data(ydm20.train)
data(ydm20.test)
table(ydm20.train)
table(ydm20.test)
```

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